

# A three-constituent damage model for arterial clamping in computer-assisted surgery

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**Abstract** Robotic surgery is an attractive, minimally invasive and high precision alternative to conventional surgical procedures. However, it lacks the natural touch and force feedback that allows the surgeon to control safe tissue manipulation. This is an important problem in standard surgical procedures such as clamping, which might induce severe tissue damage. In complex, heterogeneous, large deformation scenarios, the limits of the safe loading regime beyond which tissue damage occurs are unknown. Here, we show that a continuum damage model for arteries, implemented in a finite element setting, can help to predict arterial stiffness degradation and to identify critical loading regimes. The model consists of the main mechanical constituents of arterial tissue: extracellular matrix, collagen fibres and smooth muscle cells. All constituents are allowed to degrade independently in response to mechanical overload. To demonstrate the modularity and portability of the proposed model, we implement it in a commercial finite element programme, which allows to keep track of damage progression via internal variables. The loading history during arterial clamping is simulated through four successive steps, incorporating residual strains. The results of our first prototype simulation demonstrate significant regional variations in smooth muscle cell damage. In three additional steps, this damage is evaluated by simulating an isometric contraction experiment. The entire finite element simulation is finally compared with actual in vivo experiments. In the short term, our computational simulation tool can be useful to optimise surgical tools with the goal to minimise tissue damage. In the long term, it can potentially be used to inform computer-assisted surgery and identify safe

loading regimes, in real time, to minimise tissue damage during robotic tissue manipulation.

**Keywords** Artery · Damage · Smooth muscle cells · Active contraction · Residual stress · Finite elements

## 1 Introduction

For the past two decades, computer-assisted surgery has revolutionised surgical treatment in various different fields. Initially developed to surgically manipulate the brain, see [Kwoh et al. \(1988\)](#), robotic surgery has now gained widespread use. The da Vinci surgical system, for example, offers a computer-enhanced surgical option for complex cardiovascular procedures, see [Mohr et al. \(2001\)](#). Robotic surgery enables minimally invasive and high-precision treatment. However, in contrast to conventional surgeries, robotic surgery inherently lacks the natural touch and force feedback. This is an important problem during common surgical procedures such as grasping, cutting, stapling, clipping and clamping, which may induce severe tissue damage when not controlled appropriately.

To illustrate these effects, within this manuscript, we focus in particular on arterial clamping, which always entails a certain degree of undesired iatrogenic tissue damage ([Barone et al. 1989](#)). Research has been directed towards decreasing this unnecessary intra-operative trauma, for example through the design of less traumatic surgical instruments ([Gupta et al. 1997](#)). Obviously, the effectiveness of these new designs and techniques depends on how well damage mechanisms are understood and how accurately thresholds for safe tissue loading can be defined.

An important aspect is the accurate modelling of the loading and the resulting damage process. This article describes

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62 a new material model for cardiovascular tissue, which is an  
 63 extension of the Holzapfel-material model for arterial tissue  
 64 (Holzapfel et al. 2000), incorporating smooth muscle cell  
 65 activation according to Murtada et al. (2010) and damage  
 66 according to Balzani et al. (2006). The model is suitable  
 67 to simulate the damage process during the clamping of an  
 68 artery. It displays the decrease of active force generation in  
 69 smooth muscle cells due to the sustained damage. Embedded  
 70 in a finite element environment, this new model provides a  
 71 useful tool to define safe loading regimes for arterial tissue,  
 72 which could be used to inform computer-enhanced surgical  
 73 systems to minimise tissue damage in robotic surgery and, in  
 74 general, to optimise clamp design towards minimal trauma.

## 75 Physiology of the healthy artery

76 An artery consists of three distinct layers. In healthy  
 77 arterial tissue, the inner layer, or intima, consists of an endo-  
 78 thelial layer. The middle layer, the media, is the most impor-  
 79 tant load-bearing layer of the artery within the physiological  
 80 loading domain. It consists of collagen, elastin and smooth  
 81 muscle cells separated by fenestrated elastic laminae. The  
 82 outer layer, the adventitia, is surrounded by loose connective  
 83 tissue. It consists mainly of thick bundles of collagen fibres  
 84 arranged in a helical structure (Rhodin 1979). For a more  
 85 detailed description of arterial wall morphology, the reader  
 86 is referred to, for example, Rhodin (1979) and Holzapfel and  
 87 Ogden (2010b).

88 Arterial blood pressure is regulated acutely by altering the  
 89 luminal diameter, which is controlled by balancing vasocon-  
 90 stricting and vasodilating influences on the smooth muscle  
 91 cells in a mechanochemical process. Smooth muscle cells  
 92 contain actin and myosin filaments that slide relative to each  
 93 other, causing contraction and relaxation. This relative slid-  
 94 ing is accomplished by configurational changes of the cross-  
 95 bridges, or myosin heads, that connect the myosin to the  
 96 actin filament. These configurational changes are caused by  
 97 phosphorylation and dephosphorylation of the myosin heads,  
 98 as a function of the intracellular calcium concentration. For  
 99 a detailed description of the mechanochemical process of  
 100 smooth muscle cell contraction, the reader is referred to, for  
 101 example, Stålhand et al. (2008) or Murtada et al. (2010).

## 102 Material modelling

103 Constitutive models characterise the mechanical behaviour  
 104 of materials through a functional relation between stresses  
 105 and strains. A great number of models for cardiovascular tis-  
 106 sue exist, aimed at capturing its specific features (Vito and  
 107 Dixon 2003; Göktepe et al. 2011). For an overview of consti-  
 108 tutive models for cardiovascular tissue, or for biological soft  
 109 tissue in general, the reader is referred to, for example, Gasser  
 110 et al. (2006); Famaey and Vander Sloten (2008). Holzapfel

111 et al. (2000) have introduced one of the most commonly used  
 112 hyperelastic, anisotropic material models for arteries, which  
 113 accounts for two collagen fibre families along two symmet-  
 114 rically arranged directions and allows for a certain amount  
 115 of dispersion. This model nicely captures the typical nonlin-  
 116 ear behaviour as wavy collagen fibres are gradually recruited  
 117 when the tissue is stretched. In this baseline model, however,  
 118 the material behaves completely passive, that is, the model  
 119 does not account for the contractile nature of the smooth  
 120 muscle cells present in the arterial wall.

121 The first mechanical representation of a muscle was pro-  
 122 posed by Hill (1938), which was extended to the three-ele-  
 123 ment Hill model by Fung (1970). This model consists of a  
 124 contractile element in series with a spring element, represent-  
 125 ing the contractile unit. Another spring in parallel represents  
 126 the surrounding material. For smooth muscle, Gestrelus and  
 127 Borgström (1986) proposed a variation of the three-element  
 128 Hill model. Yang et al. (2003) were the first to couple the  
 129 mechanical representation to an electrochemical model by  
 130 Hai and Murphy (1988), incorporating the calcium-driven  
 131 configurational changes of the cross-bridges. This approach  
 132 was also followed and improved for situations with large  
 133 deformations, by Stålhand et al. (2008), Murtada et al. (2010),  
 134 Kroon (2010) and Schmitz and Böhl (2011). However, so far,  
 135 the active contribution of smooth muscle has not yet been  
 136 combined with the collagen fibre contribution, nor have the  
 137 models been implemented in a finite element framework.  
 138 The model proposed by Zulliger et al. (2004) does combine  
 139 the active contribution with a stochastic collagen fibre con-  
 140 tribution in a pseudoelastic-type strain energy function. In  
 141 Göktepe and Kuhl (2010) and Rausch et al. (2011), finite  
 142 element formulations were proposed in which mechanical  
 143 contraction was controlled via electrical and chemical fields,  
 144 respectively. Unfortunately, these models are phenomeno-  
 145 logical and thus less straightforward to populate with realis-  
 146 tic experiment-based material parameters. In this article, the  
 147 active contribution by Murtada et al. (2010) will be combined  
 148 with the collagen fibre contribution by Holzapfel et al. (2000)  
 149 and implemented in a finite element framework to account  
 150 for tissue heterogeneity. Moreover, the material parameters  
 151 related to the active constituent will be calibrated for rat  
 152 abdominal arteries by means of in vivo experiments.

153 Most existing material models are designed to describe the  
 154 material in its physiological state. These models, however,  
 155 fail to capture damage mechanisms that may occur when the  
 156 tissue is loaded in the sub- or supra-physiological domain,  
 157 for example, during surgical manipulation. Motivated by  
 158 the typical stress softening or Mullins effect in rubber-like  
 159 materials, Simo and Ju (1987) introduced a discontinuous  
 160 damage model that allows progressive degradation of an  
 161 isotropic material to be captured. Balzani et al. (2006) have  
 162 adapted this approach to describe damage to arterial tissue  
 163 based on the Holzapfel-material model. Other approaches

164 exist to model damage in rubber-like materials, in a con- 215  
 165 tinuous manner (Miehe 1995), or pseudoelastically (Ogden 216  
 166 and Roxburgh 1999). Dargazany and Itskov (2009) proposed 217  
 167 a network evolution model to model anisotropic damage in 218  
 168 rubber which was later applied for biological tissues by Ehret  
 169 and Itskov (2009). Hokanson and Yazdani (1997) incorpo-  
 170 rated anisotropic damage in arteries by weighting an Ogden-  
 171 type strain energy function with a fourth order damage tensor.  
 172 Another suggestion for anisotropic damage to arterial tissue  
 173 controlled by material constants was made in Volokh (2008,  
 174 2011). Also for arterial tissue, damage to the collagen fibres  
 175 has been described in a stochastic, worm-like chain model  
 176 by Rodríguez et al. (2006). From the same group, Calvo et al.  
 177 (2007) presented a continuum damage model with discontinu-  
 178 ous softening in matrix and collagen fibres. Viscoelasticity  
 179 was introduced in these damage models by Pena et al. (2010).  
 180 These damage models, however, neither include the active  
 181 smooth muscle contribution nor the damage to the smooth  
 182 muscle cells. In this article, damage will be incorporated in  
 183 a manner similar to Balzani et al. (2006), this time including  
 184 the contributions of healthy and potentially damaged smooth  
 185 muscle cells.

