

The F -measure for Research Priority

Ronald Rousseau[†]

University of Antwerp, Faculty of Social Sciences, B-2020 Antwerp, Belgium & KU Leuven,
Facultair Onderzoekscentrum ECOOM, Naamsestraat 61, Leuven B-3000, Belgium

Abstract

Purpose: In this contribution we continue our investigations related to the activity index (AI) and its formal analogs. We try to replace the AI by an indicator which is better suited for policy applications.

Design/methodology/approach: We point out that fluctuations in the value of the AI for a given country and domain are never the result of that country's policy with respect to that domain alone because there are exogenous factors at play. For this reason we introduce the F -measure. This F -measure is nothing but the harmonic mean of the country's share in the world's publication output in the given domain and the given domain's share in the country's publication output.

Findings: The F -measure does not suffer from the problems the AI does.

Research limitations: The indicator is not yet fully tested in real cases.

R&D policy management: In policy considerations, the AI should better be replaced by the F -measure as this measure can better show the results of science policy measures (which the AI cannot as it depends on exogenous factors).

Originality/value: We provide an original solution for a problem that is not fully realized by policy makers.

Keywords Activity index; Harmonic mean; F -measure; Research policy; Endogenous and exogenous factors

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1 Introduction

In this contribution we continue our investigations (Rousseau & Yang, 2012) related to the activity index (AI) and its formal analogs. The activity index (AI) of country C with respect to a given domain D (and with respect to the world, W) over a given period P is defined as:



[†] Corresponding author: Ronald Rousseau (E-mail: ronald.rousseau@uantwerpen.be; ronald.rousseau@kuleuven.be).

$AI(C, D, W, P)$ = the country's share in the world's publication output during the period P in the given domain D divided by the country's share in the world's publication output during the same period P in all science domains.

(1)

We note, moreover, that publications are counted as retrieved in a given database. This index was introduced in informetrics by Frame (1977). We refer to this formulation as the basic activity index because, instead of the world one might, for instance consider the USA or China and instead of a country one may consider a state or province. Clearly many other variants are imaginable. The basic activity index is said to characterize the relative research effort a country devotes to a given domain D . Stated otherwise, the AI gauges the share of a country's or region's publication activity in a given domain in its total publication output against the corresponding world standard. The lower bound of the AI is zero, while it has no upper bound. It is easy to show, see Equation (3) and i.e., (Schubert & Braun, 1986) that the activity index can also be expressed as:

$AI(C, D, W, P)$ = the given domain's share in the country's publication output during the period P divided by the given domain's share in the world's publication output during the same period P .

(2)

When the context is clear or when it does not matter we simply write AI . The mathematical framework of the AI , though with other meanings and sometimes slightly transformed, has been used in many contexts and with other names. In all cases one studies a nominal cross-classification table. Some of these, such as the attractivity index (replacing the term publication output by received citations in Equation (1), the relative specialization index and the (relative) priority index, are discussed further on.

The AI and the attractivity index are classified by Vinkler (2010) among the contribution indicators, used to characterize the contribution or weight of a subsystem, such as a country, to the total system, e.g., the world.

Next we have a look at the constituent parts of the AI and introduce some notations. For simplicity we stay within the context of Equations (1) and (2) but recall that everything we show in the context of the basic activity index can also be said in other contexts. Criticisms we exert refer to the meaning of the mathematical formula: a ratio of ratios, but to make things precise we work mostly in the context of the standard activity index.

We consider the following parameters: O_{CD} , O_D , O_C and O_W , where, as a memory aid, the symbol O refers to the word output. Further:



- O_{CD} denotes the number of publications by country C in domain D during a given publication window;
- O_D denotes the total number of publications in the world in domain D during the same publication window;
- O_C denotes the number of publications – in all domains – by country C during the same publication window;
- O_W denotes the total number of publications in the world and in all domains during this publication window.

Then clearly, we have the following relations:

- $0 \leq O_{CD} \leq O_D \leq O_W$; $0 \leq O_{CD} \leq O_C \leq O_W$; and further:
- O_{CD}/O_D is: the country's share in the world's publication output in the given domain D
- O_{CD}/O_C is: the given domain's share in the country's publication output
- O_C/O_W is: the country's share in the world's publication output in all science domains
- O_D/O_W is: the given domain's share in the world's publication output

Finally we note that

$$AI = \frac{\left(\frac{O_{CD}}{O_D}\right)}{\left(\frac{O_C}{O_W}\right)} = \frac{\left(\frac{O_{CD}}{O_C}\right)}{\left(\frac{O_D}{O_W}\right)}. \quad (3)$$

It is well-known that, assuming disjoint domains, a country cannot have an $AI(D)$ value larger than one for all domains D (Rousseau, 2012).

2 A Short Literature Study

In this section we recall some articles that used or studied the activity index, the attractivity index or its variants, without trying to be exhaustive.

