

# A physics-based high-resolution BIPV model for building performance simulations

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## Abstract

Building integrated photovoltaic (BIPV) systems are considered a promising solution to increase the share of renewable energy in the built environment. To evaluate the BIPV performance at the building level, the implementation of BIPV models in building performance simulation tools is an essential step. This paper presents the development of a multi-physics BIPV model for the simulation of BIPV facades within the openIDEAS framework for building and district energy simulations. The model couples a high-resolution electrical model to physics-based thermal and airflow models. The combination of these two modelling approaches is not common in BIPV models, particularly for building performance simulations. The model predictions are compared to three months of experimental data from a naturally ventilated BIPV module installed in the facade of a test building in Leuven, Belgium. A good agreement is obtained in terms of both BIPV energy yield and temperature. The error in daily energy yield estimations is on average below 3 % and the error in the monthly energy yield is below 2 %. The back-of-module temperature is predicted with a MAE lower than 2 °C and RMSE lower than 5 °C.

*Keywords:* Building integrated photovoltaic (BIPV), Building performance simulation (BPS), Energy yield, Temperature, Natural ventilation

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## 1. Introduction

One of the main challenges concerning energy use and greenhouse gas emissions is the future sustainability of urban areas. Worldwide, nations have set strategic plans to promote the deployment of renewable energy and reduce the CO<sub>2</sub> emissions related to the built environment. In the European Union, the Energy Performance of Buildings Directive (Directive 2010/31/EU) states that all new buildings must be nearly zero-energy buildings (NZEB) by 2021 and supports, in parallel, the transformation of existing buildings into NZEBs (EPBD, 2010). In China, the government issued the China Act on the Energy Efficiency of Civil Buildings to promote energy efficiency and decrease the energy consumption in buildings (Ma et al., 2018). Equally important energy policies have been defined in Latin American countries, such as Argentina, Brazil, Chile and Uruguay (Silvero et al., 2018).

In addition to improving the energy efficiency of buildings, the deployment of renewable energy sources in the built environment is a key step towards the reduction of fossil fuels consumption in the building sector. Photovoltaic (PV) technology is particularly suitable as renewable energy source in view of its stable market increase and price reduction (Masson & Brunisholz, 2015). PV modules have usually been used in the built environment as open-rack installations on building roofs (Sánchez-Pantoja et al., 2018), which classify them as building applied photovoltaic (BAPV). BAPVs are not commonly employed on building facades, mainly due to aesthetic reasons (Aguacil et al., 2019).

Alternatively, the concept of building integrated photovoltaic (BIPV) concerns the use of PV elements as part of the building envelope. Besides generating electricity, BIPV modules perform at least one additional function, such as insulation, weather barrier or sun shading (Osseweijer et al., 2018). By replacing conventional building components, BIPVs provide savings in land, materials and construction time (Jelle et al., 2012). The assimilation of PV into the building architectural concept is also facilitated (Saretta et al., 2018; Aguacil et al.,

2019). The prospect to exploit additional surfaces for renewable energy generation in the built environment makes BIPV a key technology to comply with the increasingly stricter building energy policies. In particular, facade integration is considered a promising BIPV application, complementing the limited roof surface area (Osseweijer et al., 2018). BIPV facades can also provide a balanced power generation profile over the day, with relatively higher energy production in the early and late daylight hours (Redweik et al., 2013; Brito et al., 2017; Díez-Mediavilla et al., 2019).

Over the recent years, a significant effort has been invested in the development of BIPV models, as reviewed by Norton et al. (2011), Agathokleous & Kalogirou (2016), Yang & Athienitis (2016) and Biyik et al. (2017). Concerning the level of detail of the BIPV models, two trends are observed. On the one hand, BIPV models that propose a detailed physics-based thermal modelling often employ a simplified electrical model, assuming that the PV efficiency decreases linearly with increasing operating temperature, e.g. Assoa & Ménézo (2014), Ioannidis et al. (2017) Athienitis et al. (2018), Assoa et al. (2018), Ghosh et al. (2019), Alrashidi et al. (2020). On the other hand, BIPV models that propose a high-resolution electrical model either employ a simplified thermal model, e.g. Tsai (2010), d’Alessandro et al. (2015), Hofer et al. (2016), Sprenger et al. (2016), Gallardo-Saavedra & Karlsson (2018) and Walker et al. (2019), and/or focus on stand alone PV modules, e.g. Tsai (2010), d’Alessandro et al. (2015), Goverde et al. (2017) and Horváth et al. (2018). Moreover, most of high-resolution (BI)PV models are developed in software dedicated to the simulation of electrical circuits, such as PSPICE or LTSpice (e.g. Tsai (2010); d’Alessandro et al. (2015); Goverde et al. (2017); Horváth et al. (2018); Gallardo-Saavedra & Karlsson (2018)). Although such circuit-based environments can be used to represent the thermal behaviour of PV modules, they are not particularly suitable for building performance simulations.

Another important aspect that deserves further attention is the influence of the wind flow on the heat dissipation conditions in BIPV elements. As research on wind flow in the built environment progresses, new insights on how the wind

affects the convective heat dissipation in buildings have been published (Emmel et al., 2007; Defraeye et al., 2011; Mirsadeghi et al., 2013; Montazeri et al., 2015; Montazeri & Blocken, 2017, 2018; Iousef et al., 2019). In particular, it has been demonstrated that convective heat transfer coefficients resulting from wind effects not only vary over the building surfaces, but also depend on the building geometry (Montazeri et al., 2015; Montazeri & Blocken, 2017). However, BIPV models are often based on simplified models for the exterior convective heat transfer that only take the wind speed into account in a linear relationship, e.g. Assoa & Ménézo (2014) Buonomano et al. (2016) Athienitis et al. (2018) Assoa et al. (2018) Alrashidi et al. (2020). A further simplification is the use of a constant value for the convective heat transfer coefficient as considered by Hu et al. (2017). This means that other important factors that influence the wind flow around a building, such as the wind direction, the building surroundings or the building surface (i.e. roof vs. facade surfaces), are not considered.

This paper proposes a multi-physics BIPV model for the simulation of BIPV facades within a building performance simulation (BPS) environment. The model combines a high-resolution electrical modelling with a detailed physics-based thermal and airflow modelling, which is not common in BIPV modelling. The multi-physics BIPV model predictions are compared to experimental data from a naturally ventilated crystalline silicon (c-Si) BIPV module. The comparison is based on energy yield and temperature results. Simplified BIPV power and temperature models available in the literature are also included in the comparative analysis. The relevance and novelty of this work lies on the combination of four aspects, discussed next.

First, the multi-physics BIPV model is developed as an exterior wall component within IDEAS library, an open-source Modelica-based library for building performance simulations (BPS). Incorporating a BIPV model as a wall component into IDEAS enables the simulation of the whole building, considering the thermal coupling between the BIPV element and building interior. The importance of this BIPV-building coupling has been discussed by Athienitis et al. (2018). In contrast to circuit-based modelling environments, the multi-

domain nature of Modelica language enables the combination of high-resolution (circuit-based) electrical models with thermal and airflow models within the same modelling platform (avoiding the need for co-simulation or decoupled simulation).  
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Second, the multi-physics BIPV model represents an improvement over BIPV models available for building performance simulation, in particular concerning the high-resolution electrical modelling. The PV electrical modelling employed in building simulations is generally based on power models, e.g. (Miyazaki et al., 2005; Didoné & Wagner, 2013; Ng et al., 2013; Ioannidis et al., 2017; Athienitis et al., 2018; Sánchez-Palencia et al., 2019), which represent a simplified approach with specific limitations (Roberts et al., 2017). In addition, BPS tools typically assume that all (BI)PV modules within the array operate at maximum power point (MPP) and under the same conditions. This means that mismatch losses are not taken into account and, therefore, neither shading (intra-array) nor different electrical architectures can be simulated.  
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Third, the multi-physics BIPV model is based on detailed physics-based thermal and airflow models. A physics-based modelling provides the flexibility necessary to carry out modifications of the BIPV design, which is not possible when (semi-)empirical temperature models are employed, e.g. Walker et al. (2019) and Gallardo-Saavedra & Karlsson (2018). Furthermore, compared to existing BIPV models in the literature, the multi-physics BIPV model considers the following three additional factors in the exterior convective heat transfer modelling: the building geometry, the wind direction, and the building surface (i.e. roof, windward, leeward or side facades). Another differentiation is that the airflow modelling in this paper is based on the experimental pressure characterisation of the BIPV module. Such experiments are not always carried out in BIPV studies; instead, a theoretical approach is normally employed, e.g. Ioannidis et al. (2017).  
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Fourth, the multi-physics BIPV model predictions are compared to experimental data from a naturally ventilated BIPV module that is fully integrated into a test building. The full building integration guarantees realistic boundary  
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conditions for the BIPV operation (including realistic wind flow around a building). Note that BIPV setups are not always part of a realistic building structure, e.g. Ioannidis et al. (2017), Assoa et al. (2018), Agathokleous & Kalogirou (2018a), Agathokleous & Kalogirou (2018b), Walker et al. (2019) and Alrashidi et al. (2020). The comparative analysis also considers power predictions based on the linear power model and back-of-module temperature predictions based on (semi-)empirical correlations presented in the literature (Ross, 1976; Skoplaki et al., 2008; Skoplaki & Palyvos, 2009). The intention here is to assess possible differences between the results obtained from the multi-physics BIPV model and the results from these simplified models for the naturally ventilated BIPV module investigated in this paper.