## 186 Experimental characterisation

187 Every constitutive model introduces a set of material param- 219  
 188 eters that needs to be calibrated for the particular type of tissue. 220  
 189 Specific experimental setups, such as uniaxial and biaxial 221  
 190 tensile tests or extension-inflation tests can be performed to 222  
 191 calibrate the material parameters for standard passive hyper- 223  
 192 elastic models, as described, for example, in Sacks and Sun 224  
 193 (2003), Holzapfel and Ogden (2010a). 225

194 To quantify the active response of the smooth muscle, iso- 226  
 195 metric and/or isotonic contraction experiments can be per- 227  
 196 formed ex vivo, as described in Barone et al. (1989), Gleason 228  
 197 et al. (2004), Murtada et al. (2010) and Böhl et al. (2012). 229  
 198 Recently, Itoh et al. (2009) and Tsamis et al. (2011) have 230  
 199 reported in vivo experiments to identify active muscle force 231  
 200 in cardiovascular tissue in situ.

201 Damage is frequently assessed through the evaluation of 232  
 202 histological images of the tissue, for example in Hsi et al. 233  
 203 (2002), Manchio et al. (2005) and De et al. (2007). For exam- 234  
 204 ple, live-dead stains can help to identify cell viability, and H 235  
 205 and E (haematoxylin and eosin) and collagen stainings can 236  
 206 visualise ruptures in the collagen fibres. Unfortunately, most 237  
 207 studies of tissue damage are qualitative in nature, both in the 238  
 208 application of the tissue load to induce the damage and in 239  
 209 the subsequent damage assessment. To calibrate the damage 240  
 210 material parameters, however, quantitative experiments are 241  
 211 essential. De et al. (2007) were the first to characterise dam- 242  
 212 age quantitatively for porcine liver. For cardiovascular tis- 243  
 213 sue, previous work (Famaey et al. 2010) reports on a study in 244  
 214 which the damage to the smooth muscle cells of rat abdominal 245  
 246  
 247

arteries is quantitatively assessed in an isometric contraction 215  
 test after in vivo clamping to well-defined loading levels. In 216  
 this article, this quantitative damage information will be used 217  
 to calibrate the parameters of the new material model. 218

## 219 Outline

220 Section 2 introduces our new material model, accounting 221  
 for the three major tissue constituents: extracellular matrix, 222  
 collagen and smooth muscle cells. In particular, we allow 223  
 each constituent to degrade independently. The features of 224  
 the model are first illustrated in a simple homogeneous uni- 225  
 axial cyclic extension and compression test in Sect. 3. Section 226  
 4 then demonstrates how the model can be applied to predict 227  
 smooth muscle cell damage in rat abdominal arteries through 228  
 clamping and how the damage parameters can be identified 229  
 using actual experiments. Section 5 discusses the presented 230  
 model and suggests further directions for future work.

## 231 2 Governing equations for arteries

232 Through an additive decomposition of the strain energy, the 233  
 following constitutive model for active healthy and degraded 234  
 arterial tissue characterises the properties of (i) an isotropic 235  
 matrix material constituent, (ii) an anisotropic constituent 236  
 attributed to the dispersed collagen fibres and (iii) an aniso- 237  
 tropic smooth muscle cell constituent. The first two consti- 238  
 tuents are motivated by the Holzapfel-material model as pro- 239  
 posed in Holzapfel et al. (2000), whereas the third compo- 240  
 nent is motivated by the mechanical smooth muscle-activa- 241  
 tion model described by Murtada et al. (2010). The damage 242  
 accumulating in the different constituents during mechanical 243  
 loading is characterised through a strain energy-driven dam- 244  
 age function for each individual constituent, motivated by the 245  
 formulation by Balzani et al. (2006). In the remainder of the 246  
 article, the model will be referred to as the three-constituent 247  
 damage model.

### 248 2.1 Kinematic prerequisites

249 Since soft biological tissues can undergo large physiological 250  
 deformations, the key kinematic quantity to characterise the 251  
 deformation process is the deformation gradient  $\mathbf{F}$ , that is, 252  
 the gradient of the deformation map  $\varphi$  with respect to the 253  
 undeformed position  $\mathbf{X}$ :

$$254 \mathbf{F} = \nabla_{\mathbf{X}} \varphi \quad \text{and} \quad J = \det(\mathbf{F}). \quad (1) \quad 255$$

256 Here,  $J$  denotes its Jacobian  $J$ , which is close to one,  $J \approx 1$ , 257  
 for nearly incompressible materials. In that case, it proves 258  
 convenient to decompose the deformation gradient into a 259  
 deviatoric part,  $\bar{\mathbf{F}}$ , and a volumetric part,  $J^{1/3} \mathbf{I}$ , 260

$$\mathbf{F} = J^{1/3} \bar{\mathbf{F}}. \tag{2}$$

Typically, the deformation of incompressible materials is characterised in terms of the invariants of the deviatoric part  $\bar{\mathbf{C}}$  of the right Cauchy-Green tensor  $\mathbf{C}$ , with

$$\mathbf{C} = \mathbf{F}^T \mathbf{F} \quad \text{and} \quad \bar{\mathbf{C}} = \bar{\mathbf{F}}^T \bar{\mathbf{F}}. \tag{3}$$

The basic deviatoric invariants  $\bar{I}_i$  take the following explicit representation:

$$\begin{aligned} \bar{I}_1 &= \text{tr}(\bar{\mathbf{C}}), \\ \bar{I}_2 &= \frac{1}{2} [\text{tr}^2(\bar{\mathbf{C}}) - \text{tr}(\bar{\mathbf{C}}^2)], \\ \bar{I}_3 &= \det(\bar{\mathbf{C}}). \end{aligned} \tag{4}$$

While the basic invariants characterise the isotropic material behaviour, the anisotropic invariants  $\bar{I}_4^{\text{fib}}$ ,  $\bar{I}_6^{\text{fib}}$ , and  $\bar{I}_4^{\text{smc}}$  characterise the stretches along the fibre and smooth muscle cell directions, see Gasser et al. (2006):

$$\begin{aligned} \bar{I}_4^{\text{fib}} &= \lambda_\theta^2 \cos^2 \alpha^{\text{fib}1} + \lambda_z^2 \sin^2 \alpha^{\text{fib}1}, \\ \bar{I}_6^{\text{fib}} &= \lambda_\theta^2 \cos^2 \alpha^{\text{fib}2} + \lambda_z^2 \sin^2 \alpha^{\text{fib}2}, \\ \bar{I}_4^{\text{smc}} &= \lambda_\theta^2 \cos^2 \alpha^{\text{smc}} + \lambda_z^2 \sin^2 \alpha^{\text{smc}} \end{aligned} \tag{5}$$

Here,  $\lambda_\theta$  and  $\lambda_z$  are the stretches in the circumferential and axial directions, respectively. Moreover,  $\alpha^{\text{fib}1}$ ,  $\alpha^{\text{fib}2}$  and  $\alpha^{\text{smc}}$  denote the angles between the circumference and the mean directions of the fibre and smooth muscle families. In the case of arteries, two fibre families are oriented symmetrically with respect to the cylinder axis, so that  $\alpha^{\text{fib}1} = -\alpha^{\text{fib}2}$  and, consequently,  $\bar{I}_4^{\text{fib}} = \bar{I}_6^{\text{fib}}$ . Finally, the pseudo-invariants  $I_4^{\text{fib}\star}$  and  $I_6^{\text{fib}\star}$  are introduced to account for dispersion,

$$\begin{aligned} I_4^{\text{fib}\star} &= \kappa \bar{I}_1 + [1 - 3\kappa] \bar{I}_4^{\text{fib}}, \\ I_6^{\text{fib}\star} &= \kappa \bar{I}_1 + [1 - 3\kappa] \bar{I}_6^{\text{fib}}, \end{aligned} \tag{6}$$

where the fibre dispersion  $\kappa$  characterises the degree of anisotropy varying from  $\kappa = 0$  in the anisotropic non-dispersed state to  $\kappa = \frac{1}{3}$  in the isotropic state.

## 2.2 Constitutive equations

Since the tissue is assumed to be nearly incompressible, it is common to additively decompose the strain energy function  $\Psi$ ,

$$\Psi = \Psi^{\text{vol}} + \Psi^{\text{dev}} = \Psi^{\text{vol}} + \Psi^{\text{mat}} + \Psi^{\text{fib}1} + \Psi^{\text{fib}2} + \Psi^{\text{smc}}, \tag{7}$$

into a volumetric  $\Psi^{\text{vol}}$  and a deviatoric  $\Psi^{\text{dev}}$  part. The latter consists of an isotropic contribution of the matrix material  $\Psi^{\text{mat}}$ , an anisotropic contribution of two families of collagen fibres  $\Psi^{\text{fib}1}$  and  $\Psi^{\text{fib}2}$ , and a contribution of the smooth muscle cells  $\Psi^{\text{smc}}$ . The individual contributions will be specified in detail in the following section. All deviatoric components are allowed to undergo degradation in the case of physiological overload. Simo and Ju (1987) in general and Balzani et al. (2006) for arteries have described the approach

of weighting the strain energy with a scalar valued damage variable  $[1 - d]$ . This model builds upon the classical damage concept, and introduces an independent damage variable for each individual constituent.

### Volumetric bulk material

The volumetric free energy  $\Psi^{\text{vol}}$  can, for example, be expressed as follows (Arruda and Boyce 1993):

$$\Psi^{\text{vol}} = \Lambda \left[ \frac{1}{2} [J^2 - 1] - \ln(J) \right]. \tag{8}$$

The penalty parameter  $\Lambda$  corresponds to  $\kappa/2$ , with  $\kappa$  the bulk modulus (in MPa), and should be set high enough to ensure near-incompressibility.

Since this term is handled separately in an incompressible finite element formulation, we will now focus on the four contributions to the deviatoric energy  $\Psi^{\text{dev}}$ , which are the primary descriptors of the material behaviour.