Thijs and Glänzel (2008) used the AI to describe the national profile of eight European countries' research fields. Zhou, Thijs, and Glänzel (2009) studied the regions of China, including in their investigations the scientific production (where the AI plays a role), relative received citations (but they did not include the attractivity index), and regional R&D expenditure. Ramakrishnan and Thavamani (2015) used the basic activity index in a study of the contribution of India to the field of leptospirosis. Further, Sangam et al. (2017) show that the AI (they use the term relative priority index) depends on the used database. Concretely, they study hepatitis research and compare results obtained from data retrieved from PubMed, Web of Science (WoS), and a sub-database of the WoS consisting of fields in the life sciences.



Instead of the term *AI* Nagpaul and Sharma (1995) use the term (relative) priority index, but with the same meaning as the *AI*. This terminology has also been used by Bhattacharya (1997) and in the already mentioned publication by Sangam et al. (2017). The revealed comparative advantage (*RCA*) or Balassa Index (Balassa, 1965) is an index used in international economics for calculating the relative advantage or disadvantage of a certain country in a certain class of goods or services as evidenced by trade flows. The *RCA* is defined as the proportion of the country's exports that are of the class under consideration divided by the proportion of world exports that are of that class. Mathematically this index has the same form as the *AI*. A comparative advantage is "revealed" if $RCA > 1$. If *RCA* is less than unity, the country is said to have a comparative disadvantage in the commodity or industry under consideration.

Next we draw our attention to studies that include some theoretical aspects or variations of the *AI*. First we mention that some authors prefer the *AI* multiplied by 100 and refer to this as the modified activity index (*MAI*), see e.g., (Guan & Gao, 2008). These authors studied the *MAI* for bioinformatics over the period 2000–2005 and observe that the *MAI* value (hence also the *AI*-value) of China in this field has doubled over the observed period. Chen and Xiao (2016) proposed the Keyword Activity Index (*KAI*) of a keyword in a given domain as:

$KAI = (\text{the share of the given domain in publications containing the given keyword}) / (\text{the share of the given domain in all publications}).$

Egghe and Rousseau (2002) place the activity and the attractive index within a larger abstract framework of relative indicators. Hu and Rousseau (2009) compare the research performance in biomedical fields of 10 selected Western and Asian countries. The results confirm that there are many differences in intra- and interdisciplinary scientific activities between the West and the East. In particular they found that in most biomedical fields Asian countries perform below world average. Stimulated by these experimental results they find that the ratio of the attractivity index over the activity index, in a given domain and for a given country, can be expressed in terms of normalized mean citation rates (for the precise results we refer the reader to the original publication).

The relative specialization index (*RSI*) as used e.g., in Glänzel (2000) and Aksnes, van Leeuwen, and Sivertsen (2014) is defined as:

$$RSI = \frac{AI - 1}{AI + 1}. \quad (4)$$

The *RSI* is a strict order preserving normalization of the *AI*. If $AI = 0$ then $RSI = -1$ and if *AI* increases to infinity, then *RSI* tends to 1. This transformation makes



sure that values stay bounded between -1 and +1. This indicator but with Chinese universities instead of countries was used in Li, Miao, and Ding (2015). Besides comparisons with the world, they also performed comparisons with respect to China and with respect to leading universities in the world as reference group. Aksnes, van Leeuwen, and Sivertsen (2014) studied the impact on the *RSI* of the increased representation of China in the WoS. They choose the Netherlands as a case study to study this effect. We note that here two dynamic aspects are at play: the huge growth of China in terms of publications (described as “booming”) and the change of the WoS over time (possibly influenced by China). They concluded however that, although the influence of China is visible in the *RSI* for the Netherlands, and this especially in the last decade and in domains where these countries have opposite specializations, the basic research profile of the Netherlands as measured by the *RSI* remains the same. We note though that this is not a strictly mathematical result but rather a heuristic impression related to the stability of this index. Zhang, Rousseau, and Glänzel (2011) applied the *RSI* formula using document types instead of scientific domains. They find that the USA, Canada, and Australia are balanced cases, while the UK has the highest relative contribution in book reviews.

Stare and Kejžar (2014) point out that although +1 is indeed an upper bound for the *RSI*, this upper bound depends on the domain under study and as such can in practice be much lower than +1 (for a given domain). They show that for the period 2005–2009 and for the *Natural Sciences*, this upper bound is as low as 0.32. They conclude that the differences in maximum values of *AI* and *RSI* between scientific fields are so big that any conclusions based on analyses of these indices seem questionable. For this reason they propose another index which takes the maximum value of the *AI* for a given domain into account. This indicator, denoted as *SAI* (standardized *AI*) is defined as follows:

$$SAI = \begin{cases} \frac{AI}{2} & \text{if } AI \leq 1 \\ 1 - \frac{MAX(AI) - AI}{2(MAX(AI) - 1)} & \text{otherwise} \end{cases} \quad (5)$$

Here, $MAX(AI)$ is the theoretical maximum value of *AI*, given the real number of publications in the domain. Clearly, *SAI* takes values between 0 and 1 and when $AI = 1$, then $SAI = 0.5$.