This paper is structured as follows. The methodology is described in Section 2, starting with a general description of the BIPV module and the test building in Section 2.1. Next, Section 2.2 presents the multi-physics BIPV model in detail, covering thermal, airflow and electrical aspects. Section 2.3 describes the experimental setup used to monitor the weather conditions and the BIPV behaviour (power, temperature and heat flux measurements). Section 2.4 summarises the inputs used in the multi-physics BIPV model, including the experimental pressure characterisation. Section 3 presents the results of the comparative analysis between the experimental data, the multi-physics BIPV model, and the simplified models. Section 4 discusses the results and the limitations of the proposed multi-physics model, indicating the topics of ongoing and future research. Finally, the Section 5 concludes the paper.

## 2. Methodology

### 2.1. BIPV module and building description

A schematic representation of the naturally-ventilated BIPV module is presented in Figure 1. The BIPV module is composed of two PV mini-modules connected to a 14 cm cavity and a 15 cm Rockwool layer. Two openings of 0.58 x 0.05 m<sup>2</sup>, one at the bottom and one at the top, allow the exterior air to flow

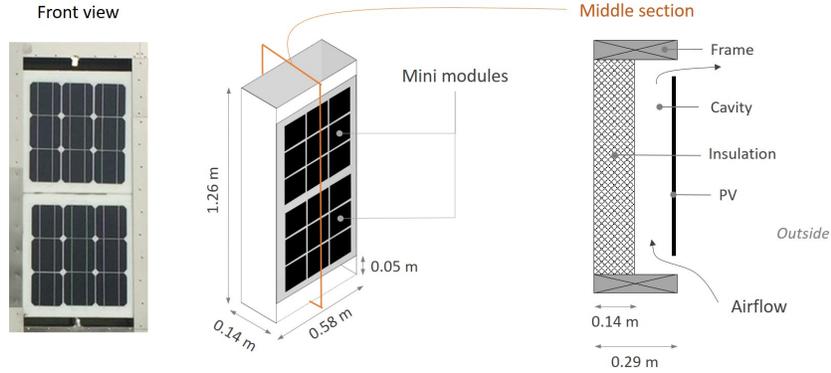


Figure 1: Front view and schematic representation of the BIPV module.

through the cavity to improve the heat dissipation. Each mini-module consists of nine monocrystalline silicon (c-Si) PV cells connected in series. The cells are encapsulated in a transparent EVA (ethyl vinyl acetate) layer at the front and in a white EVA layer at the back; both sides are covered with glass. The mini-modules that compose the BIPV module have been rated under standard test conditions (STC). Together, their power output is 70.6 W.

As shown in Figure 2a, the BIPV module was installed in the southwest facade of the Vliet test building in Leuven, Belgium ( $50^{\circ}52'N$ ,  $4^{\circ}41'E$ ), ensuring realistic indoor and outdoor conditions. The inclination of the facade is  $90^{\circ}$  and its azimuth angle is  $225^{\circ}$  (north as reference). Figure 2b shows that the building has a rectangular footprint and is located in an open environment, mostly free of shading events from the surroundings. The building facade where the BIPV module was installed is 4.3 m high and 25.2 m wide.

## 2.2. Multi-physics BIPV model

Figure 3 presents the control volume approach employed in the multi-physics BIPV model. A BIPV control volume corresponds to the dimensions of one PV cell and includes the following layers: glass, PV cell, glass, air volume, and building wall. EVA layers are not explicitly modelled due to their small thickness compared to the glass thickness. The PV cells are modelled explicitly

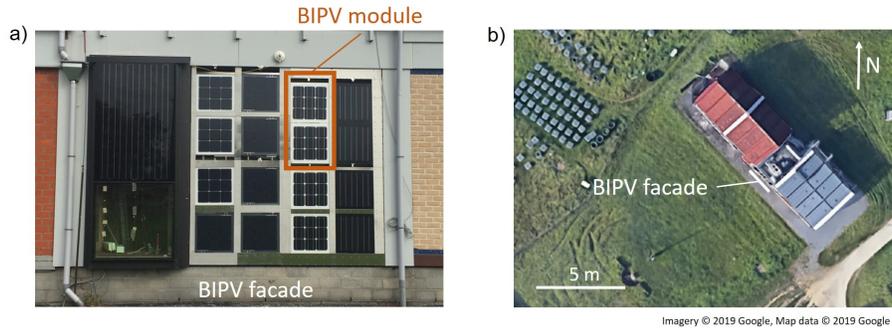


Figure 2: (a) The BIPV module integrated into the BIPV facade of the Vliet test building. (b) Surroundings of the Vliet test building (Google Maps image), indicating the BIPV southwest facade.

to enable the coupling between thermal and electrical model, which is achieved by using the PV cell to calculate the power output while imposing the generated power as a heat sink on the PV layer. The airflow through the cavity connects the BIPV control volume to one another.

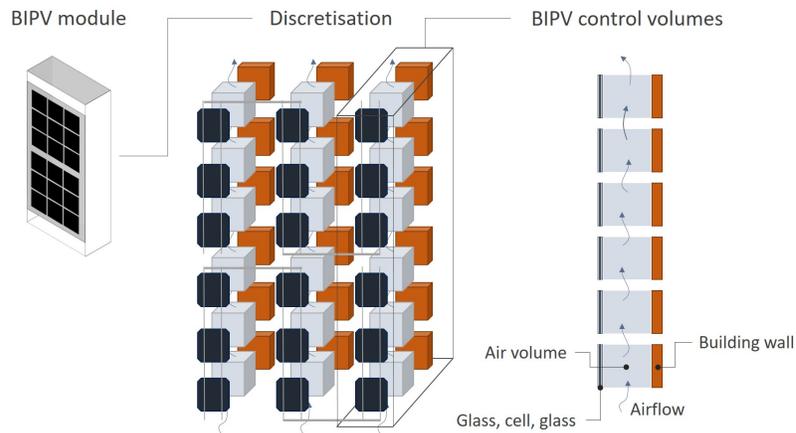


Figure 3: Control volume modelling approach applied to the ventilated BIPV module described in Section 2.1.

175 As illustrated in Figure 4, the multi-physics BIPV model was developed as an exterior wall component within IDEAS library, an open-source Modelica-based library for building performance simulations (BPS), part of the openIDEAS

environment. IDEAS provides transient models for the simulation of thermal and electrical systems at both building and feeder level. IDEAS models have  
 180 been verified against the IEA EBC BESTEST reference results and the IEA EBC Annex 58 Twin House experiments (Jorissen et al., 2018).

Figure 4 also illustrates the multi-physics structure of the BIPV model proposed in this paper, including electrical, thermal and airflow modelling. The couplings between electrical and thermal modelling, between thermal and air-  
 185 flow modelling as well as between the BIPV and the building zone are also indicated in this figure. The remainder of this section follows the same structure: the thermal modelling is described in Section 2.2.1, the airflow modelling in Section 2.2.2, and the electrical modelling in Section 2.2.3).

### 2.2.1. Thermal modelling

Figure 5 illustrates the different aspects of the thermal modelling that are  
 190 encapsulated in one BIPV control volume. In a BIPV module, only part of the solar irradiance is converted into electricity by the PV cells. Another relatively small part is reflected by the glass surface. Most of the energy is dissipated as heat to the exterior environment and to the cavity, in the form of conductive,  
 195 convective and radiative heat exchanges, described in detail here.

Conduction through the glass, PV cell and building wall is treated as a one-dimensional heat transfer problem, with conductive heat transfer computed as:

$$Q_{i,j} = G_{ij} (T_{i,j} - T_{i,j+1}) A \quad (1)$$

with the time-derivative:

$$C_{i,j} \frac{dT_{i,j}}{dt} = (Q_{i,j-1} - Q_{i,j}) A \quad (2)$$

where each material layer  $i$  consists of  $n_i$  time-dependent temperature states  $T_{i,j}(t)$  [K] with heat capacity  $C_{i,j}$  and  $n_i-1$  thermal conductors with thermal conductance  $G_{i,j}$ .  $C_{i,j}$  and  $G_{i,j}$  are computed assuming homogeneous material thermal properties over each element layer.  $A$  is the surface area of a BIPV  
 200 control volume.