### Extracellular matrix

The extracellular matrix is characterised through an isotropic free energy  $\Psi^{\text{mat}}$ , which is allowed to degrade according to the classical damage concept:

$$\Psi^{\text{mat}} = [1 - d^{\text{mat}}] \hat{\Psi}^{\text{mat}}. \tag{9}$$

Here,  $\hat{\Psi}^{\text{mat}}$  denotes the elastic energy of the extracellular matrix:

$$\hat{\Psi}^{\text{mat}} = \frac{1}{2} c [\bar{I}_1 - 3], \tag{10}$$

where  $c > 0$  characterises the matrix stiffness (in kPa). The evolution of the damage variable of the extracellular matrix  $d^{\text{mat}}$  is driven by the undamaged elastic extracellular matrix energy, as proposed by Balzani et al. (2006):

$$d^{\text{mat}} = \gamma^{\text{mat}} [1 - \exp(-\beta^{\text{mat}}/m^{\text{mat}})]. \tag{11}$$

The weighting factor  $\gamma^{\text{mat}}$  (in kPa) can be used to tune the sensitivity to damage,  $\gamma^{\text{mat}} \in ]0, 1]$ , or to turn the damage off altogether,  $\gamma^{\text{mat}} = 0$ .  $m^{\text{mat}}$  is a dimensionless parameter of the damage model. The variable  $\beta^{\text{mat}}$  is an internal variable keeping track of the maximum elastic strain energy experienced so far, within the time interval  $0 \leq t \leq \tau$  (Balzani et al. 2006):

$$\beta^{\text{mat}} = \max_{0 \leq t \leq \tau} (\hat{\Psi}^{\text{mat}}(t) - \Psi_0^{\text{mat}}). \tag{12}$$

Since it can be assumed that no damage occurs in the physiological range, the damage threshold  $\Psi_0^{\text{mat}}$  is initialised with the strain energy in the extracellular matrix at systolic pressure. For heterogeneous problems,  $\Psi_0^{\text{mat}}$  may therefore differ for each material point, and is thus not strictly a material property.

341 *Collagen fibres*

342 Collagen fibres will only contribute when under tension. Sim-  
343 ilar to the free energy of the matrix, the free energy of the  
344 collagen fibres accounts for both an elastic and a degrading  
345 response,

$$346 \Psi^{\text{fib}_i} = [1 - d^{\text{fib}_i}] \widehat{\Psi}^{\text{fib}_i} \quad i = 1, 2, \quad (13)$$

347 where the energy contributions of the two families of colla-  
348 gen fibres are formulated according to Gasser et al. (2006):

$$349 \widehat{\Psi}^{\text{fib}_i} = \frac{k_1}{2k_2} [\exp(k_2 [I_i^{\text{fib}_i} - 1]^2) - 1]. \quad (14)$$

350 Here,  $k_1 > 0$  characterises the fibre stiffness (in kPa) and  
351  $k_2 > 0$  is a dimensionless parameter. Damage of the two  
352 fibre families  $d^{\text{fib}_i}$  can again be described in terms of the  
353 elastic fibre energies  $\widehat{\Psi}^{\text{fib}_i}$  (Balzani et al. 2006):

$$354 d^{\text{fib}_i} = \gamma^{\text{fib}} [1 - \exp(-\beta^{\text{fib}_i} / m^{\text{fib}})], \quad (15)$$

355 where  $\gamma^{\text{fib}}$  and  $m^{\text{fib}}$  are the two fibre damage parameters and  
356  $\beta^{\text{fib}_i}$  are the internal variables of each fibre family keeping  
357 track of the maximum value of the elastic fibre energies expe-  
358 rienced so far (Balzani et al. 2006):

$$359 \beta^{\text{fib}_i} = \max_{0 \leq t \leq \tau} (\widehat{\Psi}^{\text{fib}_i}(t) - \Psi_0^{\text{fib}}). \quad (16)$$

360 Again, the damage threshold  $\Psi_0^{\text{fib}}$  is initialised with the strain  
361 energy of the fibres at systolic pressure and may therefore dif-  
362 fer for each material point. Since the internal variables  $\beta^{\text{fib}_i}$   
363 are driven by the elastic strain energies  $\widehat{\Psi}^{\text{fib}_i}$ , material degra-  
364 dation will only take place when the fibres are under tension,  
365 as the strain energy is zero when in compression.

366 *Smooth muscle cells*

367 The smooth muscle cells form an integral part of the matrix  
368 constituent, even in their passive state. Therefore, their degra-  
369 dation is assumed to depend on both the passive damage  
370  $d_{\text{pas}}^{\text{smc}}$  in the surrounding matrix and the active damage  $d_{\text{act}}^{\text{smc}}$   
371 in the smooth muscle cells themselves:

$$372 \Psi^{\text{smc}} = [1 - d_{\text{pas}}^{\text{smc}}][1 - d_{\text{act}}^{\text{smc}}] \widehat{\Psi}^{\text{smc}}. \quad (17)$$

373 In the undamaged state, the energy of the smooth muscle cells  
374  $\widehat{\Psi}^{\text{smc}}$  can be expressed as follows (Murtada et al. 2010):

$$375 \widehat{\Psi}^{\text{smc}} = \frac{1}{2} \mu^{\text{smc}} [n_{\text{III}} + n_{\text{IV}}] [\sqrt{I_4^{\text{smc}} + u_{\text{rs}}} - 1]^2, \quad (18)$$

376 where  $\mu^{\text{smc}}$  characterises the stiffness of the actin-myosin  
377 filament apparatus (in kPa). The kinetics of the actin-my-  
378 osin power stroke are modelled through a four-state model  
379 described by Hai and Murphy (1988) and adopted by Mur-  
380 tada et al. (2010), Kroon (2010) and Stålhand et al. (2011).  
381 This model describes the transitions between the four states

382  $n_{\text{I}}$ ,  $n_{\text{II}}$ ,  $n_{\text{III}}$  and  $n_{\text{IV}}$  of the myosin heads as a function of the  
383 calcium concentration as follows:

$$\begin{bmatrix} \dot{n}_{\text{I}} \\ \dot{n}_{\text{II}} \\ \dot{n}_{\text{III}} \\ \dot{n}_{\text{IV}} \end{bmatrix} = \begin{bmatrix} -\kappa_1 & \kappa_2 & 0 & \kappa_7 \\ \kappa_1 & -(\kappa_2 + \kappa_3) & \kappa_4 & 0 \\ 0 & \kappa_3 & -(\kappa_4 + \kappa_5) & \kappa_6 \\ 0 & 0 & \kappa_5 & -(\kappa_6 + \kappa_7) \end{bmatrix} \begin{bmatrix} n_{\text{I}} \\ n_{\text{II}} \\ n_{\text{III}} \\ n_{\text{IV}} \end{bmatrix} \quad (19)$$

384 Here,  $n$  are the fractions of the four states, which sum up  
385 to one,  $\sum n_i = 1$ . The  $\kappa_i$  (in  $\text{s}^{-1}$ ) are the rate constants of  
386 the model, where  $\kappa_1$  and  $\kappa_7$  are a function of the calcium  
387 concentration. In particular,  $n_{\text{I}}$  and  $n_{\text{II}}$ , are the fractions of  
388 dephosphorylated and phosphorylated myosin heads that are  
389 not attached to the actin filament, and thus not mechanically  
390 contributing.  $n_{\text{III}}$  and  $n_{\text{IV}}$  are the fractions of phosphory-  
391 lated and dephosphorylated myosin heads, or cross-bridges,  
392 attached to the actin filaments, and thus contributing to the  
393 stiffness. The power stroke occurs through a conformational  
394 change in state III, after which the myosin heads transform  
395 back into state II. As long as the myosin heads remain phos-  
396 phorylated, they cycle back and forth between states II and  
397 III, thus generating contraction. In state IV, the myosin heads  
398 are still attached to the actin filament but dephosphorylated  
399 and thus unable to perform a power stroke.

400 In Eq. (18),  $u_{\text{rs}}$  is the average normalised relative slid-  
401 ing between the myosin and the actin filaments. It follows a  
402 viscous evolution law:

$$403 \dot{u}_{\text{rs}} = \frac{1}{\eta} [P^{\text{smc}} - P^{\text{mat}}], \quad (20)$$

404 where  $\eta$  is a viscosity parameter (in MPa s),  $P^{\text{smc}}$  denotes the  
405 active stress exerted by the attached myosin heads and  $P^{\text{mat}}$   
406 denotes the stress from the surrounding matrix. The active  
407 stress  $P^{\text{smc}}$  can be approximated by the following step func-  
408 tion:

$$409 P^{\text{smc}} = \begin{cases} \kappa_c n_{\text{III}} & \text{for } P^{\text{mat}} < \kappa_c n_{\text{III}} \\ P^{\text{mat}} & \text{else} \\ \kappa_c [n_{\text{III}} + n_{\text{IV}}] & \text{for } \kappa_c [n_{\text{III}} + n_{\text{IV}}] < P^{\text{mat}}, \end{cases} \quad (21)$$

410 where  $\kappa_c$  is a material parameter (in MPa) related to the driv-  
411 ing force per myosin head, see Murtada et al. (2010) and  
412 Kroon (2010) for details. Smooth muscle cell degradation is  
413 governed by two damage variables,  $d_{\text{pas}}^{\text{smc}}$  characterising the  
414 damage to the surrounding matrix and  $d_{\text{act}}^{\text{smc}}$  characterising  
415 the damage to the smooth muscle cells themselves:

$$416 d_{\text{pas}}^{\text{smc}} = \gamma_{\text{pas}}^{\text{smc}} [1 - \exp(-\beta^{\text{mat}} / m_{\text{pas}}^{\text{smc}})], \quad (22)$$

$$417 d_{\text{act}}^{\text{smc}} = \gamma_{\text{act}}^{\text{smc}} [1 - \exp(-\beta^{\text{smc}} / m_{\text{act}}^{\text{smc}})].$$

418 The internal variable for matrix damage  $\beta^{\text{mat}}$  is defined in  
419 Eq. (12), and the internal variable for smooth muscle cell  
420 damage  $\beta^{\text{smc}}$  is defined as:

$$421 \beta^{\text{smc}} = \max_{0 \leq t \leq \tau} (\widehat{\Psi}^{\text{smc}}(t) - \Psi_0^{\text{smc}}). \quad (23)$$

Both keep track of the loading history through the maximum value of the elastic matrix and smooth muscle cell energies experienced so far.

In the present application, damage values are relatively low and no localised deformation has been observed. To avoid the loss of uniqueness of the underlying boundary value problem in the context of larger damage values, we recommend the use of gradient enhanced damaged models, see Kuhl and Ramm (1999), Mahnken and Kuhl (1999) for details.

In general, it would be possible to also include viscous effects. However, viscosity plays a rather minor role in arterial clamping. Firstly, in view of the application of tissue overload prevention in surgery, an overestimation is more acceptable than an underestimation. Not including viscosity will result in an overestimation of the loading. Secondly, during surgery, the typical movements of a surgeon are at a rather low frequency of maximally 2 Hz.