3 Reflections on the Meaning of the Activity Index

What is the meaning of the activity index? In (Rousseau, 2012) we stated that if the values of O_{CD} , O_D , and O_C stay the same—and these are the parameters we are



interested in—then $AI(Y+1)$ may differ from $AI(Y)$, the values of the activity index in the years $Y+1$ and Y , if there is an increase or decrease in O_W , unrelated to country C or domain D . Concretely, the activity index of the USA in chemistry may increase just because China, or any other country, has an increase in articles on biology (leading to an increase in O_W). Hence a change (increase or decrease) in the activity index can happen for reasons which have nothing to do with the country or the domain one is interested in. This observation is important for policy reasons as fluctuations in the value of the AI for a given country and domain is never the result of that country's policy with respect to the domain D alone. For this reason we consider O_{CD} , O_C , and O_D as endogenous factors (the factors of interest), while O_W is considered an uncontrollable external, i.e., exogenous factor.

Because of these remarks strange, i.e., counterintuitive, results may occur when calculating an AI . We provide two examples.

Example A. Suppose that a country is the leading country in the world, according to the activity index, in a particular domain. Then it is possible that another country becomes the leading one by publishing less in other domains. Consider the following Table 1. At the start the activity indices for countries 1 and 2 are respectively 5.33 and 4.48. When country 2 publishes 17,000 articles less in other domains the activity indices become respectively 5.28 and 5.34. Although this is a fictitious case, it clearly demonstrates the fact that this indicator does not behave as intuitively expected, and worse it does not measure what it (probably) is supposed to measure. The problem lies in the parameter O_W .

Table 1. Calculations related to Example A; the indicator F is introduced further on.

| | Original situation | | New situation: Country 2 publishes 17,000 articles less in other domains | |
|----------|--------------------|-----------|--|-----------|
| | Country 1 | Country 2 | Country 1 | Country 2 |
| O_{CD} | 200 | 1,400 | 200 | 1,400 |
| O_D | 5,000 | 5,000 | 5,000 | 5,000 |
| O_C | 12,000 | 100,000 | 12,000 | 83,000 |
| O_W | 1,600,000 | 1,600,000 | 1,583,000 | 1,583,000 |
| AI | 5.33 | 4.48 | 5.28 | 5.34 |
| F | 0.0235 | 0.0267 | 0.0235 | 0.0318 |

Example B. Next we provide another counterintuitive example which comes from (Rousseau & Yang, 2012). This example is even more counterintuitive as there are no pure exogenous influences. It shows that if a country's activity in a domain (parameter O_{CD}) increases and nothing else changes (the changes in the domain, country and world, are only the result of the change introduced by the country and the domain under study), then it is possible that the AI decreases and similarly if the activity decreases it is possible that the AI increases. Of course this again is a



purely theoretic example, but it clearly shows the intrinsic problem with the *AI*-formula. Data and results are shown in Table 2.

Table 2. Data and calculations related to Example B.

| | Basic | Increase in O_{CD} | Decrease in O_{CD} |
|-----------|-------|----------------------|----------------------|
| O_{CD} | 190 | 200 | 180 |
| O_D | 200 | 210 | 190 |
| O_C | 200 | 210 | 190 |
| O_W | 400 | 410 | 390 |
| <i>AI</i> | 1.9 | 1.859 | 1.945 |
| <i>F</i> | 0.95 | 0.9524 | 0.9474 |

These two examples clearly show that there are serious problems in the interpretation of the *AI*. Finally, we mention the following situation. Consider O_{CD} , O_C , O_D , and O_W in a particular year. The next year O_{CD} , O_C , and O_D are exactly the same, but O_W has increased. Comparing the *AI* for these two years we see that the numerator has stayed the same but the denominator has decreased. Consequently the *AI*-value has increased. Reflecting on this we see that, with respect to the world, the contribution of country *C* and of the domain *D* have decreased. Yet, according to the *AI*, the activity of *C* in *D* has increased! Also this result is difficult to grasp.

4 A New Proposal: *F*-measure for Research Priority

Although the *AI* and its variants do have a meaning as relative (or even double relative) measures (Rousseau, 2012) we think that in many cases researchers are actually interested in another indicator.