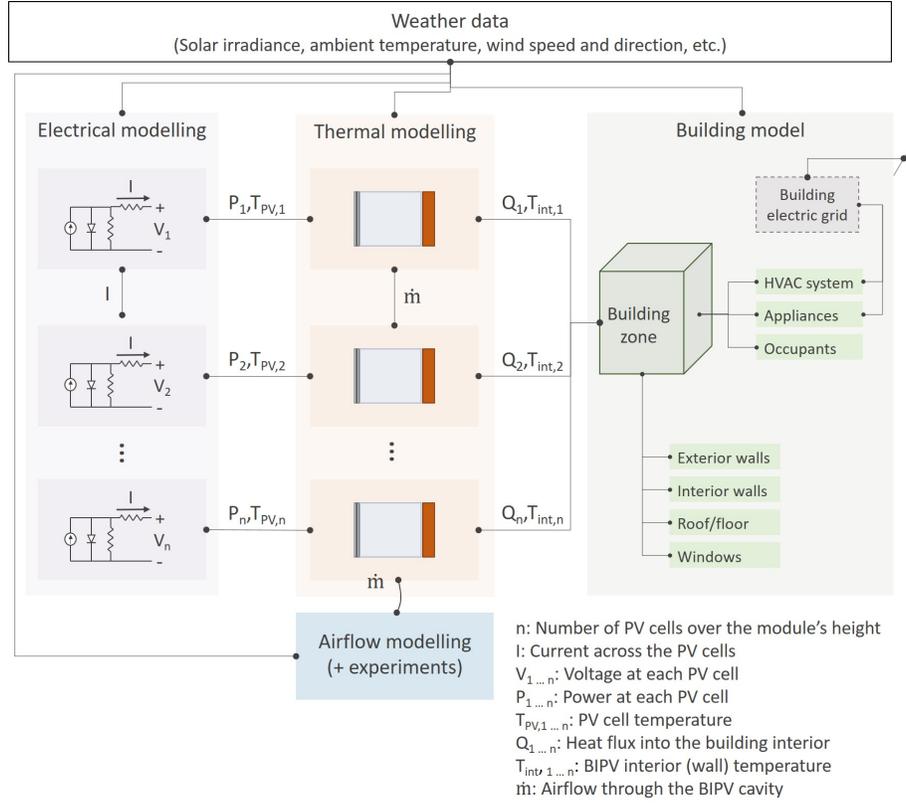


Figure 4: Multi-physics BIPV model composed of electrical, thermal and airflow modelling and integrated into the IDEAS environment.

As explained by Jorissen et al. (2018), the number of nodes  $n_i$  in each material layer is computed based on Wetter (2004), as follows:

$$n_i = \max\left(2, 3 \frac{\Pi_i}{\Pi_{\text{ref}}}\right) \quad (3)$$

with

$$\Pi = \frac{d}{\sqrt{\alpha}} \quad (4)$$

where  $\alpha$  is the thermal diffusivity of each layer  $i$ , and  $\Pi_{\text{ref}}$  is a reference value computed for a concrete slab of 20 cm.

For the PV layer, the PV power is included in Equation 2 as a heat sink (see

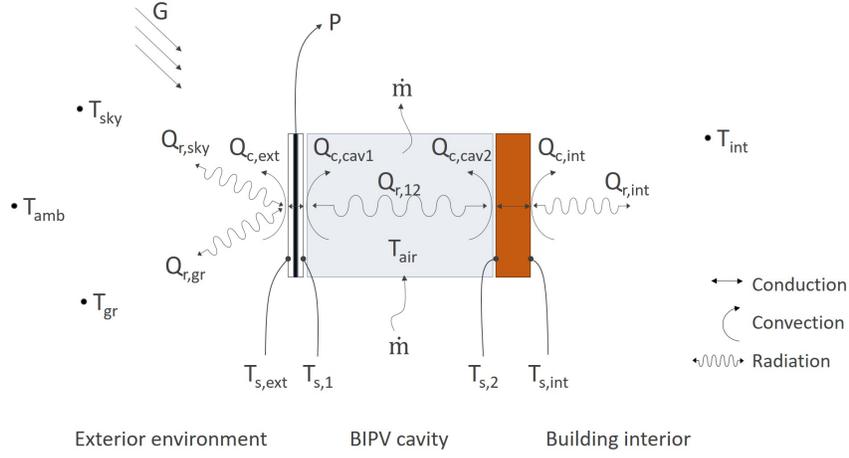


Figure 5: BIPV control volume, where  $G$  represents the solar irradiance,  $P$  represents the PV power as a heat sink,  $T$  [K] indicates temperatures at different locations,  $\dot{m}$  represents the airflow through the cavity, and  $Q$  indicates heat exchanges.

Section 2.2.3 for the electrical modelling). Note that edge effects and vertical  
 205 conduction between control volumes are not considered in the multi-physics  
 BIPV model.

The heat exchange with the exterior environment is composed of radiative and convective heat exchanges, as follows:

$$Q_{\text{ext}} = Q_{r,\text{sky}} + Q_{r,\text{gr}} + Q_{c,\text{ext}} \quad (5)$$

where  $Q_{r,\text{sky}}$  is the radiative heat transfer between the BIPV and the sky dome,  $Q_{r,\text{gr}}$  is the radiative heat transfer between the BIPV and the ground, and  $Q_{c,\text{ext}}$  is the convective heat transfer between the BIPV surface and the ambient air.

Assuming the sky dome and the ground as black bodies,  $Q_{r,\text{sky}}$  and  $Q_{r,\text{gr}}$  are defined as:

$$Q_{r,\text{sky}} = F_{\text{sky}} \varepsilon_{\text{ext}} \sigma (T_{s,\text{ext}}^4 - T_{\text{sky}}^4) A \quad (6)$$

and

$$Q_{r,\text{gr}} = F_{\text{gr}} \varepsilon_{\text{ext}} \sigma (T_{s,\text{ext}}^4 - T_{\text{gr}}^4) A \quad (7)$$

210 where  $T_{s,\text{ext}}$  is the temperature of the exterior glass surface,  $T_{\text{sky}}$  is the effective

sky temperature,  $T_{\text{gr}}$  is the ground temperature,  $F_{\text{sky}}$  is the view factor between the BIPV module and the sky,  $F_{\text{gr}}$  is the view factor between the BIPV module and the ground,  $\varepsilon_{\text{ext}}$  is the long-wave emissivity of the glass,  $\sigma$  is the Stefan-Boltzmann constant ( $= 5.67 \times 10^{-8} \text{ W/m}^2\text{K}^4$ ), and  $A$  is the surface area of a  
215 BIPV control volume.

The view factors  $F_{\text{sky}}$  and  $F_{\text{gr}}$  are calculated as:

$$F_{\text{sky}} = \frac{1 + \cos\beta}{2} \quad (8)$$

and

$$F_{\text{gr}} = \frac{1 - \cos\beta}{2} \quad (9)$$

where  $\beta$  is the inclination of the surface (equal to  $90^\circ$  for BIPV facades).

In the multi-physics BIPV model, the ground surface temperature is assumed equal to the ambient temperature ( $T_{\text{gr}} = T_{\text{amb}}$ ), and the sky temperature is based on the correlation proposed by Swinbank (1963):

$$T_{\text{sky}} = 0.0552T_{\text{amb}}^{1.5} \quad (10)$$

The exterior convective heat transfer,  $Q_{\text{c,ext}}$ , is defined as:

$$Q_{\text{c,ext}} = h_{\text{c,ext}}(T_{\text{s,ext}} - T_{\text{amb}})A \quad (11)$$

where  $h_{\text{c,ext}}$  is the exterior convective heat transfer coefficient and  $T_{\text{amb}}$  is the ambient temperature.

To model  $h_{\text{c,ext}}$ , the multi-physics BIPV model combines natural and forced convection as follows (Bergman et al., 2011):

$$h_{\text{c,ext}} = \left( h_{\text{c,f}}^3 + h_{\text{c,n}}^3 \right)^{\frac{1}{3}} \quad (12)$$

where  $h_{\text{c,f}}$  is the forced convective heat transfer coefficient, and  $h_{\text{c,n}}$  is the  
220 natural convective heat transfer coefficient. This formulation guarantees that natural convection dominates the heat transfer when forced convection is limited and vice-versa. This is important because forced and natural convection have significantly different magnitudes, with forced convection being stronger than natural convection, as highlighted by e.g. Agathokleous & Kalogirou (2016).

225 Forced convection is the result of the wind flow around the building. In  
the multi-physics BIPV model,  $h_{c,f}$  corresponds to the convective heat transfer  
correlations presented by Montazeri & Blocken (2017). These correlations have  
been obtained from computational fluid dynamics (CFD) simulations and are  
valid for isolated buildings. The correlations not only take into account the  
230 building geometry, wind speed and wind direction, but also distinguish between  
windward, leeward and side facades. In contrast to other BIPV models in the  
literature, three additional factors are thus taken into account in the multi-  
physics model: the building geometry, the wind direction, and the building  
surface (with respect to the incoming wind).

Natural convection is the result of the buoyant flow over the BIPV surface  
and is related to density variations caused by temperature variations. In the  
multi-physics BIPV model,  $h_{c,n}$  is modelled using the following correlation for  
natural convection for vertical plates (Churchill & Chu, 1975):

$$h_{c,n} = \left(0.825 + 0.325Ra_h^{1/6}\right)^2 \quad (13)$$

235 where  $Ra_h$  is the Rayleigh number based on the characteristic length  $h$ , which  
in this case is the height of the BIPV control volume.

Inside the cavity, the variation of the specific enthalpy,  $h_{air}$ , of the mass of  
each air volume,  $m_{air}$ , is described as:

$$m_{air} \frac{dh_{air}}{dt} = q_{c,cav1} + q_{c,cav2} + \left(h_{air,ext} - h_{air,in}\right)\dot{m} \quad (14)$$

where  $q_{cav,1}$  and  $q_{cav,2}$  are the convective heat fluxes between the cavity walls  
and the air, and  $\dot{m}$  is the mass flow rate through the cavity, associated with the  
enthalpy flux  $(h_{air,ext} - h_{air,in})$ .

240 As illustrated in Figure 3, the airflow connects the BIPV control volumes, in  
a way that  $(\dot{m} h_{air})_{ext}$  from one control volume is the  $(\dot{m} h_{air})_{int}$  of the other,  
except for the first and last control volumes. The temperature of the air entering  
the BIPV cavity is an input to the multi-physics BIPV model and is discussed  
later in Section 2.4.