### 3 Computational modelling of arteries

This section addresses the implementation of the arterial model into the finite element programme Abaqus.

#### 3.1 Implementation

The constitutive model is implemented in the Abaqus user subroutine UANISOHYPER\_INV, a family of subroutines designed for anisotropic, hyperelastic material models, in which the strain energy density function  $\Psi$  is formulated as a function of the strain invariants. This subroutine can handle and update solution-dependent internal variables and requires that the derivatives of the strain energy function are defined with respect to the scalar invariants  $\bar{I}_1, \bar{I}_2, \bar{I}_3, \bar{I}_4^{\text{fib}}, \bar{I}_6^{\text{fib}}, \bar{I}_4^{\text{smc}}$ , which are provided as input. It is called at each integration point during each load increment to calculate the total strain energy  $\Psi$  and its first and second derivatives with respect to the invariants  $\partial\Psi/\partial\bar{I}_i$  and  $\partial^2\Psi/\partial\bar{I}_i\partial\bar{I}_j$  for  $i, j = 1, 2, 3, 4^{\text{fib}}, 6^{\text{fib}}, 4^{\text{smc}}$ .

Through the input file, a local coordinate system must be set, containing the local directions  $\alpha^{\text{fib}}$  for the collagen fibres and  $\alpha^{\text{smc}}$  for the smooth muscle cells. When defining the material, memory must be allocated for nine solution-dependent state variables, namely the damage driving forces  $\beta^{\text{mat}}, \beta^{\text{fib}_1}, \beta^{\text{fib}_2}$ , and  $\beta^{\text{smc}}$ , and the damage thresholds  $\Psi_0^{\text{mat}}, \Psi_0^{\text{fib}_1}, \Psi_0^{\text{fib}_2}$ , and  $\Psi_0^{\text{smc}}$ . The ninth state-dependent variable is the relative sliding  $u_{\text{rs}}$  in the actin-myosin complex, which needs to be stored because of its viscous nature.

The anisotropic, hyperelastic, user-defined material model must be specified with all the material parameters described above, choosing the options `'formulation = invariant'`, `'local directions = 3'` and `'type =`

**Table 1** Parameter sets for cyclic uniaxial tension and compression test in Sect. 3.2

Parameter	Var 1	Var 2	Var 3	Var 4
$\mu^{\text{smc}}$	0.0 kPa	0.0 kPa	0.2 kPa	0.2 kPa
$\gamma^i$	0.0 (-)	0.9 (-)	0.0 (-)	0.9 (-)

$i = \text{mat, fib, smc}_{\text{pas}}, \text{smc}_{\text{act}}$

All other material parameters can be found in Table 2

incompressible'. A conceptual drawback of the UANISOHYPER\_INV subroutine is that it does not provide access to the time step of the solution process, which should be known for correct programming of the viscous evolution law described in Eq. (20). This implies that the exact time step is only known if a fixed time increment is set, by adding the option `'direct'` to the keyword `'static'` in the input file. Otherwise, only the minimum and maximum allowable time step can be externally prescribed.

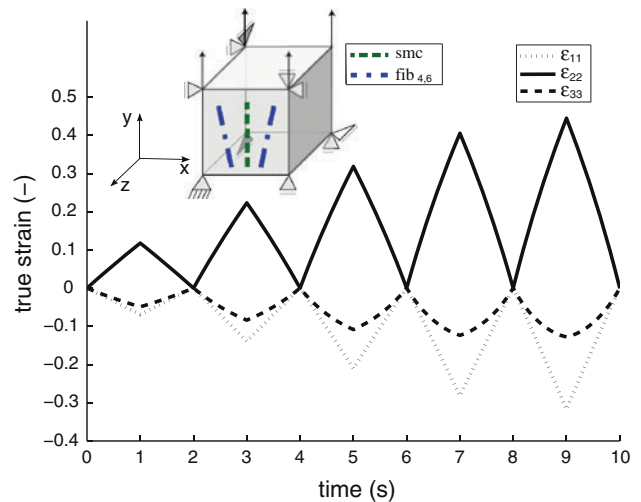
#### 3.2 Model problem of cyclic uniaxial tension and compression

The new constitutive model was tested for the simple model problem of cyclic uniaxial tension and compression using a hexahedral C3D8H element. Homogeneous boundary conditions were applied, namely a gradually increasing, sawtooth stretch pattern, as shown in Fig. 1. To explore the parameter sensitivity of the model, four different sets of material parameters were compared in tension by altering the smooth muscle cell stiffness  $\mu^{\text{smc}}$  and the damage weighting factor  $\gamma^i$ , see Table 1. All other parameters were selected according to the rationale explained in Sect. 4.2 as shown in Table 2.

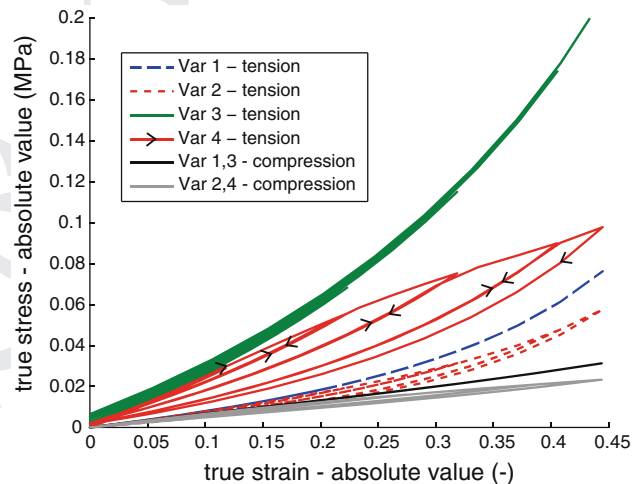
As a first benchmark test, the three-constituent damage model was compared with the Abaqus implementation of the standard Holzapfel–Gasser–Ogden model, where the smooth muscle cell stiffness  $\mu^{\text{smc}}$  and the damage weighting factors  $\gamma^i$  were set to zero (variation 1). Both simulations yielded exactly the same results, verifying the correct implementation of the baseline model. Next, different features of the model were gradually added and evaluated for consistency. Figure 2 shows the stress–strain curves for the prescribed loading pattern from Fig. 1 for four variations of the new material model in tension and two variations in compression. By turning off the smooth muscle contribution  $\mu^{\text{smc}}$  and the damage  $\gamma^i = 0$  in variation 1, the model captures the Holzapfel–Gasser–Ogden material by Abaqus as a special case. When the damage material parameter  $\gamma^i$  is increased to 0.9 (-) in variation 2, the dashed red curve is obtained, showing the progressive failure of the fibres and matrix material. When the smooth muscle stiffness  $\mu^{\text{smc}}$  is increased to a value of 0.2 MPa in variation 3, the solid green curve is obtained. It shows how, in the fully contracted state, the smooth muscle

**Table 2** Parameters used in the finite element model

Parameter	Value	Source
<i>Matrix material</i>		
$c$	23.63 kPa	Famaey et al. (2012)
$\gamma^{\text{mat}}$	0 (-)	Not studied
$m^{\text{mat}}$	/ kPa	Not studied
<i>Collagen fibres</i>		
$\alpha^{\text{fib}}$	$\pm 5^\circ$	O'Connell et al. (2008)
$k_1$	32.51 kPa	Famaey et al. (2012)
$k_2$	3.05 (-)	
$\kappa$	0.16 (-)	
$\gamma^{\text{fib}}$	0 (-)	Not studied
$m^{\text{fib}}$	/ kPa	Not studied
<i>Smooth muscle cells—chemical rate constants</i>		
$\kappa_1, \kappa_6$	$0.14 \text{ s}^{-1}$	Hai and Murphy (1988)
$\kappa_2, \kappa_5$	$0.5 \text{ s}^{-1}$	
$\kappa_3, 4\kappa_4$	$0.44 \text{ s}^{-1}$	
$\kappa_7$	$0.01 \text{ s}^{-1}$	
<i>Smooth muscle cells—mechanical constants</i>		
$\mu^{\text{smc}}$	0.25 MPa	Fitted to experiments
$\kappa_c$	0.93 MPa	Fitted to experiments
$\eta$	60 MPa s	Murtada et al. (2010)
$\alpha^{\text{smc}}$	$0^\circ$	O'Connell et al. (2008)
$\gamma_{\text{act}}^{\text{smc}}$	0 (-)	Not studied
$m_{\text{act}}^{\text{smc}}$	/ kPa	Not studied
$\gamma_{\text{pas}}^{\text{smc}}$	0.9 (-)	Fitted to experiments
$m_{\text{pas}}^{\text{smc}}$	0.03 kPa	Fitted to experiments



**Fig. 1** Strain profile for homogeneous cyclic uniaxial tension and compression test.  $\epsilon_{11}$ ,  $\epsilon_{22}$  and  $\epsilon_{33}$  are the strains in the three principal directions. The lines in the block depict the average direction of the two collagen fibre families and the smooth muscle cells



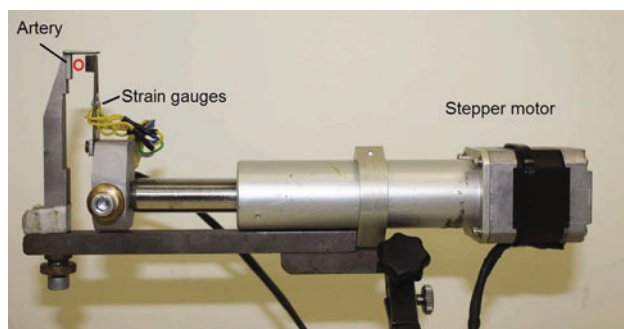
**Fig. 2** Stress-strain curve for a homogeneous cyclic uniaxial tension test and a compression test. Curves correspond to healthy smooth muscle, fibres and matrix material (solid green), progressively damaging smooth muscle, fibres and matrix (solid red with arrows), no smooth muscle with healthy fibres and matrix (dashed blue), and progressively damaging fibres and matrix (dashed red), all in tension. The solid black curve corresponds to healthy material in compression, and the solid grey curve corresponds to progressively damaging material in compression. Note that the absolute values of the stress and the strain are provided. The prescribed loading profile is shown in Fig. 1. The different sets of material parameters are summarised in Table 1

512 cells actively contribute to the stiffness. A slight effect of the  
 513 contractile element can be observed. When the damage material  
 514 parameter  $\gamma^i$  is increased to 0.9 (-) in variation 4, the  
 515 solid red curve with arrows is obtained, clearly demonstrat-  
 516 ing the progressive smooth muscle cell degradation as well  
 517 as the degradation of the fibres and the smooth muscle cells.  
 518 By increasing or decreasing the damage weighting factor  $\gamma^i$   
 519 within the range  $0 < \gamma^i < 1$ , the solid red curve with arrows  
 520 decreases or increases, respectively, bounded from above and  
 521 below by the solid green and dashed blue lines.