The ratios O_{CD}/O_D , namely the country's share in the world's publication output in the given domain *D* and O_{CD}/O_C , namely the given domain's share in the country's publication output are the indicators in which one generally is interested. Working with O_{CD}/O_D and O_{CD}/O_C we form their harmonic means, which conceptually is the same as the *F*-score with respect to Recall and Precision in information retrieval (Manning, Raghavan, & Schütze, 2008). This leads to the indicator, see (6), we propose instead of the activity index and its variants.

$$F(C, D, W, P) = \frac{2}{\frac{1}{O_{CD}/O_D} + \frac{1}{O_{CD}/O_C}} = \frac{2}{\frac{O_D}{O_{CD}} + \frac{O_C}{O_{CD}}} = \frac{2O_{CD}}{O_D + O_C} \leq 1. \quad (6)$$

We further write $F(C, D, W, P)$ simply as *F* when *C*, *D*, *W* and *P* are assumed to be known. We already note that

$$0 \leq F \leq 1,$$



where the minimum and the maximum value only occur in the uninteresting cases that $O_{CD} = 0$, i.e., the country has no contribution in that particular domain or when the country is the only one active in that particular domain and is, moreover, only active in that domain: $O_{CD} = O_D = O_C$. So, from now on we assume the strict inequalities in (7). Being a mean we have for each concrete case that

$$\min\left(\frac{O_{CD}}{O_C}, \frac{O_{CD}}{O_D}\right) \leq F \leq \max\left(\frac{O_{CD}}{O_C}, \frac{O_{CD}}{O_D}\right). \quad (8)$$

The value of the F -measure in a domain D for the whole world is $\frac{2O_D}{O_D + O_W}$. The larger O_D the larger this world value. Of course one could divide the value for a country in a domain with the corresponding value for the world, but this would re-introduce the parameter O_W . For this reason we prefer to consider the world value as a separate piece of information about the priority given by the whole world to this particular domain. We note that a special application of the F -score, the so-called feature F -measure was used by Lamirel (2012) as an element in an unsupervised clustering method.

In (Rousseau & Yang, 2012) we investigated under which conditions an increase in O_{CD} (or a decrease) would lead to an increase (decrease) in AI . Recall that we already know that this—expected—behavior does not always happen. Yet, we think that such an increase or decrease should not depend on other variables but should always happen. The next result shows that this is the case for the F -measure for research priority. Here and further on we exclude the trivial case that $O_{CD} = O_D = O_C$.

Theorem 1.

- 1) If O_{CD} increases then the F -measure increases (addition property).
- 2) If O_{CD} decreases then the F -measure decreases (subtraction property).

Proof.

- 1) Let $\lambda > 0$ then we have to show that

$$\begin{aligned} \frac{2O_{CD}}{O_D + O_C} &< \frac{2(O_{CD} + \lambda)}{(O_D + \lambda) + (O_C + \lambda)} \\ \Leftrightarrow 2O_{CD} \cdot O_D + 2O_{CD} \cdot O_C + 4O_{CD} \cdot \lambda &< 2O_{CD} \cdot O_D + 2O_{CD} \cdot O_C + 2\lambda \cdot O_D + 2\lambda \cdot O_C \\ \Leftrightarrow 2O_{CD} &< O_D + O_C \end{aligned}$$

This last inequality obviously holds.



2) Similarly, for $O_{CD} > \lambda > 0$, we show that:

$$\begin{aligned} \frac{2O_{CD}}{O_D + O_C} &> \frac{2(O_{CD} - \lambda)}{(O_D - \lambda) + (O_C - \lambda)} \\ \Leftrightarrow 2O_{CD} \cdot O_D + 2O_{CD} \cdot O_C - 4O_{CD} \cdot \lambda &> 2O_{CD} \cdot O_D + 2O_{CD} \cdot O_C - 2\lambda \cdot O_D - 2\lambda \cdot O_C \\ \Leftrightarrow -2O_{CD} \cdot \lambda &> -\lambda(O_D + O_C) \\ \Leftrightarrow 2O_{CD} &< O_D + O_C \end{aligned}$$

Proving the case of a decrease in O_{CD} .

We further note the logical property that if O_D and/or O_C increases and O_{CD} stays the same then F decreases.

Reconsidering Examples A and B we calculate the F -measure in these cases and notice that for Example A country C_2 has already a higher F -measure than country C_1 ; while for Example B, all counterintuitive results disappear (illustrating Theorem 1). Next we briefly discuss the notion of independence (Bouyssou & Marchant, 2011) in relation with the F -measure.

If S_1 and S_2 represent sets of publications then strict independence for an indicator J means that if $J(S_1) < J(S_2)$ and one adds to S_1 and to S_2 the same publications, leading to sets S_1' and S_2' then still $J(S_1') < J(S_2')$.

The indicator J is said to be relative independent if the independence property holds for sets S_1 and S_2 with the same number of elements. If one wants to stress the difference between independent and relative independent one may use the term absolute independent for the former.

Theorem 2 (Relative independence)

If countries C_1 and C_2 have the same number of publications, i.e., $O_{C_1} = O_{C_2} = O_C$, if the relation $F(C_1, D, W, P) < F(C_2, D, W, P)$ holds and if we add the same number of publications, $q > 0$, in the domain D , to the output of these two countries then still $F(C'_1, D, W, P) < F(C'_2, D, W, P)$ where the notations C'_1 and C'_2 refer to the same countries but with an increased number of publications in the field F .