The convective heat fluxes inside the cavity are defined as:

$$q_{c,cav1} = \frac{Q_{c,cav1}}{A} = h_{c,1} (T_{s,1} - T_{air}) \quad (15)$$

and

$$q_{c,cav2} = \frac{Q_{c,cav2}}{A} = h_{c,2} (T_{s,2} - T_{air}) \quad (16)$$

245 where  $T_{s,1}$  and  $T_{s,2}$  are the surface temperatures of the cavity walls (Figure 5),  $T_{air}$  is the temperature of the (well mixed) air volume, and  $h_{c,1}$  and  $h_{c,2}$  are the convective heat transfer coefficients inside the cavity. Both  $h_{c,1}$  and  $h_{c,2}$  are modelled using Equation 13.

The radiative heat transfer between the glass surface and building wall surface is defined as:

$$Q_{r,12} = \frac{\sigma (T_{s,1}^4 - T_{s,2}^4) A}{\frac{1 - \varepsilon_1}{\varepsilon_1} + \frac{1}{F_{12}} + \frac{1 - \varepsilon_2}{\varepsilon_2}} \quad (17)$$

250 where  $T_{s,1}$  is the glass surface temperature,  $T_{s,2}$  is the building wall surface temperature,  $\varepsilon_1$  is the glass emissivity,  $\varepsilon_2$  is the building wall emissivity,  $F_{12}$  is the view factor between the glass and building wall surfaces, and  $A$  is the surface area of a BIPV control volume.

Assuming that  $F_{12} = 1$ , Equation 17 results in:

$$Q_{r,12} = \frac{\sigma (T_{s,1}^4 - T_{s,2}^4) A}{\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1} \quad (18)$$

Finally, the heat exchange with the building interior is also composed of radiative and convective heat exchanges, as follows:

$$Q_{int} = Q_{c,int} + Q_{r,int} \quad (19)$$

255 where  $Q_{c,int}$  is the convective heat transfer between the BIPV building wall and the building interior and  $Q_{r,int}$  is the radiative heat transfer between the BIPV building wall and surfaces composing the building interior. These two heat exchanges are based on the modelling already available in the IDEAS library, as described by Jorissen et al. (2018). Moreover, in this paper,  $Q_{int}$  is a measured variable and is used as input to the multi-physics BIPV model, as explained later in Section 2.4.

260 *2.2.2. Airflow modelling*

To calculate the airflow rate, the multi-physics BIPV model relates the airflow rate,  $\dot{m}$ , to the driving pressure differential,  $\Delta P$ , as follows:

$$\dot{m} = \rho_{\text{air}} C \Delta P^n \quad (20)$$

where  $C$  is the flow coefficient, which represents the cavity (friction and turbulent) losses, and  $n$  is the flow exponent, which represents the flow regime (laminar or turbulent). In this work, a dedicated experimental pressurisation setup has been developed to obtain  $C$  and  $n$  for the naturally-ventilated BIPV module investigated in this paper (presented later in Section 2.4.2).  
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In naturally ventilated elements, the driving pressure differential  $\Delta P$  is a result of buoyancy and wind effects:

$$\Delta P = \Delta P_{\text{b}} + \Delta P_{\text{w}} \quad (21)$$

where  $\Delta P_{\text{b}}$  is the buoyancy-driven pressure differential and  $\Delta P_{\text{w}}$  is the wind-driven pressure differential.

Buoyancy is the consequence of density differences between the air inside the cavity and the ambient air. In the multi-physics BIPV model, the resulting buoyancy-induced pressure is computed over all the air volumes in Figure 5, which are considered as well-mixed air volumes, using the following equation:

$$\Delta P_{\text{b}} = g \left[ \rho_{\text{ext}} H - \sum_{i=1}^n \rho_i h_i \right] \quad (22)$$

where  $g$  is the gravity force,  $\rho_{\text{ext}}$  is the exterior air density,  $H$  is the total height of the air column inside the cavity,  $\rho_i$  is the air density of each BIPV control volume, and  $h_i$  is the height of each BIPV control volume (of a total of  $n$  control volumes).  
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The wind-driven pressure is calculated as:

$$\Delta P_{\text{w}} = \Delta C_{\text{p}} V_{\text{w}}^2 \quad (23)$$

where  $\Delta C_{\text{p}}$  accounts for the wind pressure difference between the openings of the BIPV module and  $V_{\text{w}}$  is the wind speed at 10 m height.

The  $C_p$  coefficients used in the multi-physics BIPV model are obtained from  
 275 the CFD simulations performed by Blocken & Carmeliet (2002), as presented  
 by Saelens & Hens (2001). These simulations have been developed specifically  
 for the Vliet test building in which the BIPV module is integrated (as described  
 in Section 2.1). The coefficients correspond to a wind direction perpendicular  
 to the building facade. In this work, this coefficient has been applied to wind  
 280 coming from any direction within the range of  $\pm 45$  deg from the direction  
 perpendicular to the BIPV module. The pressure effects of wind coming from  
 any other direction are not considered. Note that the use of the multi-physics  
 BIPV model for different buildings requires the adaptation of these values.

### 2.2.3. PV electrical modelling

The one-diode model is adopted in the multi-physics BIPV model as it provides a good balance between complexity and accuracy (Chin et al., 2015). In the one-diode model, the I-V characteristic of a PV device is described by the following implicit transcendental equation:

$$I = I_{ph} - I_{sat} \left[ \exp\left(\frac{V + IR_S}{mN_S V_{th}}\right) - 1 \right] - \frac{V + IR_S}{R_{sh}} \quad (24)$$

285 where  $I$  and  $V$  are the diode current and voltage,  $I_{ph}$  is the photo current (or  
 light current),  $I_{sat}$  is the (reverse) saturation current,  $R_S$  is the series resistance,  
 $R_{sh}$  is the shunt resistance,  $m$  is the diode ideality factor,  $N_S$  is the number of  
 (identical) cells connected in series, and  $V_{th} = \frac{kT}{q}$  is the thermal voltage, with  $k$   
 the Stefan-Boltzmann constant ( $1.381 \times 10^{-23}$  J/K), and  $q$  the electronic charge  
 290 ( $-1.602 \times 10^{-19}$  C).

The five unknown parameters in Equation 24, i.e.  $I_{ph}$ ,  $I_{sat}$ ,  $m$ ,  $R_S$  and  $R_{sh}$ ,  
 have to be determined. In the multi-physics BIPV model,  $m$ ,  $R_S$  and  $R_{sh}$  are  
 assumed constant, independent of temperature and irradiance (Villalva et al.,  
 2009; Orioli & Di Gangi, 2013). To obtain  $I_{ph}$ , Equation 24 is considered at  
 short-circuit (SC) conditions. Assuming that  $I_{sat}$  and  $R_S$  can be neglected at  
 SC (Orioli & Di Gangi, 2013), Equation 24 results in:

$$I_{ph} = I_{SC} \quad (25)$$

with the short-circuit current,  $I_{SC}$ , defined as (Villalva et al., 2009):

$$I_{SC} = \frac{G}{G_{STC}} \left[ I_{SC,STC} + \mu_{I_{SC}}(T - T_{STC}) \right] \quad (26)$$

where  $G$  is the solar irradiance,  $G_{STC}$  is the irradiance at STC ( $= 1000 \text{ W/m}^2$ ),  $I_{SC,STC}$  is the short circuit current at STC,  $\mu_{I_{sc}}$  is the temperature coefficient of short-circuit current,  $T$  is the cell temperature, and  $T_{STC}$  is the temperature at STC ( $= 25 \text{ }^\circ\text{C}$ ).

Once  $I_{ph}$  is known, the saturation current,  $I_{sat}$ , can be estimated from Equation 24 at open-circuit (OC) conditions. Assuming  $R_{sh} \approx \infty$  (Villalva et al., 2009), Equation 24 then becomes:

$$I_{sat} = \frac{I_{SC,STC} + \mu_{I_{SC}}(T - T_{STC})}{\exp\left(\frac{V_{OC,STC} + \mu_{V_{OC}}(T - T_{STC})}{nN_S V_{th}}\right) - 1} \quad (27)$$

with the open-circuit voltage,  $V_{OC}$ , defined as (Villalva et al., 2009):

$$V_{OC} = V_{OC,STC} + \mu_{V_{OC}}(T - T_{STC}) \quad (28)$$

295 where  $\mu_{V_{OC}}$  is the temperature coefficient of open-circuit voltage.

To allow the simulation of shading events, the multi-physics BIPV model takes into account spatial variations of solar intensity and temperature within the PV module. For that, the one-diode model is employed at the cell level by adjusting the parameters used in Equations 24-27 to correspond to a single PV  
 300 cell. The electrical parameters are summarised in Table 1.  $I_{SC}$  and  $V_{OC}$  have been determined experimentally, while typical values for c-Si cells are used for  $m$ ,  $R_S$  and  $R_{sh}$ . The BIPV power at STC,  $P_{STC}$ , is also listed in Table 1.

Finally, the multi-physics BIPV model employs a perturb-and-observe (P&O) algorithm to track the maximum power point by varying the load connected to  
 305 the module. The algorithm is available in the Open Source PhotoVoltaics Library for Systemic Investigations, an open-source Modelica library (Brkic et al., 2019). The maximum power point tracker (MPPT) algorithm adjusts the PV electric operating point for every simulation step. Every time the MPPT algorithm acts, a time event is triggered and the entire system of equations is solved

310 (including thermal and airflow coupling). The simulation time step is discussed later in Section 2.4.