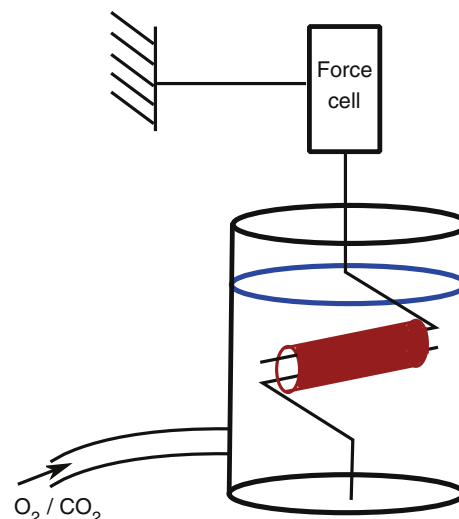
522 The solid black curve is obtained when loading variation  
 523 1 or variation 3 of the model in compression. In this regime,  
 524 the smooth muscle cells do not contribute and the fibres contrib-  
 525 ute only very slightly due to their small angle with respect  
 526 to the loading direction. The grey curve, finally, is obtained  
 527 when variations 2 or 4 are loaded in compression. Again, pro-  
 528 gressive degradation (of the matrix material) can be observed.  
 529 Note that in these last two curves the absolute values of the  
 530 stress and the strain are provided.

#### 4 Smooth muscle cell damage through clamping

531  
 532 The three-constituent damage model is put to use to simulate  
 533 the damage process occurring during the clamping of a rat  
 534 abdominal artery. To test the realism of the model, the results  
 535 were compared with actual experiments, more thoroughly  
 536 described in Famaey et al. (2010), in which the abdominal



**Fig. 3** Mechanical clamping device



**Fig. 4** Custom made functional testing device. Two rods slide into the lumen of the sample, one rod is connected to the base of the set-up, the other to a load cell suspended above the set-up, so that isometric tension can be recorded. The sample is immersed in water-jacketed organ chamber filled with Krebs buffer

537 arteries of rats were clamped up to a defined clamping force.  
 538 Subsequently, to quantify the degradation of the smooth muscle  
 539 cells, the contracting capability of the clamped segment  
 540 was measured in a myograph as explained in Sect. 4.1. Both  
 541 experimental processes, that is, arterial clamping and subse-  
 542 quent myograph testing, were simulated numerically using  
 543 the three-constituent damage model as described in Sect. 4.2.

#### 544 4.1 Experimental model

##### 545 *Arterial clamping*

546 In order to correlate the degree of damage to the degree of  
 547 mechanical loading to which the tissue was previously sub-  
 548 jected, loading should be applied in a controllable way. Ide-  
 549 ally, loading should be applied *in vivo*, so that the induced  
 550 damage can be solely attributed to the loading and not to non-  
 551 physiological *ex vivo* conditions. Since subsequent damage  
 552 quantification requires excision of tissue, undamaged control  
 553 segments should also be excised and tested as controls,  
 554 to rule out damage due to the excision process. To clamp the  
 555 artery in a controlled way, a hand-held mechanical device,  
 556 shown in Fig. 3, was designed that allows clamping of a rat  
 557 abdominal artery in an *in vivo* setting to a known force, mea-  
 558 sured with strain gauges on the clamping arms (Famaey et al.  
 559 2010).

##### 560 *Functional damage assessment*

561 One damage quantification method is to compare the degree  
 562 of functionality of a damaged tissue to that of an intact one.  
 563 For the specific case of arterial tissue, functionality refers to  
 564 the vasoregulating capability of the tissue, that is, the poten-  
 565 tial of the smooth muscle cells to contract or relax in order  
 566 to regulate the blood pressure. This vasoregulating capabil-  
 567 ity can be quantified in an experimental setup, known as a  
 568 ‘myograph’.

569 Schematically shown in Fig. 4, the myograph consists of  
 570 a water-jacketed organ chamber in which an excised cylind-  
 571 rical section of an artery can be mounted. Two rods slide

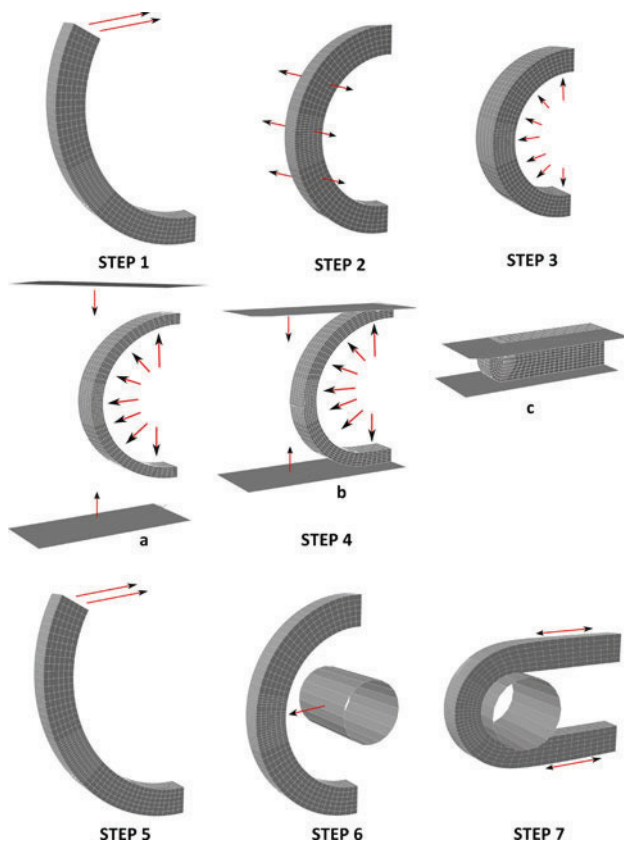
572 into the lumen of the sample, whereby one rod is connected  
 573 to the base of the setup, and the other to a load cell suspen-  
 574 ded above the set-up, so that isometric tension can be recorded.  
 575 The height of the load cell can be manually adjusted to set  
 576 an optimal preload on the sample. The sample is immersed  
 577 in a Krebs buffer at 37 °C and continuously gassed with a  
 578 mixture of 95% oxygen and 5% carbon dioxide. After stabi-  
 579 lisation at the optimal preload level, Phenylephrine (PE) at  
 580  $10^{-6}$ M is added to the solution to induce contraction. PE is  
 581 a contracting agent that acts directly on the smooth muscle  
 582 cells. Sodium nitroprusside (SNP) ( $10^{-6}$ M) induces an endo-  
 583 thelium-independent relaxation so consequently an adequate  
 584 level of SNP-induced relaxation will indicate intactness of  
 585 the smooth muscle cells (Callera et al. 2000). Absolute val-  
 586 ues of relaxation as well as the percentage of relaxation rela-  
 587 tive to the amount of contraction are recorded and provide  
 588 a quantitative measure of the damage to the smooth muscle  
 589 cells when comparing these values to those of an intact sam-  
 590 ple. More details on the experimental setup can be found in  
 591 Famaey et al. (2010). A similar custom-designed device to  
 592 test active force generation in response to electrical stimula-  
 593 tion is reported in Böl et al. (2012).

#### 594 4.2 Computational model

##### 595 *Arterial clamping*

596 A three dimensional finite element model was built in Aba-  
 597 quus/Standard 6.10-2. Here, an idealised cylindrical geometry  
 598 was used with an outer radius of 0.58 mm, a wall thickness  
 599 of 0.14 mm and an initial length of 0.1 mm. These values





**Fig. 5** Schematic overview of the seven steps in the FE simulation representing the loading history of arterial clamping (steps 1–4) and the functional damage assessment (steps 5–7)

of the third step, the undamaged elastic strain energy of each of the four constituents is written into a matrix of internal or 'solution-dependent variables' for each integration point, using Python scripting. These are the initial damage threshold levels  $\Psi_0^i$ , described in Eqs. (12), (16) and (23) to be used in step 4.

Step 4 starts with a new input file, in which the state of the artery after the first three steps is imported. By importing, the deformations are included as 'initial values' for the model. The solution-dependent variables defined earlier contain the damage threshold levels  $\Psi_0^i$  specified as 'initial conditions' in the input file. The material model is now updated to enable damage accumulation,  $\gamma^i > 0$ , and four extra solution-dependent variables, representing the  $\beta^i$  described in Eqs. (12), (16) and (23) are added. In addition, two extra parts are added to the assembly of the system, namely an upper and lower clamp, which are gradually moved towards each other during step 4, until a clamping force of 5 mN is reached. A friction coefficient of  $\mu^{\text{clamp}} = 0.5$  is used between the clamp and the outer arterial surface. Finally, also the internal pressure boundary conditions are modified to a pulsating pressure between 10 and 16 kPa, that gradually decays to zero when the vessel is completely closed. To keep track of the maximum energy level reached for each constituent at every integration point of the system, the four extra solution-dependent variables are updated and stored at each step as internal variables  $\beta^i$ . At the end of the simulation, these solution-dependent variables are again written to a matrix using Python scripting to inform the next step.

#### Functional damage assessment

After clamping, damage has accumulated in the different constituents. For the smooth muscle cells, this amount of damage can be calibrated and validated in a myograph, as explained in Sect. 4.1. The simulation starts from the same mesh as in step 1 of Sect. 4.2. This time, however, the initial conditions are specified for the solution-dependent variables taking into account the earlier loading history through the internal variables  $\beta^i$ . The material model is adapted, such that damage due to the energy accumulation of clamping is present, but no further damage is induced. Similar to step 1 of Sect. 4.2, the segment is closed to form a half cylinder in step 5, thus incorporating the circumferential residual stress. To reproduce the experimental situation, this time, no longitudinal stretch or internal pressure was added. Next, in step 6, a rod is translated radially from inside the section, pulling it until it exerts a certain load, corresponding to the experimentally measured value after complete relaxation due to the addition of SNP. A friction coefficient of  $\mu^{\text{rod}} = 0.5$  is used between the rod and the outer arterial surface. Up to the end of step 6, no smooth muscle cell contribution is added in the material model. This is accomplished by multiplying

the fractions  $n_{III}$  and  $n_{IV}$  with a switch function that is set to zero in steps 5 and 6.