Proof. We know that

$$\frac{2O_{CD,1}}{O_D + O_C} < \frac{2O_{CD,2}}{O_D + O_C}$$

Hence $O_{CD,1} < O_{CD,2}$. Now we have to show that:

$$\frac{2(O_{CD,1} + q)}{(O_D + 2q) + (O_C + q)} < \frac{2(O_{CD,2} + q)}{(O_D + 2q) + (O_C + q)}$$

This is obvious as $O_{CD,1} < O_{CD,2}$.



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Note. The F -measure is not an absolute independent indicator. Indeed, consider the following example. Let $O_{CD,1} = 2$; $O_{CD,2} = 3$; $O_D = 88$; $O_{C,1} = 49$ and $O_{C,2} = 99$. Then

$$F_1 = \frac{2.2}{88 + 49} \approx 0.029 < F_2 = \frac{2.3}{88 + 99} \approx 0.032.$$

If we add now one unit to $O_{CD,1}$ and $O_{CD,2}$ then we obtain the following values for the parameters: $O_{CD,1} = 3$; $O_{CD,2} = 4$; $O_D = 90$; $O_{C,1} = 50$ and $O_{C,2} = 100$. The relation between the new F -values, denoted as F_1' and F_2' , now becomes:

$$F_1' = \frac{2.3}{90 + 50} \approx 0.0429 > F_2' = \frac{2.4}{90 + 100} \approx 0.0421.$$

This shows that the F -measure for research priority is not an absolute independent measure.

If the domain stays fixed a ranking of countries (C_1 and C_2) according to AI and to the F -measure may yield opposite results. Consider, indeed, the following example: let $O_{CD,1} = 4$; $O_D = 20$; $O_{C,1} = 14$; $O_{CD,2} = 3$ and $O_{C,2} = 10$, where subscripts refer to the corresponding countries, then $AI_1 = 4 O_W/280$ and $AI_2 = 3 O_W/200$ and hence $AI_1 < AI_2$. Yet $F_1 = 8/34 > F_2 = 6/30$.

Similarly, if the country is fixed then a ranking of domains according to AI and to the F -measure may yield opposite results. This remark is nothing but a confirmation that AI and F measure different properties. Only the second one is determined by endogenous factors and hence can be the direct result of an appropriate policy.

5 Further Mathematical Results

Next we answer the question: if O_{CD} increases with a given percentage p , what is its influence on the other parameters?

We first consider the parameter O_{CD}/O_D : the country's share in the world's publication output in the given domain D .

Proposition 1. Let $0 < p < 1$ then an increase of $100p\%$ in O_{CD} leads to an increase between 0 and $100p\%$ in O_{CD}/O_D . In many realistic cases, i.e., $O_{CD} \ll O_D$, this increase is close to $100p\%$.

Proof. If O_{CD} becomes $O_{CD} + O_{CD} \cdot p$, then O_{CD}/O_D becomes $(O_{CD} + O_{CD} \cdot p)/(O_D + O_{CD} \cdot p)$. Then:

$$\begin{aligned} \frac{O_{CD} + O_{CD} \cdot p}{O_D + O_{CD} \cdot p} &= \frac{O_D(1+p)}{O_D + O_{CD} \cdot p} = \frac{O_D + O_{CD} \cdot p}{O_D + O_{CD} \cdot p} + \frac{p(O_D - O_{CD})}{O_D + O_{CD} \cdot p} \\ &= \frac{O_{CD}}{O_D} + \frac{p(O_D - O_{CD})}{O_D + O_{CD} \cdot p} \\ &= 1 + p \frac{O_D - O_{CD}}{O_D + O_{CD} \cdot p} = 1 + p \frac{1 - \frac{O_{CD}}{O_D}}{1 + \frac{O_{CD} \cdot p}{O_D}} = 1 + p \cdot R \end{aligned}$$



The factor R is strictly positive and smaller than 1, proving this result. If O_{CD}/O_D is small then R is close to 1 and the increase in O_{CD}/O_D is close to p (but always strictly smaller).

This proposition also holds for O_{CD}/O_C .

As the *F*-measure is an average the proposition also holds here. For completeness sake we calculate the value of the corresponding R parameter:

$$\begin{aligned} & \frac{2O_{CD}(1+p)}{(O_D + O_{CD}\cdot p) + (O_C + O_{CD}\cdot p)} \\ & \frac{2O_{CD}}{O_D + O_C} \\ & = \frac{(1+p)(O_D + O_C)}{O_D + O_C + 2O_{CD}\cdot p} = \frac{O_D + O_C + 2O_{CD}\cdot p}{O_D + O_C + 2O_{CD}\cdot p} + \frac{p(O_D + O_C - 2O_{CD})}{O_D + O_C + 2O_{CD}\cdot p} \\ & = 1 + p \frac{O_D + O_C - 2O_{CD}}{O_D + O_C + 2O_{CD}\cdot p} = 1 + p \frac{1 - \frac{2O_{CD}}{O_D + O_C}}{1 + \frac{2O_{CD}\cdot p}{O_D + O_C}} \end{aligned}$$

The corresponding factor R is $\frac{1 - \frac{2O_{CD}}{O_D + O_C}}{1 + \frac{2O_{CD}\cdot p}{O_D + O_C}}$ which is again close to 1 if the

F-measure is small and close to zero if F is close to 1. For small values of the *F*-measure an increase of O_{CD} by $p100\%$ leads to an increase of the *F*-measure by almost $p100\%$.