Table 1: Electrical parameters.  $I_{SC}$ ,  $V_{OC}$  and  $P_{STC}$  have been determined experimentally with an accuracy of 10 % due to irradiance uniformity and current sweep.

Parameter	Value	
$I_{SC}$ (cell)	8.25*	A
$V_{OC}$ (cell)	0.62*	V
$R_S$ (cell)	0.0067	$\Omega$
$R_{sh}$ (cell)	$\infty$	$\Omega$
$m$ (cell)	1.1	-
$P_{STC}$ (BIPV module)	70.6*	W

### 2.3. Experimental setup

Figure 6 shows a schematic representation of the experimental setup and Table 2 summarises the characteristics and accuracy of the measurement equip-  
 315 ment. The measured dataset correspond to three summer months in 2017. The next subsections describe the experimental data in detail, including weather conditions, power, temperature and heat flux measurements.

#### 2.3.1. Weather conditions

The weather conditions include the ambient temperature, the wind speed  
 320 and direction, and the solar irradiance on the BIPV facade. As illustrated in Figure 6, ambient temperature is recorded with a resolution of 60 s by the weather station located on the roof of the building (about 5 m above the flat part of the roof). The wind speed and direction are monitored by a ultrasonic anemometer located at 10 m height, in the open field in front of the BIPV facade.  
 325 Wind conditions are recoded with a resolution of 300 s. A pyranometer located next to the BIPV module measures the solar irradiance on the facade every 10 s. Table 3 reports the average weather conditions over the measuring period for each month. These data form the weather input data used in the multi-physics BIPV model. As mentioned previously, the simulations employ a time step

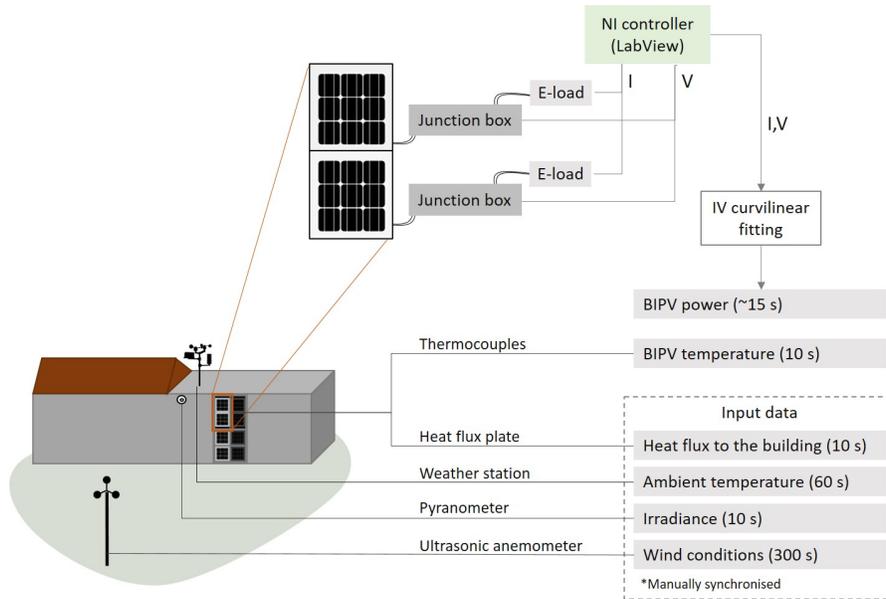


Figure 6: Overview of the experimental setup (not to scale).

Table 2: Characteristics and accuracy of the measurement equipment.

Variable	Equipment/Sensor	Time resolution	Accuracy
Ambient temperature	Hygroclip 2L	60 s	$\pm 0.2$ K
Wind speed	Ultrasonic anemometer Gill Windmaster	300 s	0-20 m/s 1.5 %
			20-35 m/s 1.5-3 %
			35-60 m/s 3 %
Wind direction	Ultrasonic anemometer Gill Windmaster	300 s	$<25$ m/s $\pm 2$ deg
			$>25$ m/s $\pm 4$ deg
Solar irradiance	Thermopile pyranometer type CMP Kipp & Zonen	10 s	$<3$ %
Surface and air temperatures	Thermocouple Type T Class 1	10 s	$\pm 0.5$ K
Heat flux	Hukseflux heat flux plate	10 s	$\pm 3$ %
Power	Electronic loads +	$\sim 15$ s	$\sim 0.6$ % (MPP)
	NI controller		$\sim 4$ % low-irradiance

330 of 10 s, which corresponds to the resolution of the irradiance data; the other variables are interpolated using Akima splines (continuous first derivative).

Table 3: Average daily weather conditions for each month of the experimental data.

	Solar irradiance [W/m <sup>2</sup> ]	Ambient temperature [°C]	Wind speed [m/s]
June	139.0	20.2	1.9
July	116.0	19.8	1.6
August	107.8	19.2	0.9

### 2.3.2. Power measurements

As illustrated in Figure 6, the acquisition of I-V data is made via LabView using electronic loads (E-loads) with variable resistances and a controller from  
 335 National Instruments (NI). The E-loads operate in constant current mode and are controlled using a NI real-time controller running a LabView-based software. First, the short-circuit current of each module is measured. Then, the I-V curves are swept backwards, starting at 10 % above the short circuit current and ending at open circuit. The module voltages at the junction boxes are measured by the  
 340 NI controller in differential mode, using 4-wire probing. The I-V curve sweeping takes about 5-6 s, which leads to a non-uniform interval of about 15 s for the power data. The maximum power is determined by curvilinear fitting of I-V curves (containing 50 points each). For further information on this procedure, the reader is addressed to Spiliotis et al. (2017).

### 345 2.3.3. Temperature and heat flux measurements

The scheme in Figure 7 indicates the location of the thermocouples and the heat flux meter. The BIPV surface temperature is measured at five different positions at the back of each mini-module, as shown in the figure. The insulation surface temperature on the cavity side is measured at the middle section at  
 350 three locations, also equidistant over the height (bottom, middle and top). The air temperature is monitored at both openings as well as inside the cavity at

the middle section at three equidistant points over the BIPV height (bottom, middle and top). Surface and air temperatures are measured using Type T class 1 thermocouples and the heat flux to the building interior is measured  
 355 by a heat flux plate, both with a time resolution of 10 s. Note that surface measurements at the back of the mini-modules refer to the glass surface and not to the PV cell temperature.

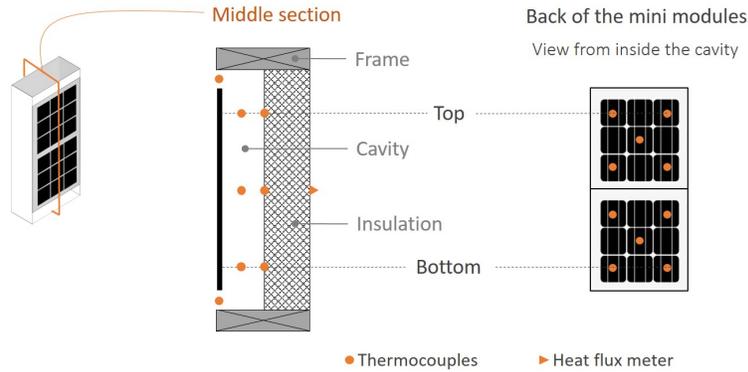


Figure 7: The BIPV module and the experimental instrumentation, including thermocouples and heat flux meter. For the sake of clarity, the thermocouples at the back of the PV modules are omitted in the middle section and are only shown in the view from inside the cavity.

The quality of contact measurements can be evaluated by assessing the so-called installation errors, which are associated with the following aspects (Bentley, 1995; Saelens, 2002; AlWaaly et al., 2015): (1) the thermal contact resistance between the glass and the thermocouple, (2) the relative position of the thermocouple compared to the thermal gradient, and (3) the fin effect of the thermocouple wire. Because thermo-optical properties of the tape differ from the module properties, solar irradiation may also cause measurement errors, as  
 360 discussed by Saelens (2002) and Kalyanova (2008). In order to reduce the installation errors, the thermocouples were tightly attached to the glass surface using  
 365 tape, as recommended by Herteleer (2016), and the wires of the thermocouples were placed parallel to the respective isotherm (at each vertical position), as suggested by Saelens (2002). Because the white encapsulant used in the BIPV

370 module is not completely opaque to the solar radiation, the thermocouples inside  
the cavity are vulnerable to the transmitted radiation. In order to reduce this  
effect, reflective tape was used to attach the thermocouples to the surfaces, and  
cylindrical aluminum shells were used to shield the thermocouples measuring  
the air temperature.

#### 375 2.4. Inputs to the multi-physics BIPV model

##### 2.4.1. Material properties

Table 4 lists the material properties of the BIPV module used in the multi-  
physics BIPV model. Note that the building wall in the BIPV module corre-  
sponds to a single insulation layer.

Table 4: Material properties of the BIPV module.