After reaching the relaxed state, in the final step, the switch function is smoothly ramped to one, so that the smooth muscle cells reach the completely contracted state. Physiologically, this situation corresponds to the state after the addition of PE. In this step only, because of the time dependence of the evolution law for the relative sliding  $u_{rs}$ , the time step of the implicit solution scheme is fixed to  $dt = 10^{-5}$ . Figure 5 gives a schematic overview of all seven steps of the simulation.

### Parameter selection

Table 2 gives an overview of all parameters of the material model. The first set of parameters are related to the extracellular matrix with two embedded fibre families. For the rat abdominal aorta, the main direction of the collagen fibres  $\alpha^{fib}$  is set to  $\pm 5^\circ$ , that is, it is almost aligned with the circumferential direction, see O'Connell et al. (2008). The four remaining parameters are set to  $\kappa = 0.16$  (-),  $k_1 = 32.51$  kPa,  $k_2 = 3.05$  (-) and  $c = 23.63$  kPa, using experimental data from extension-inflation tests as described in Famaey et al. (2012). Alternatively, a parameter set from human arteries can be found in Stålhand (2009).

The next set of parameters are the rate constants of the chemical model defining the fractions  $n_{III}$  and  $n_{IV}$  in equation (see Eq. 19). They are chosen according to Hai and Murphy (1988). These values led to the fractions of  $n_{III} = 0.164$  and  $n_{IV} = 0.547$ , which were used as fixed input values into the mechanical model. Additional parameters are related to the mechanical model of the smooth muscle cell contribution. According to O'Connell et al. (2008), the smooth muscle cells of rat abdominal arteries are oriented circumferentially with  $\alpha^{smc} = 0^\circ$ . The parameter  $\mu^{smc}$  depending on the stiffness of the actin-myosin filament structure and the parameter  $\kappa_c$  related to the driving force per cross-bridge were both tuned to fit the experimental contraction measured in the myograph due to addition of PE for a previously undamaged segment, as described in Sect. 4.1. The viscous damping constant  $\eta$  was set to 60 MPa s, corresponding to the value used in Murtada et al. (2010).

To characterise damage progression appropriately, two parameters need to be calibrated for each constituent, plus two additional ones for the smooth muscle cells, totalling ten parameters. Since the myograph experiment only allows for damage quantification in the smooth muscle cells, with the current setup, no reasonable damage parameters can be defined for the extracellular matrix and the collagen fibres. Additional complementary experiments will be needed for this task, as discussed in Sect. 5. Accordingly, here,  $\gamma^{mat}$  and  $\gamma^{fib}$  were set to zero, such that  $m^{mat}$  and  $m^{fib}$  can take any

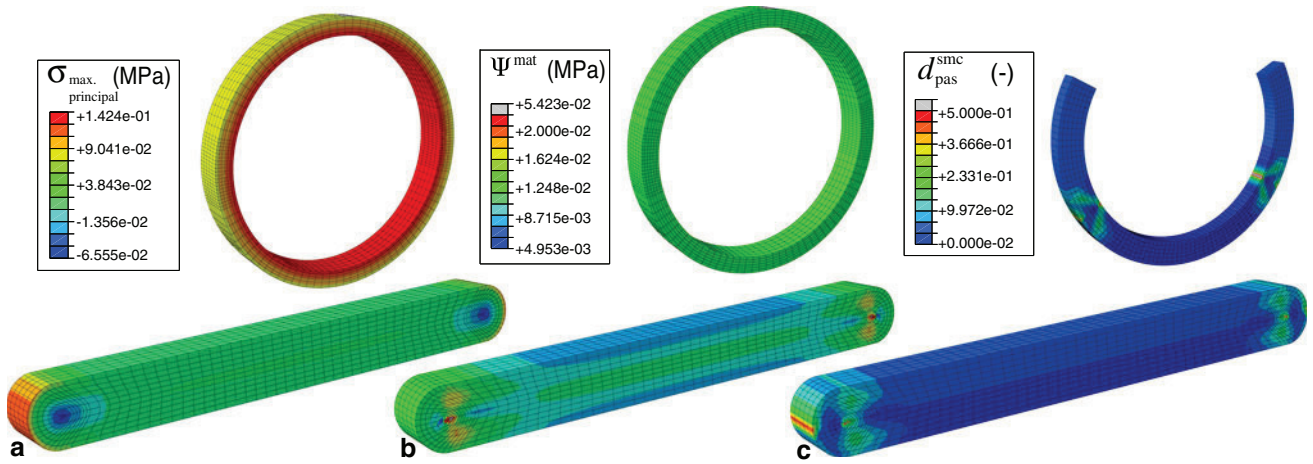
arbitrary value. Secondly, the assumption was made that, during clamping, the smooth muscle cells were completely passive, and thus not contributing to the stiffness. Consequently, no damage could accumulate here, so that  $\gamma_{act}^{smc}$  could also be set to zero, and  $m_{act}^{smc}$  to an arbitrary value. The two remaining parameters  $\gamma_{pas}^{smc}$  and  $m_{pas}^{smc}$  were then calibrated using the experimental data. For a systematic approach to calibrate damage material parameters in a heterogeneous setting, the reader is referred to Mahnken and Kuhl (1999).

### 4.3 Results

The top image in Fig. 6a shows the maximum principal stress in an arterial segment in the systolic physiological state. This state defines the damage threshold above which damage is initiated. In the lower image of Fig. 6a, the maximum principal stress is shown for the same arterial segment when clamped up to a clamping force of 5 mN. Figure 6b shows the same set of images, this time displaying the elastic strain energy in the matrix material,  $\widehat{\Psi}^{mat}$ , that is, the driving force for both isotropic matrix damage  $d^{mat}$  and passive smooth muscle cell damage  $d_{pas}^{smc}$ . As shown in the lower image of Fig. 6c, the clamping has induced an inhomogeneous damage pattern to the smooth muscle cells. Even when the segment returns to its reference state (top image in Fig. 6c), this damage is irreversible and remains.

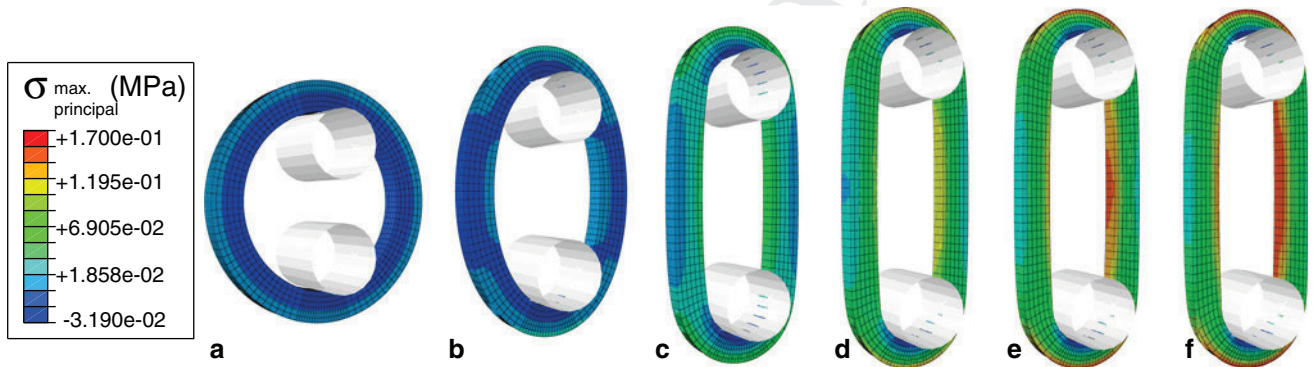
Figure 7 shows snapshots of the myograph experiment, with the colour code depicting the maximum principal stress. The left graph of Fig. 8 shows the force measured in the rods of the myograph as a function of time, for a previously undamaged segment, solid line, and for a segment that was previously clamped at 5 mN, dashed. The letters along the curve correspond to the stages shown in Fig. 7. The first section of the graph corresponds to step 6 of the simulation, that is, the pulling of the rod to the passive state. After 2 s, the smooth muscle cells are activated, corresponding to step 7.

The right graph of Fig. 8 shows the force measured in the rod for a segment that was previously clamped with the device described in Sect. 4.1 to a level of 5 mN, normalised to the width of the numerical model, and for a segment that was undamaged. The force in the rod was also normalised to the width of the numerical model. Again, in the first section of the graph, the rod is gradually pulled to reach the passive preload state. At the point indicated with the arrow, PE is added to the Krebs solution, triggering the activation of the smooth muscle cells. Note that the time scales in the two graphs do not agree. To calibrate the model appropriately, an additional time parameter would have to be included into the model. Here, however, we were only interested in the end result of the curve, rather than in calibrating the model to real physical times.