The *F*-measure, considered a mathematical function, depends on two variables $x = O_{CD}/O_D$ (the country's share in the world's publication in domain D) and $y = O_{CD}/O_C$ (the domain's share in the country's publication output). As a function of x and y we have:

$$F(x, y) = \frac{2}{\frac{1}{x} + \frac{1}{y}} = \frac{2xy}{x + y} \quad (9)$$

defined for $x \geq 0$, $y \geq 0$ and $(x, y) \neq (0, 0)$. We already note that $F(x, x) = x$.

Considering the parallel lines $x + y = c$, with c a strictly positive constant, we see that for points (x, y) on this line $F(x, y) = \frac{2x(c-x)}{c}$. Hence when $x + y = c$, $F(x, y)$ has the form of a parabola, taking the value zero for $x = 0$ and $x = c$, i.e., $y = 0$. The top of such a parabola is obtained for $x = c/2 = y$, and takes the value $F(c/2, c/2) = c/2$. From this analysis it follows that when either x or y is close to zero also the



F -measure for research priority is small. Figure 1 shows the function $F(x,y)$ for x and y between 0 and 1. It also shows the F -values for points on $x + y = 0.5$ and on $x + y = 1$.

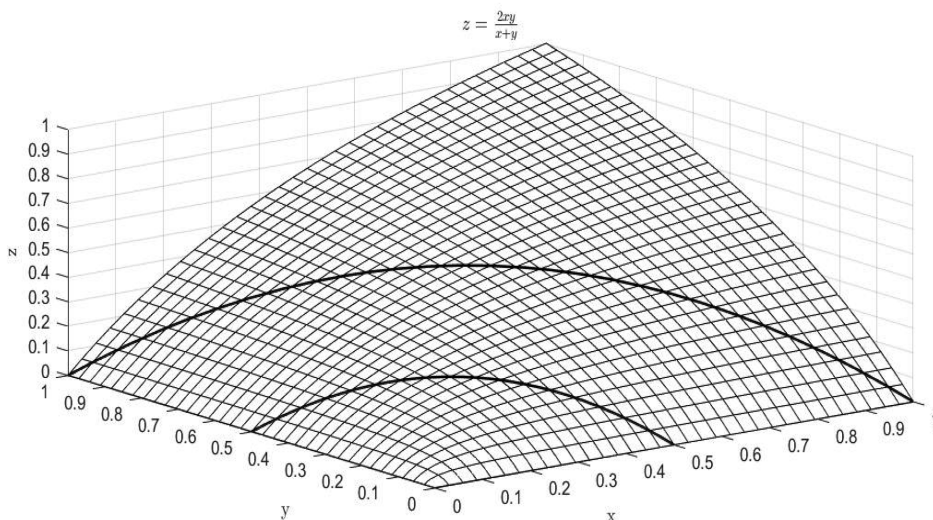


Figure 1. Graph of the function $F(x,y)$; origin is nearest to the viewer.

6 A Real-world Example

As a real-world application we consider a table of publications in the Humanities, containing information on publications by Flemish researchers (Engels, Ossenblok, & Spruyt, 2012). These data, published as part of Table 1 in (Engels, Ossenblok, & Spruyt, 2012), came about as follows: In 2008 the Flemish government provided the legal framework for the construction of the Flemish Academic Bibliographic Database for the Social Sciences and Humanities (“Vlaams Academisch Bibliografisch Bestand voor de Sociale en Humane Wetenschappen” or “VABB-SHW” in short). This database provided the Flemish government with a useful tool to fine-tune the distribution of research funding over universities in Flanders. As a consequence it became possible for researchers to analyze changing publication patterns in the larger Flemish peer reviewed literature (not just restricted to the WoS). Five publication types are included in the VABB-SHW:

- (a) articles in journals;
- (b) books as author;
- (c) books as editor;
- (d) articles or chapters in books;
- (e) proceedings papers that are not part of special issues of journals or edited books



In Table 3 a distinction is made between articles in journals included in the WoS and other ones, and similarly for proceedings papers, leading to seven types of publications. In the VABB-SHW all records are assigned to disciplines on the basis of the author(s) affiliation(s) with a SSH unit in which the author carries out research. For the Humanities one makes a distinction between the following disciplines: Archaeology; Art History (including Architecture and Arts); Communication Studies; History; Law; Linguistics; Literature; Philosophy (including History of Ideas); Theology (including Religious Studies). Finally, we mention that data in our Table 3 do not include the remainder category “Humanities-general.”