	Glass	PV cell	Insulation
Thickness [m]	0.003	0.0001	0.15
Thermal conductivity [W/mK]	0.96	710	0.036
Heat capacity [J/kgK]	750	710	840
Density [kg/m <sup>3</sup> ]	2500	2330	110
Short-wave emissivity [-]	0.95	-	-
Long-wave emissivity [-]	0.9	-	0.8
Reflectivity [-]	0.8	-	-

##### 380 2.4.2. Experimental pressure characterisation

As explained in Section 2.2.2, the airflow model requires two parameters,  
namely the flow coefficient C and the flow exponent n. To obtain these param-  
eters for the BIPV module investigated in this paper, an experimental pressuri-  
sation setup was developed, as illustrated in Figure 8a. Table 5 summarises the  
385 characteristics and accuracy of the equipment used for the pressurisation tests.

Figure 8a shows that, at the bottom of the BIPV module, a fan imposes a  
(known) airflow rate through the cavity. At the top, the cavity is open to the  
atmospheric pressure. A pair of pressure taps records the pressure difference

Table 5: Characteristics and accuracy of the measuring equipment

Variable	Equipment	Time resolution	Accuracy
Pressure difference	Pressure gauges (Halstrup Walcher)	10 s	$\pm 0.3$ Pa
Airflow rate	Hot film anemometer (Lindab LT600)	1 s	0.0009 1/s or 5 %, whichever is greater

over the cavity associated with the imposed airflow. The relationship between  
 390 the two measured variables - airflow rate and pressure difference - determines  
 the so-called cavity pressure characteristic (i.e.  $C$  and  $n$ ). The plenum box in  
 Figure 8a helps to create a region of uniform pressure at the bottom opening,  
 attenuating the directionality effect of the fan.

Figure 8b presents the results from six pressurisation tests together with  
 395 the power law to which they fit. A theoretical restriction is imposed on the  
 flow exponent  $n$ , which should be within the interval  $[0.5, 1]$ , from laminar to  
 turbulent flow. The coefficients  $C$  and  $n$  indicated in Figure 8b are used in the  
 multi-physics BIPV model to obtain the airflow as a function of the driving  
 pressure (Equation 20).

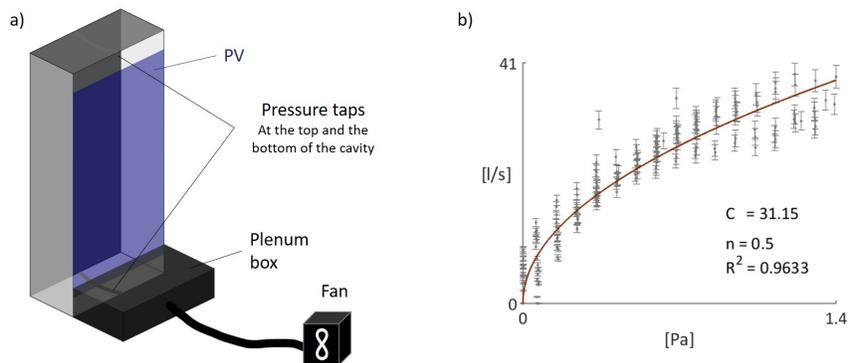


Figure 8: a) Schematic representation of the experimental pressurisation setup. b) Resulting  
 airflow rate as a function of the pressure difference over the cavity height.

400 *2.4.3. Additional assumptions*

As mentioned previously, the heat transfer to the building is not included in the simulations (*building interior* side in Figure 5). Instead, the heat flux measured at the middle of the building wall (shown in Figure 7) is imposed on the wall layer of all BIPV control volumes. Additionally, experimental results  
405 presented by Saelens et al. (2004) have shown that the inlet air temperature is different from the ambient temperature for ventilated facades due to local heating. Such local effects may also be critical in this work, since the BIPV module used for the validation is part of a facade setup comprising several modules, as shown in Figure 2. The buoyancy effects from the adjacent BIPV modules may  
410 affect the temperature at the cavity inlet. Hence, the air temperature measured at the bottom of the cavity (Figure 7) is used as inlet temperature in the model.

*2.4.4. Simulation time step*

Running the simulations at small time steps may be necessary to capture the influence of highly varying conditions, if present in the weather input dataset.  
415 In the multi-physics BIPV model, the time steps was set to 10 s to match the time resolution of the irradiance input, which is the highest resolution of the input dataset (see Table 2). This means that the boundary conditions on the BIPV module change every 10 s. Since thermal dynamics also affect the BIPV module state in the model, the use of a time steps of 5 s has been tested, but  
420 did not influence the results. Note that for the weather variables in the input data that have different time resolutions (i.e. ambient temperature and wind conditions), the data is interpolated using Akima splines such that the first derivative is continuous.

### **3. Results**

425 *3.1. Power and energy yield*

First, the power profiles over time are presented in order to provide visual insight into the results. For that, six consecutive days in June are selected:

two clear-sky days and four cloudy days. The solar irradiance on the BIPV facade and the ambient temperature measured during these six days are shown in Figure 9.

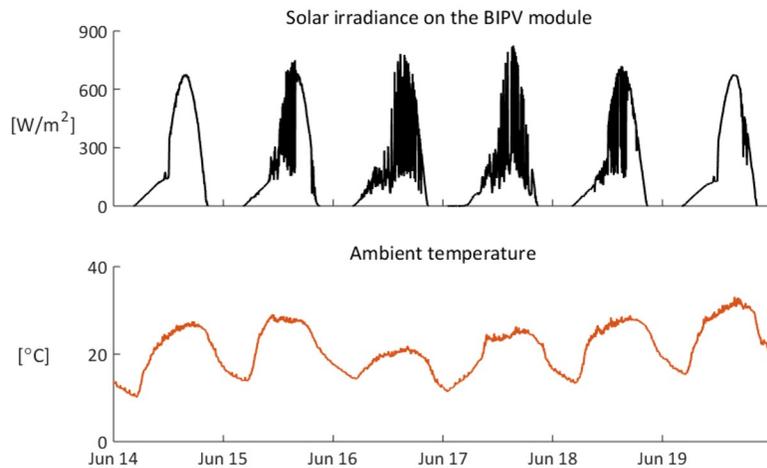


Figure 9: Solar irradiance on the BIPV facade and ambient temperature for the six days in June 2017.

The power profiles are presented in Figure 10. This figure compares predictions of the multi-physics BIPV model to the measurements. The linear power model described in Appendix A is also included in the comparison as a reference. For the two clear sky days (Jun 14 and Jun 19), the multi-physics BIPV model provides relatively good predictions, while the power model underestimates the measured power. For cloudy days, visualising the results is not straightforward, but the errors are quantified later on.

Figure 10b shows two interesting aspects. First, these plots illustrate the effects of vertical integration in a southwest facade: the peak in solar irradiance occurs late in the afternoon. During most of the morning period, the facade only receives diffuse irradiance. When the direct irradiance starts to reach the facade around late morning, a steep raise in the BIPV power is observed. Second, also when the sun starts to directly reach the facade, the pyranometer is shaded by an equipment bar that is attached perpendicularly to the building. The reduction

445 in irradiance is propagated into the model predictions (both multi-physics and power models), while the measurements do not show any reduction, since the BIPV module itself is not shaded.

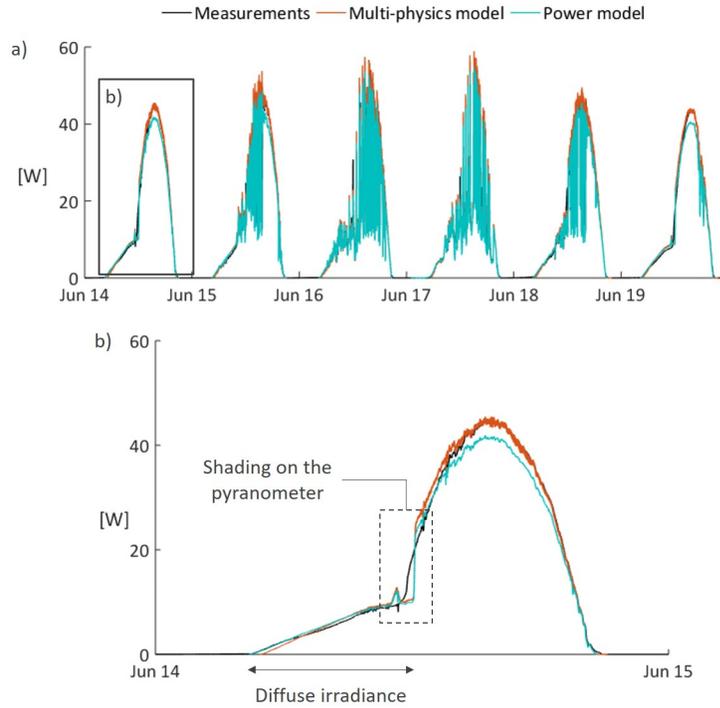


Figure 10: a) BIPV power for six days in June: Comparison between measurements and predictions from the multi-physics BIPV model and the power model. b) Zoom into one day for better visualisation of the results.

Also note that the power model has the (surface-average) back-of-module temperature measurements as input. In the absence of temperature measurements, the BIPV temperature has to be estimated either using a physics-based approach or an (semi-)empirical temperature correlation (as the ones reviewed by Skoplaki & Palyvos (2009)). In contrast, the multi-physics BIPV model couples the cell temperature to the power estimations, solving the two variables simultaneously, as described in Section 2.2.

455 Next, the energy yield is calculated at both daily and monthly basis by

numerically integrating the power results over time. The difference in energy yield between measurements and model predictions corresponds to the total error (TE). TE can be negative or positive, indicating under or overestimations. The mean relative error (MRE) is the ratio between the absolute yield difference  
 460 (i.e. absolute total error) and the measured yield (thus, always positive).