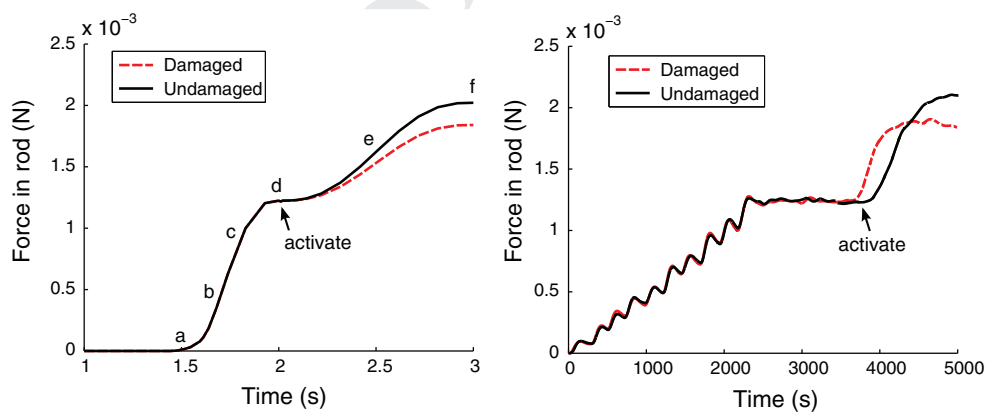
**Fig. 6** **a** Maximum principal stress in an arterial segment in systolic physiological state (*top image*), and when clamped up to a clamping force of 5 mN (*lower image*). **b** Strain energy in the same two segments as in **(a)**. **c** Damage variable  $d_{pas}^{smc}$  in the same two segments as in **(a)**,

when clamped up to a clamping force of 5 mN (*lower image*). This damage remains, even when the segment returns to its reference state (*top image*)



**Fig. 7** Different stages of the myograph experiment, with the colour code depicting the maximum principal stress. In stages a, b and c, the rods are being pulled to the preload force (step 6 of the numerical sim-

ulation). In stages d, e and f, the rods remain in position and the smooth muscle cells are activated (step 7 of the numerical simulation)



**Fig. 8** The *left graph* shows the force measured in the rod of the myograph as a function of time, for a previously undamaged segment (*solid line*) and for a segment that was previously clamped at 5 mN (*dashed*). The *letters along the curve* correspond to the snapshots shown in Fig.

*7*. The *right graph* shows the force measured in the rod during an experiment, for a segment that was previously clamped with the device described in Sect. 4.1 to a level of 5 mN and for a segment that was undamaged, both normalised to the width of the numerical model

## 774 5 Discussion

775 In this article, a three-constituent damage constitutive model  
 776 was proposed to simulate the damage process in arterial tissue.  
 777 After testing the model in a homogeneous model problem  
 778 under cyclic uniaxial tension and compression, it was  
 779 used in a finite element simulation for the clamping of an  
 780 artery and the subsequent damage evaluation in a myograph.  
 781 The model enables the analysis of the inhomogeneous damage  
 782 profile in the artery due to loading, quantitatively showing  
 783 which constituents and which sections are overloaded, compared  
 784 with the physiological state. In response to overload, driven  
 785 by the free energy, anisotropic damage develops in the smooth  
 786 muscle cells. The three-constituent damage model and numerical  
 787 simulation provide a useful tool to explore safe loading of  
 788 arterial tissue. Being able to reliably predict loading regimes  
 789 which initiate tissue damage is important in view of robotic  
 790 surgery, which lacks the natural feedback of human touch,  
 791 by which the experienced surgeon today guarantees safe tissue  
 792 loading.

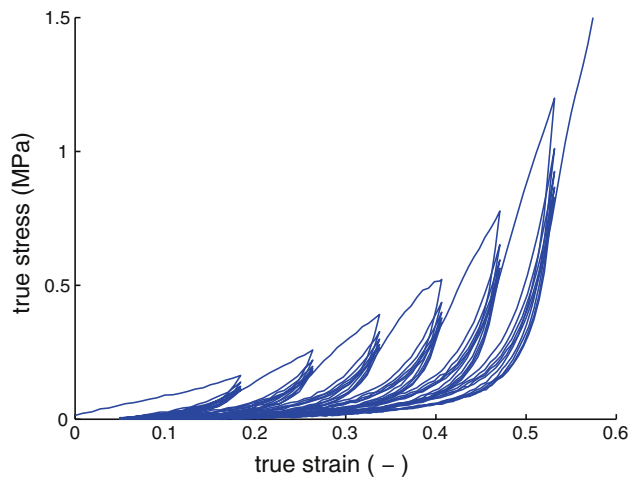
793 The material model described in Sect. 2 introduces a large  
 794 set of parameters, which need to be experimentally defined  
 795 for each tissue type. Extensive experimental data from a range  
 796 of different experiments is required to correctly calibrate all  
 797 parameters. Section 4.2 comments on the rationale behind the  
 798 parameter selection for this study. The goal of this study was  
 799 to demonstrate the feasibility of the proposed model and to  
 800 illustrate a conceptual methodology for the damage characterisation  
 801 in smooth muscle cells. Accordingly, less emphasis was placed  
 802 on the exact parameter identification for the other model  
 803 parameters. As explained in Sect. 2.2, four damage processes  
 804 can be captured by the model, one for each constituent. Each  
 805 damage process is assumed to be driven by the individual free  
 806 energy of that constituent. For smooth muscle cells, passive  
 807 damage is also affected by the energy in the matrix constituent.  
 808 Here, we focus in particular on this last passive part of damage,  
 809 assuming that smooth muscle cells are inactive during the real  
 810 clamping process. The damage parameters were chosen to  
 811 correspond to the results of an *ex vivo* experiment. In the  
 812 future, further experiments will be performed with different  
 813 clamping force levels to calibrate the model for a wider loading  
 814 range. To enable numerical comparison with higher clamping  
 815 force levels, it might become relevant to remesh the clamped  
 816 segment to avoid excessive element distortion. However, remeshing  
 817 would require the mapping of the solution, both from the node  
 818 points and from the integration points, onto the new mesh,  
 819 a feature currently still lacking for anisotropic materials in  
 820 Abaqus 6.10.

821 In order to accurately identify the damage parameters for  
 822 the different constituents, different, ideally orthogonal,  
 823 experiments are required that enable the extraction of this  
 824 specific information. Damage in the collagen fibres under

825 tension can possibly be studied using microscopic images  
 826 of the tissue at different stages in the stretching process  
 827 and assessing the images for collagen rupture. In fact, the  
 828 extension-inflation tests that were used here to calibrate the  
 829 undamaged baseline parameters of the Holzapfel model most  
 830 probably already induced damage to both collagen fibres and  
 831 matrix in the higher pressure regimes. Damage in the collagen  
 832 fibres and matrix should therefore ideally be calibrated  
 833 simultaneously, possibly through extension-inflation tests.  
 834 Damage to the smooth muscle cells is assumed to depend  
 835 on both damage of the passive extracellular matrix and damage  
 836 of the active smooth muscle cells themselves. Damage in the  
 837 passive regime has been observed and characterised  
 838 experimentally in Famaey et al. (2010) and calibrated in this  
 839 manuscript using these data. It results in a reduced activation  
 840 capability, which will only become apparent upon activation.  
 841 Damage in the active regime is caused by excessive tension  
 842 in the direction of the contractile unit, which might cause  
 843 ruptures in the myosin cross-bridges or rupture of the actin  
 844 and myosin filaments. It is included here merely theoretically  
 845 for the sake of completeness, but has not been calibrated yet.  
 846 We are currently in the process of further investigating these  
 847 phenomena to characterise the mechanisms underlying active  
 848 damage.

849 Note also that in the finite element model, the artery was  
 850 modelled as a single homogeneous layer, even though the  
 851 wall consists of two solid mechanically relevant layers, that  
 852 is, the media and the adventitia. However, in the case of a rat  
 853 abdominal artery, the complete wall thickness is only approx-  
 854 imately 0.14 mm thick, and in contrast to human tissue, it  
 855 is impossible to separate these two layers from each other.  
 856 Therefore, the most accurate approach was to model the wall  
 857 as a single layer. The assumption was also made that damage  
 858 initiates once the energy level exceeds that of the energy level  
 859 at systolic blood pressure. This was motivated by the fact that  
 860 the morphology and properties of the arterial wall change due  
 861 to chronic hypertension (Matsumoto and Hayashi 1994), but  
 862 whether this actually justifies this assumption for acute damage  
 863 scenarios should still be experimentally validated.

864 Although the three-constituent damage model already  
 865 captures a number of typical features of cardiovascular tissue,  
 866 some characteristic aspects are still not included, and a few  
 867 limitations remain. When qualitatively comparing the simulated  
 868 homogeneous cyclic tension test described in Sect. 3.2 to the  
 869 experimental results of a uniaxial tensile test on a sheep  
 870 carotid artery, shown in Fig. 9, several features, for example,  
 871 tissue nonlinearity and discontinuous softening are accurately  
 872 captured. However, in the tensile test on the sheep carotid  
 873 artery, cycling up to a certain strain level was performed five  
 874 times before the next strain level was reached, and clearly  
 875 softening does continue in these cycles, even though the  
 876 maximum energy level, the parameter  $\beta$  in our model is not  
 877 increased. This continuous damage behaviour



**Fig. 9** Uniaxial tensile test on a circumferentially oriented strip of a sheep carotid artery. The test was performed on a tensile test bench (INSTRON 5567). Cyclic loading at gradually increasing levels of elongation was applied at a crosshead speed of 1 mm/s. The tests were performed with continuous recording of tensile force, with a 1 kN load cell and gauge length, based on crosshead displacement, at a sampling frequency of 10 Hz. Cycling up to a certain strain level was performed five times before the next strain level was reached, for six increasing levels of strain

in the long term, the proposed model could enable the prediction of surgically induced damage evolution in real time. This would allow loading thresholds to be imposed on surgical instruments during an operation in a robotic teleoperation setting.