Table 3. Flemish Humanities publications (2000–2009) in the VABB.

| Disciplines | Journal articles | | Book chapters | Edited books | Monographs | Proceedings papers | | Row totals |
|-----------------------|------------------|----------|---------------|--------------|------------|--------------------|--------------|------------|
| | VABB-non-WoS | VABB-WoS | VABB | VABB | VABB | VABB-WoS | VABB-Non-WoS | |
| Archaeology | 176 | 133 | 40 | 6 | 11 | 12 | 18 | 396 |
| Art History | 295 | 150 | 135 | 38 | 12 | 22 | 28 | 680 |
| Communication Studies | 425 | 170 | 94 | 16 | 3 | 19 | 1 | 728 |
| History | 773 | 193 | 233 | 52 | 28 | 0 | 19 | 1,298 |
| Law | 4,018 | 144 | 320 | 89 | 55 | 11 | 20 | 4,657 |
| Linguistics | 908 | 457 | 511 | 135 | 59 | 54 | 83 | 2,207 |
| Literature | 631 | 143 | 376 | 87 | 36 | 0 | 31 | 1,304 |
| Philosophy | 786 | 603 | 279 | 42 | 30 | 36 | 9 | 1,785 |
| Theology | 610 | 85 | 410 | 85 | 53 | 1 | 4 | 1,248 |
| Column totals | 8,622 | 2,078 | 2,398 | 550 | 287 | 155 | 213 | 14,303 |

Next, in Table 4, we show *AI*-values for the data shown in Table 3. In this case *AI*-values refer to the relative preference of disciplines for certain publication types. Table 5 shows the corresponding *F*-values.

Table 4. Values according to the *AI*-formula for the data shown in Table 3.

| Disciplines | Journal articles | | Book chapters | Edited books | Monographs | Proceedings papers | |
|-----------------------|------------------|----------|---------------|--------------|------------|--------------------|--------------|
| | VABB-non-WoS | VABB-WoS | VABB | VABB | VABB | VABB-WoS | VABB-Non-WoS |
| Archaeology | 0.737 | 2.312 | 0.602 | 0.394 | 1.384 | 2.796 | 3.052 |
| Art History | 0.720 | 1.518 | 1.184 | 1.453 | 0.879 | 2.985 | 2.765 |
| Communication Studies | 0.968 | 1.607 | 0.770 | 0.572 | 0.205 | 2.408 | 0.092 |
| History | 0.988 | 1.023 | 1.071 | 1.042 | 1.075 | 0.000 | 0.983 |
| Law | 1.431 | 0.213 | 0.410 | 0.497 | 0.589 | 0.218 | 0.288 |
| Linguistics | 0.682 | 1.425 | 1.381 | 1.591 | 1.332 | 2.258 | 2.525 |
| Literature | 0.803 | 0.755 | 1.720 | 1.735 | 1.376 | 0.000 | 1.596 |
| Philosophy | 0.730 | 2.325 | 0.932 | 0.612 | 0.838 | 1.861 | 0.339 |
| Theology | 0.811 | 0.469 | 1.960 | 1.771 | 2.116 | 0.074 | 0.215 |



Table 5. Values according to the F -measure for the data shown in Table 3.

| Disciplines | Journal articles | | Book chapters | Edited books | Monographs | Proceedings papers | |
|-----------------------|------------------|----------|---------------|--------------|------------|--------------------|--------------|
| | VABB-non-WoS | VABB-WoS | VABB | VABB | VABB | VABB-WoS | VABB-Non-WoS |
| Archaeology | 0.039 | 0.108 | 0.029 | 0.013 | 0.032 | 0.044 | 0.059 |
| Art History | 0.063 | 0.109 | 0.088 | 0.062 | 0.025 | 0.053 | 0.063 |
| Communication Studies | 0.091 | 0.121 | 0.060 | 0.025 | 0.006 | 0.043 | 0.002 |
| History | 0.156 | 0.114 | 0.126 | 0.056 | 0.035 | 0.000 | 0.025 |
| Law | 0.605 | 0.043 | 0.091 | 0.034 | 0.022 | 0.005 | 0.008 |
| Linguistics | 0.168 | 0.213 | 0.222 | 0.098 | 0.047 | 0.046 | 0.069 |
| Literature | 0.127 | 0.085 | 0.203 | 0.094 | 0.045 | 0.000 | 0.041 |
| Philosophy | 0.151 | 0.312 | 0.133 | 0.036 | 0.029 | 0.037 | 0.009 |
| Theology | 0.124 | 0.051 | 0.225 | 0.095 | 0.069 | 0.001 | 0.005 |

Next we calculate the correlation for each type of publication (ranks for the calculation of the Spearman correlation go from 1 to 9 as there are 9 disciplines) between the numbers of publications, their AI -values and their F -values. Results are shown in Table 6.