The relative errors in monthly energy yield estimations are presented in Table 6. To calculate this indicator, the power predictions and the measurements are integrated over each month and compared to each other. For the multi-physics BIPV model, the relative error in the estimations of monthly energy yields  
 465 remains well below 2 %. For the power model with  $P_{\text{STC}} = 70.6 \text{ W}_\text{P}$  (Table 1), the monthly error exceeds 5 % in all months. Due to the uncertainty in the determination of the nominal power (see Table 1), results for  $1.05 P_{\text{STC}}$  are included in Table 6, showing how sensitive the power model is to the correct determination of this parameter.

Table 6: Monthly energy yield: Relative error [%].

	Jun	Jul	Aug
Multi-physics BIPV model	0.74	0.41	1.20
Power model ( $P_{\text{STC}}$ )	-5.15	-5.75	-5.15
Power model ( $1.05 P_{\text{STC}}$ )	-0.41	-1.04	-0.41

470 For the multi-physics BIPV model, Figure 11 presents TE and MRE results for the daily energy yield estimations (again, numerically integrated over each day in the dataset). The average daily error is 1.79 % in June, 2.55 % in July, and 2.56 % in August. While the TE is generally of the same order of magnitude ( $\pm 10 \text{ Wh}$ ), some days present MRE values significantly above the average (in  
 475 particular July 1, August 8, and August 10). These days are characterised by a low daily solar irradiation, below  $500 \text{ Wh/m}^2$ . For similar TE values, such low irradiation leads to higher MRE due to the relative nature of this indicator. Nevertheless, apart from these three days, MRE remains mostly below 5 %.

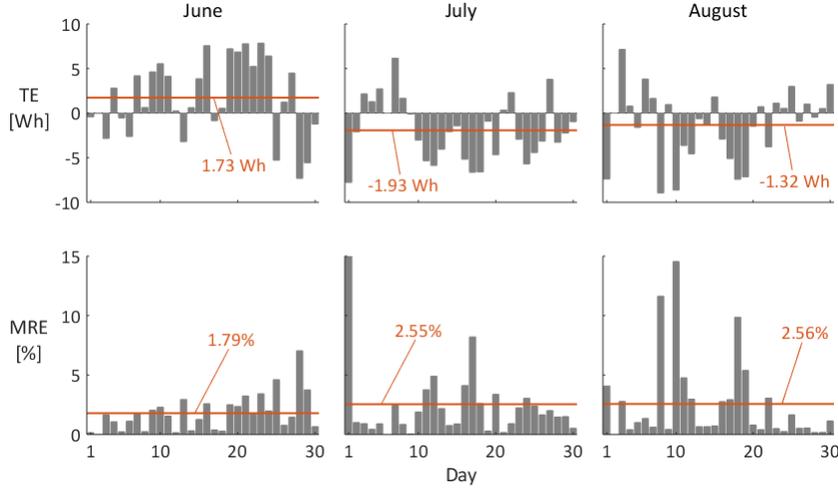


Figure 11: Daily energy yield for the whole dataset: Total error (TE) and mean relative error (MRE) between the measurements and the multi-physics BIPV model (July 6 and August 2 have been omitted due to lack of measured data).

### 3.2. Temperature results

480 Again, for the visual evaluation of the results, Figure 12 presents the back-of-module temperature profiles for the same days in June (Figure 9). Back-of-module temperature refers to  $T_{s,1}$  in Figure 5. Here, the (semi-)empirical temperature models described in Appendix B are included in the comparative analysis as reference. For the sake of clarity, the predictions of the multi-physics  
 485 BIPV model are first compared only to the measurements (Figure 12a). Next, in Figure 12b, the Ross' (Eq. B.1) and Skoplaki et al.'s (Eq. B.2) models are added to the comparison. Last, Figure 12c zooms into two days to provide a more clear visualisation.

Overall, a good agreement is observed between the multi-physics BIPV  
 490 model predictions and the measurements for the back-of-module temperature. The two (semi-)empirical models overestimate the measurements. In addition, Figure 12 demonstrates that the multi-physics model is also able to predict the temperature dynamics, while the Ross' model is only able to do so for clear sky days, such as June 14 presented in Figure 12c. Compared to the Ross'

495 model, the Skoplaki et al.'s model presents fluctuations in temperature due to the incorporation of wind speed.

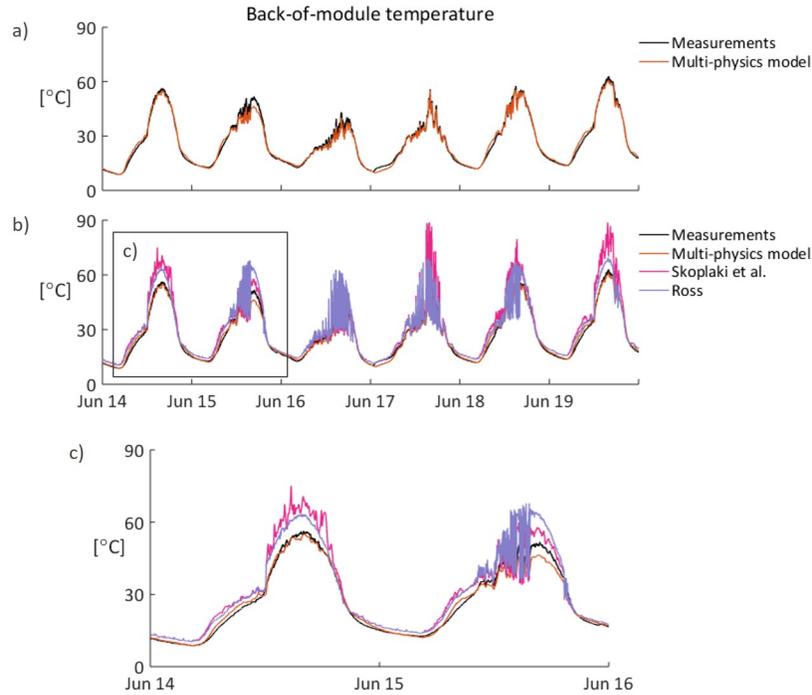


Figure 12: Back-of-module temperature for six days in June: a) Comparison between measurements and the multi-physics BIPV model. b) Same as a) including the predictions from the Ross' model (Ross, 1976; Nordmann & Clavadetscher, 2003) and Skoplaki et al.'s model (Skoplaki et al., 2008). c) Zoom into two days for better visualisation.

Figure 13 presents the difference in back-of-module temperature between the measurements and each one of the three models for the whole month of June. The average and maximum differences are also indicated (average values are presented later in Table 7 for the three months). Among the three models, the multi-physics model (Figure 13a) provides the better agreement, with lowest average and maximum differences (-0.60 and 12.4 °C, respectively). Both Ross' (Figure 13b) and Skoplaki et al.'s (Figure 13c) models generally overestimate the module temperature (averages of 2.81 and 3.12 °C, respectively), with maximum differences up to 40 and 50 °C, respectively. The models by Ross' and

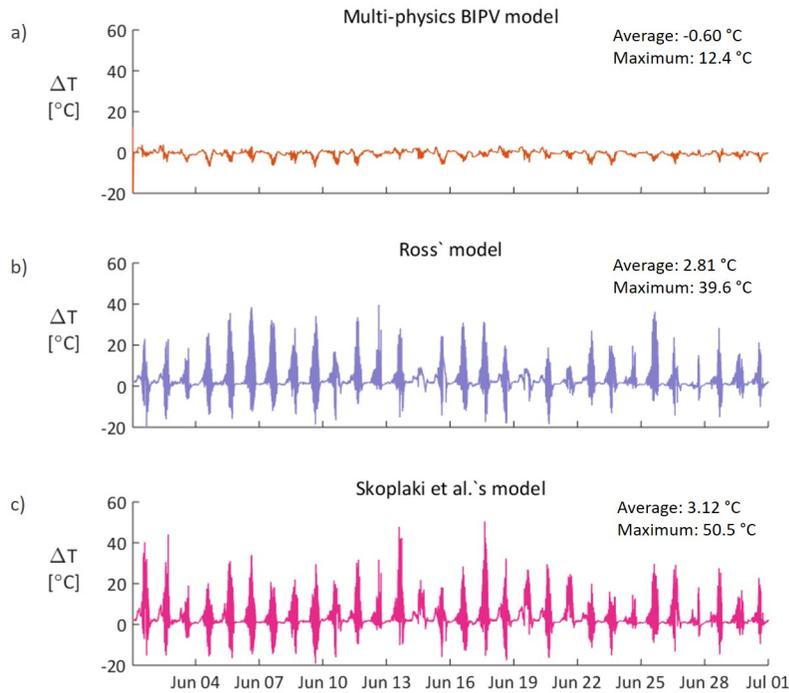


Figure 13: Difference in back-of-module temperature compared to the measurements for six days in June: a) multi-physics model, b) Ross' model, and c) Skoplaki et al.'s model.

Skoplaki et al. are based on data from a BIPV facade with limited ventilation presented by Nordmann & Clavadetscher (2003), which might explain the higher temperatures obtained from these two models.