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## References

- Arruda EM, Boyce MC (1993) A three-dimensional constitutive model for the large stretch behavior of rubber elastic materials. *J Mech Phys Solids* 41(2):389–412
- Balzani D, Schröder J, Gross D (2006) Simulation of discontinuous damage incorporating residual stresses in circumferentially overstretched atherosclerotic arteries. *Acta Biomater* 2(6):609–618
- Balzani D, Schröder J, Gross D (2007) Numerical simulation of residual stresses in arterial walls. *Comput Mater Sci* 39:117–123
- Balzani D, Böse D, Brads D, Erbel R, Klawonn A, Reinbach O, Schröder J (2011) Parallel simulation of patient-specific atherosclerotic arteries for the enhancement of intravascular ultrasound diagnosis. *Eng Comp* (submitted)
- Barone GW, Conerly JM, Farley PC, Flanagan TL, Kron IL (1989) Assessing clamp-related vascular injuries by measurement of associated vascular dysfunction. *Surgery* 105(4):465–471
- Böl M, Abilez OJ, Assar AN, Zarins CK, Kuhl E (2012) In vitro/in silico characterization of active and passive stresses in cardiac muscle. *Int J Multiscale Comput Eng* (in press)
- Callera GE, Varanda WA, Bendhack LM (2000) Impaired relaxation to acetylcholine in 2k-1c hypertensive rat aortas involves changes in membrane hyperpolarization instead of an abnormal contribution of endothelial factors. *Gen Pharmacol* 34(6):379–389
- Calvo B, Pena M, Martinez M, Doblaré M (2007) An uncoupled directional damage model for fibred biological soft tissues. Formulation and computational aspects. *Int J Numer Methods Eng* 69: 2036–2057
- Dargazany R, Itskov M (2009) A network evolution model for the anisotropic Mullins effect in carbon black filled rubbers. *Int J Solids Struct* 46(16):2967–2977
- De S, Rosen J, Dagan A, Hannaford B, Swanson P, Sinanan M (2007) Assessment of tissue damage due to mechanical stresses. *Int J Robot Res* 26:1159–1171
- Ehret A, Itskov M (2009) Modeling of anisotropic softening phenomena: application to soft biological tissues. *Int J Plast* 25:901–919
- Famaey N, Vander Sloten J (2008) Soft tissue modelling for applications in virtual surgery and surgical robotics. *Comput Methods Biomech Biomed Eng* 11(4):351–366
- Famaey N, Verbeken E, Vinckier S, Willaert B, Herijgers P, Vander Sloten J (2010) In vivo soft tissue damage assessment for applications in surgery. *Med Eng Phys* 32:437–443
- Famaey N, Sommer G, Vander Sloten J, Holzapfel GA (2012) Experimental study and numerical analysis of arterial clamping. *J Mech Behav Biomed Mater* (accepted)
- Fung YC (1970) Mathematical representation of the mechanical properties of the heart muscle. *J Biomech* 3(4):381–404
- Gasser TC, Ogden RW, Holzapfel GA (2006) Hyperelastic modelling of arterial layers with distributed collagen fibre orientations. *J R Soc Interface* 3(6):15–35

- 967 Gestrelus S, Borgström P (1986) A dynamic model of smooth muscle  
968 contraction. *Biophys J* 50(1):157–169
- 969 Gleason RL, Gray SP, Wilson E, Humphrey JD (2004) A multiaxial  
970 computer-controlled organ culture and biomechanical device for  
971 mouse carotid arteries. *J Biomech Eng* 126(6):787–795
- 972 Göktepe S, Kuhl E (2010) Electromechanics of the heart—a unified  
973 approach to the strongly coupled excitation-contraction problem.  
974 *Comput Mech* 45:227–243
- 975 Göktepe S, Acharya SNS, Wong J, Kuhl E (2011) Computational model-  
976 ing of passive myocardium. *Int J Numer Methods Biomed Eng*  
977 27:1–12
- 978 Gupta V, Reddy NP, Batur P (1997) Forces in laparoscopic surgical  
979 tools. *Presence* 6:218–228
- 980 Hai CM, Murphy RA (1988) Cross-bridge phosphorylation and regula-  
981 tion of latch state in smooth muscle. *Am J Physiol* 254(1 Pt  
982 1):C99–106
- 983 Hill A (1938) The heat of shortening and the dynamic constants of mus-  
984 cle. *Proc R Soc Lond B* 126:136–195
- 985 Hokanson J, Yazdani S (1997) A constitutive model of the artery with  
986 damage. *Mech Res Commun* 24(2):151–159
- 987 Holzapfel GA, Ogden RW (2010a) Modelling the layer-specific three-  
988 dimensional residual stresses in arteries, with an application to the  
989 human aorta. *J R Soc Interface* 7:787–799
- 990 Holzapfel GA, Ogden RW (2010b) Constitutive modeling of arteries.  
991 *Proc R Soc Lond A* 466:1551–1597
- 992 Holzapfel GA, Gasser TC, Ogden RW (2000) A new constitutive frame-  
993 work for arterial wall mechanics and a comparative study of material  
994 models. *J Elast* 61:1–48
- 995 Hsi C, Cuenoud H, Soller BR, Kim H, Favreau J, Salm TJV,  
996 Moran JM (2002) Experimental coronary artery occlusion: rele-  
997 vance to off-pump cardiac surgery. *Asian Cardiovasc Thorac Ann*  
998 10(4):293–297
- 999 Itoh A, Krishnamurthy G, Swanson J, Ennis D, Bothe W, Kuhl E, Kar-  
1000 lsson M, Davis L, Miller DC, Ingels NB (2009) Active stiffening  
1001 of mitral valve leaflets in the beating heart. *Am J Physiol Heart*  
1002 *Circ Physiol* 296:1766–1773
- 1003 Kroon M (2010) A constitutive model for smooth muscle including  
1004 active tone and passive viscoelastic behaviour. *Math Med Biol*  
1005 27(2):129–155
- 1006 Kuhl E, Ramm E (1999) Simulation of strain localization with gradient  
1007 enhanced damage models. *Comput Mater Sci* 16:176–185
- 1008 Kuhl E, Maas R, Himpel G, Menzel A (2007) Computational modeling  
1009 of arterial wall growth: Attempts towards patient specific simula-  
1010 tions based on computer tomography. *Biomech Model Mechanobiol*  
1011 6:321–331
- 1012 Kwoh YS, Hou J, Jonckheere EA, Hayall S (1988) A robot with  
1013 improved absolute positioning accuracy for ct guided stereotac-  
1014 tic brain surgery. *IEEE Trans Biomed Eng* 35:153–161
- 1015 Mahnken R, Kuhl E (1999) Parameter identification of gradient  
1016 enhanced damage models with the finite element method. *Eur J*  
1017 *Mech/A Solids* 18:819–835
- 1018 Manchio JV, Gu J, Romar L, Brown J, Gammie J, Pierson RN, Griffith  
1019 B, Poston RS (2005) Disruption of graft endothelium correlates  
1020 with early failure after off-pump coronary artery bypass surgery.  
1021 *Ann Thorac Surg* 79(6):1991–1998
- 1022 Matsumoto T, Hayashi K (1994) Mechanical and dimensional adapta-  
1023 tion of rat aorta to hypertension. *J Biomech Eng* 116(3):278–283
- 1024 Miehe C (1995) Discontinuous and continuous damage evolution in  
1025 ogden-type large-strain elastic materials. *Eur J Mech A/Solids*  
1026 14:697–720
- Mohr FW, Falk V, Diegeler A, Walther T, Gummert JF, Bucerius J,  
1027 Jacobs S, Autschbach R (2001) Computer-enhanced robotic car-  
1028 diac surgery: experience in 148 patients. *J Thorac Cardiovasc Surg*  
1029 121:842–853
- Murtada S-I, Kroon M, Holzapfel GA (2010) A calcium-driven mech-  
1030 anochemical model for prediction of force generation in smooth  
1031 muscle. *Biomech Model Mechanobiol* 9(6):749–762
- O’Connell MK, Murthy S, Phan S, Xu C, Buchanan J, Spilker R, Dalman  
1032 RL, Zarins CK, Denk W, Taylor CA (2008) The three-dimensional  
1033 micro- and nanostructure of the aortic medial lamellar unit mea-  
1034 sured using 3d confocal and electron microscopy imaging. *Matrix*  
1035 *Biol* 27(3):171–181
- Ogden RW, Roxburgh DG (1999) A pseudo-elastic model for the mul-  
1036 lins effect in filled rubber. *Proc R Soc A* 455:2861–2877
- Pena E, Alastrué V, Laborda A, Matrínez M, Doblaré M (2010) A  
1037 constitutive formulation of vascular tissue mechanics including  
1038 viscoelasticity and softening behaviour. *J Biomech* 43:984–989
- Rausch MK, Dam A, Göktepe S, Abilez OJ, Kuhl E (2011) Computa-  
1039 tional modeling of growth: systemic and pulmonary hypertension  
1040 in the heart. *Biomech Model Mechanobiol* 10(6):799–811
- Rhodin JAG (1979) Architecture of the vessel wall. In: Berne RM (ed)  
1041 *Handbook of physiology*, section 2, volume 2. Am. Physiol. Soc.,  
1042 Bethesda
- Rodríguez JF, Cacho F, Bea JA, Doblaré M (2006) A stochastic-struc-  
1043 turally based three dimensional finite-strain damage model for  
1044 fibrous soft tissue. *J Mech Phys Solids* 54(4):864–886
- Sacks MS, Sun W (2003) Multiaxial mechanical behavior of biological  
1045 materials. *Annu Rev Biomed Eng* 5:251–284
- Schmitz A, Böl M (2011) On a phenomenological model for active  
1046 smooth muscle contraction. *J Biomech* 44:2090–2095
- Simo J, Ju J (1987) Strain- and stress-based continuum damage models.  
1047 *Int J Solids Struct* 23:821–840
- Stålhand J (2009) Determination of human arterial wall parameters  
1048 from clinical data. *Biomech Model Mechanobiol* 8(2):141–148
- Stålhand J, Klarbring A, Holzapfel GA (2008) Smooth muscle con-  
1049 traction: mechanochemical formulation for homogeneous finite  
1050 strains. *Prog Biophys Mol Biol* 96:465–481
- Stålhand J, Klarbring A, Holzapfel GA (2011) A mechanochemical  
1051 3d continuum model for smooth muscle contraction under finite  
1052 strains. *J Theor Biol* 268(1):120–130
- Tsamis A, Bothe W, Kvitting JP, Swanson JC, Miller DC, Kuhl  
1053 E (2011) Active contraction of cardiac muscle: in vivo character-  
1054 ization of mechanical activation sequences in the beating heart. *J*  
1055 *Mech Behav Biomed Mater* 4:1167–1176
- Vito RP, Dixon SA (2003) Blood vessel constitutive models-1995–  
1056 2002. *Annu Rev Biomed Eng* 5:413–439
- Volokh KY (2008) Prediction of arterial failure based on a micro-  
1057 structural bi-layer fiber matrix model with softening. *J Biomech*  
1058 41(2):447–453
- Volokh KY (2011) Modeling failure of soft anisotropic materials with  
1059 application to arteries. *J Mech Behav Biomed Mater* 4(8):1582–  
1060 1594
- Yang J, Clark JW Jr, Bryan RM, Robertson C (2003) The myogenic  
1061 response in isolated rat cerebrovascular arteries: smooth muscle  
1062 cell model. *Med Eng Phys* 25(8):691–709
- Zulliger MA, Rachev A, Stergiopoulos N (2004) A constitutive formula-  
1063 tion of arterial mechanics including vascular smooth muscle tone.  
1064 *Am J Physiol Heart Circ Physiol* 287(3):H1335–H1343