Table 6. Correlation values.

| | Pearson | | | Spearman | | |
|---------------------------------|-----------|----------|------------|-----------|----------|------------|
| | PUB- AI | PUB- F | AI - F | PUB- AI | PUB- F | AI - F |
| Journal articles VABB-non-WoS | 0.873 | 0.998 | 0.872 | 0.183 | 0.983 | 0.267 |
| Journal articles VABB-WoS | 0.521 | 0.964 | 0.704 | 0.431 | 0.470 | 0.750 |
| Book chapters VABB | 0.599 | 0.922 | 0.852 | 0.633 | 0.933 | 0.783 |
| Edited books VABB | 0.621 | 0.789 | 0.965 | 0.500 | 0.683 | 0.933 |
| Monographs VABB | 0.461 | 0.645 | 0.961 | 0.233 | 0.533 | 0.867 |
| Proceedings papers VABB-WoS | 0.631 | 0.724 | 0.990 | 0.731 | 0.849 | 0.950 |
| Proceedings papers VABB-Non-WoS | 0.595 | 0.734 | 0.979 | 0.633 | 0.800 | 0.933 |

Note. PUB stands for number of publications

Generally, correlations between the numbers of publications and the AI -values are the lowest, while correlations for PUB- F and AI - F are roughly of the same level, the case of the Spearman rank-correlation between journal articles in non-WoS journals being an exception. The main lesson to be learned from this example is that numbers of published items per discipline per publication type, relative preference of disciplines for certain publication types (based on the AI -formula) and the corresponding F -measure are different, but to some extent correlated indicators.

7 Discussion and Conclusion

The criticism on the AI -formula (in general) is not always valid. If in the original table row or column sums are fixed, the criticism does not hold. This is clarified in the Appendix.



Any average, including weighted averages, of (O_{CD}/O_D) and (O_{CD}/O_C) satisfies the addition property (Theorem 1). Because of the formal analogy with the F -score from information retrieval and because it is generally agreed that when rates are involved one should use a harmonic mean, we choose this option. In this way we obtain the additional sensitivity benefit that if either O_{CD}/O_D (the country's share in the world's publication output in the given domain D) or O_{CD}/O_C (the given domain's share in the country's publication output) is small also the F -measure for research priority is small. This property does not hold for an arithmetic mean. If deemed necessary one may even consider weighted harmonic means of (O_{CD}/O_D) and (O_{CD}/O_C) . Another sensitivity aspect relates to the parameters O_D and O_C . If one studies a large domain such as the *Natural Sciences* or *Medicine* then the parameter O_D , being for most countries and certainly for most universities, much larger than the parameter O_C , has the largest influence on the actual value of F . On the other hand, if one studies a small specialty then the parameter O_C may have the biggest influence. However, we do not think that actual values of F are of importance but rather changes in value and resulting changes in rankings between comparable units.

Although the AI and its mathematical equivalents, such as the attractivity index, or their monotone transformations such as the relative specialization index, can be used to characterize the contribution or weight of a subsystem to the total system, they can certainly not be used for science policy purposes. The number of publications by country C in domain D during a given publication window (O_{CD}), the total number of publications in the world in domain D during the same publication window (O_D) and the number of publications—in all domains—by country C during the same publication window (O_C), can be considered as endogenous factors in a science policy model, while the total number of publications in the world and in all domains during this publication window (O_W) is an exogenous factor. For this reason we propose the F -measure as a better and more sensitive policy indicator.

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Appendix

The *AI*-formula can be calculated for any nominal cross-classification table. Focusing on one cell and using the earlier notation, this leads to Equation (10).

$$AI = \frac{O_{CD} * O_W}{O_C * O_D}. \quad (10)$$

One may observe that for the calculation of one specific *AI*-value the original table is reduced to a two by two table:

| | |
|---|--|
| Value for country <i>C</i> and domain <i>D</i> , denoted as $V_1 = O_{CD}$ | Value for country <i>C</i> and all domains except <i>D</i> , denoted as $V_2 = O_C - O_{CD}$ |
| Value for domain <i>D</i> and all countries except country <i>C</i> , denoted as $V_3 = O_D - O_{CD}$ | All values except country <i>C</i> and domain <i>D</i> , denoted as $V_4 = O_W - O_C - O_D + O_{CD}$ |

Using this reduction, Equation (10) can be rewritten using four values referring to non-overlapping sets:

$$AI = \frac{V_1 * (V_4 + V_2 + V_3 + V_1)}{(V_2 + V_1) * (V_3 + V_1)}. \quad (11)$$

If a cross-tabulation is such that row or column totals are fixed, then the examples showing the irrationality of the *AI*-index cannot be given. Indeed: when row or column totals are fixed, then what is added to one value (in one cell) must be deducted from another. In those cases the *AI*-formula has a clear meaning as a relative index and can be used in a rational analysis and for decision making.



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