Next, temperature results are analysed for the whole dataset in terms of absolute differences. Relative differences are not suitable for temperature analysis, as they depend on the temperature scale (Kelvin scale resulting in lower relative differences compared to Celsius scale). Table 7 presents the results for the back-of-module temperature for the three models, for the three months in the measured dataset. The multi-physics BIPV model estimates the back-of-module temperature with a MAE within 1.0-2.5 °C and a RMSE within 1.5-4.5 °C. The Ross' model presents a MAE between 3.0-3.5 °C and a RMSE between 5.0 and 5.5 °C. The Skoplaki et al.'s model presents a MAE between 3.5-4.5 °C and a RMSE between 5.5 and 7.5 °C. Compared to the mean absolute error (MAE),

Table 7: Back-of-module temperature results: Average difference, MAE, and RMSE (all in °C). The differences are plotted in Figure 13 for June.

Model	Average difference			MAE			RMSE		
	Jun	Jul	Aug	Jun	Jul	Aug	Jun	Jul	Aug
Multi-physics	-0.60	-1.32	-1.62	1.11	2.40	2.18	1.91	4.23	3.77
Ross	2.81	2.91	2.31	3.37	3.48	3.09	5.21	5.47	5.04
Skoplaki et al.	3.12	3.31	3.77	3.66	3.82	4.32	5.66	6.10	7.41

Table 8: Air and wall temperatures: Comparison between the multi-physics BIPV model and measurements.

Surface	Average difference			MAE			RMSE		
	Jun	Jul	Aug	Jun	Jul	Aug	Jun	Jul	Aug
Wall ( $T_{s,2}$ )	-0.08	-0.82	-1.39	0.74	1.96	1.89	1.04	3.71	3.32
Air ( $T_{air}$ )	-1.58	-0.75	-1.08	2.07	1.88	1.66	3.43	3.61	2.92

the square formulation of the root mean squared error (RMSE) emphasises  
520 larger differences.

For the multi-physics BIPV model, the cavity air temperature ( $T_{air}$  in Figure 5) and the surface temperature of the building wall ( $T_{s,2}$  in Figure 5) are also evaluated. As presented in Table 8, a generally good agreement between measurements and predictions is obtained for  $T_{air}$  and  $T_{s,2}$ . The (semi-)empirical  
525 models do not provide such information and are, thus, not included in this analysis.

#### 4. Discussion

For the naturally ventilated BIPV module investigated in this work, the multi-physics BIPV model is able to predict the BIPV energy yield and back-  
530 of-module temperature within an acceptable error range for building performance simulations. In addition, the multi-physics BIPV model provides a good agreement for the cavity air and wall temperatures. The air temperature is an important variable if the cavity air is used as heat source for space heating,

while the wall temperature is an important boundary condition on the build-  
535 ing thermal performance. An ongoing effort in this context is the simulation  
of BIPV envelopes combining the multi-physics BIPV model with the building  
models available in the IDEAS library.

The results in this paper are associated with a specific BIPV module and  
a specific experimental data. Using additional experimental data is certainly  
540 important to further verify the reliability of the multi-physics BIPV model.  
Note that, the three summer months presented here are already a relevant pe-  
riod for BIPV operation in view of their annual energy share. Furthermore,  
physics-based models are generally less data intensive. Future work will nev-  
ertheless consider different BIPV modules operating under different conditions.  
545 This effort is supported by the flexible and modular environment provided by  
IDEAS/Modelica library. Such flexibility enables the adaptation of the multi-  
physics BIPV model to a mechanically ventilated or unventilated variant, for  
example. Furthermore, differently from the conventional approach in building  
performance simulation, the PV elementary unit developed in this work has the  
550 dimensions of a PV cell. In this way, BIPV modules of different sizes can also  
be simulated.

To enable the simulation of shading events, the multi-physics BIPV model  
takes into account the spatial variation of solar intensity and temperature at  
the cell level. However, it is important to stress that, while the model is able  
555 to simulate shading effects, the experimental BIPV setup investigated in this  
paper is mostly free of shading. Therefore, shading effects are not present  
in the experimental data. Previous research has shown that a high-resolution  
electrical model such as the one employed in the multi-physics BIPV model is  
capable of simulating PV systems under complex shading conditions (Sprenger  
560 et al., 2016; Gallardo-Saavedra & Karlsson, 2018; Walker et al., 2019). Detailed  
investigations on the impact of shading effects are beyond the scope of this  
paper, but are part of ongoing research efforts.

This paper also investigates simplified models available in the literature for  
the estimation of the BIPV power and (back-of-module) temperature. In terms

565 of energy yield predictions, the linear power model predicts the BIPV energy  
yield with slightly larger errors. However, the power model depends on accurate  
STC data and accurate temperature estimations. In terms of back-of-module  
temperature predictions, (semi-)empirical temperature correlations generally  
overestimate the measurements. Moreover, empirical correlations do not pro-  
570 vide information on the air and wall temperatures. The advantage of simplified  
models is that they do not require detailed data and do not demand significant  
computational resources. In contrast, the multi-physics BIPV model requires  
detailed information about the BIPV module and its environment, such as geom-  
etry, construction aspects, wind pressure coefficients, etc. The high-resolution  
575 detailed modelling also poses challenges concerning the total simulation time.

The observations above have to be put into perspective to the goal of the  
analysis (research vs. engineering goal), the design stage of the project (early vs.  
late stage), and the scale of the problem (module vs. building vs. district level).  
Conducting representative simulations at building/district level involves a more  
580 complex system, where minor variations in the BIPV daily energy yield may not  
be relevant for the whole system performance and the total simulation time may  
be a more important constrain. In such cases, simplified models may be more  
appropriate, possibly in combination with a simplified method that accounts  
for shading losses, e.g. Zomer & R  ther (2017a), Zomer & R  ther (2017b). In  
585 contrast, assessing the integration of the BIPV power into the electrical grid  
may require a higher degree of accuracy and time and space resolution. For  
these applications, broadening the scope of the electrical model may be more  
relevant, e.g. Sprenger et al. (2016), Walker et al. (2019).

## 5. Conclusion

590 The main contribution of this work is the development of a multi-physics  
BIPV model for facade applications within a building performance simula-  
tion environment. The model combines a high-resolution electrical model with  
physics-based thermal and airflow models. This work was motivated by a general

trend observed in BIPV models that focus either on a high-resolution electrical  
595 model or on a detailed thermal model. The combination of both approaches is  
not common in BIPV modelling, particularly in the context of building perfor-  
mance simulations.

In summary, the characteristics of the multi-physics BIPV model are the  
following: (1) thermal coupling between the BIPV module and the building in-  
600 door environment; (2) high resolution electrical model (temperature-dependent  
one-diode at cell level); (3) the possibility of simulating shading effects intra  
and inter-modules; (4) the modelling of external heat transfer considering both  
buoyancy and wind effects, the latter taking into account the building geome-  
try, wind speed and direction, and the building surface with respect to incoming  
605 wind flow; (5) a detailed modelling of the airflow through the cavity based on  
experimental pressurisation data, including both buoyancy and wind effects.

The multi-physics BIPV model predictions are compared to three months of  
experimental data from a realistic BIPV facade implementation. A good agree-  
ment is observed for daily energy yield as well as for temperature predictions.  
610 On average, the BIPV daily energy yield is estimated with an error below 3 %  
and the monthly energy yield with an error below 2 %. The back-of-module PV  
temperature is predicted with a MAE lower than 2 °C and RMSE lower than  
5 °C. Similar results are verified for the air temperature inside the cavity and  
the building wall temperature (inside the cavity).

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## 625 **Appendix A. Linear power model**

The power model is calculated as follows:

$$P = \eta_{\text{ref}}[1 - \beta(T - T_{\text{ref}})]AG, \quad (\text{A.1})$$

with

$$\eta_{\text{ref}} = \frac{P_{\text{STC}}}{G_{\text{ref}}A}, \quad (\text{A.2})$$

where  $\eta_{\text{ref}}$  is the module efficiency at STC,  $T$  is the temperature of the module,  $T_{\text{ref}}$  is the reference temperature ( $= 25 \text{ }^\circ\text{C}$ ),  $\beta$  is the temperature coefficient of power ( $= 0.42 \text{ } \%/ \text{K}$ ),  $A$  is the PV module area,  $G$  is the actual solar irradiance on the BIPV modules (plane-of-array irradiance), and  $G_{\text{ref}}$  is the reference  
630 irradiance ( $= 1000 \text{ W}/\text{m}^2$ ).

In this model,  $T$  is an input, which in this paper corresponds to the (surface-average) back-of-module temperature measurements. No correction is applied to obtain the cell temperature from back-of-module measurements.

## **Appendix B. Empirical temperature correlations**

635 The following two (semi-)empirical models are used to obtain the BIPV temperature:

(1) Ross' model, which defines the module temperature as (Ross, 1976):

$$T_{\text{BIPV}} = T_{\text{amb}} + kG, \quad (\text{B.1})$$

where  $T_{\text{amb}}$  is the ambient temperature,  $G$  is the plane-of-array irradiance, and  $k = 0.0538$  (Nordmann & Clavadetscher, 2003; Skoplaki & Palyvos, 2009).

(2) Skoplaki et al.'s model, which includes the wind speed (WS) in the equation, as follows (Skoplaki et al., 2008):

$$T_{\text{BIPV}} = T_{\text{amb}} + \omega G \frac{0.32}{8.91 + 2WS}, \quad (\text{B.2})$$

where  $T_{\text{amb}}$  is the ambient temperature,  $G$  is the plane-of-array irradiance, and  
640  $\omega = 2.4$ .

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