



Unraveling interdiffusion effects at material interfaces –  
Learning from tensors and large-scale computer  
simulations

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March 9, 2017



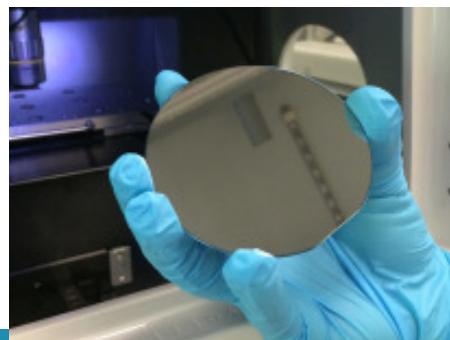
# The Periodic Table

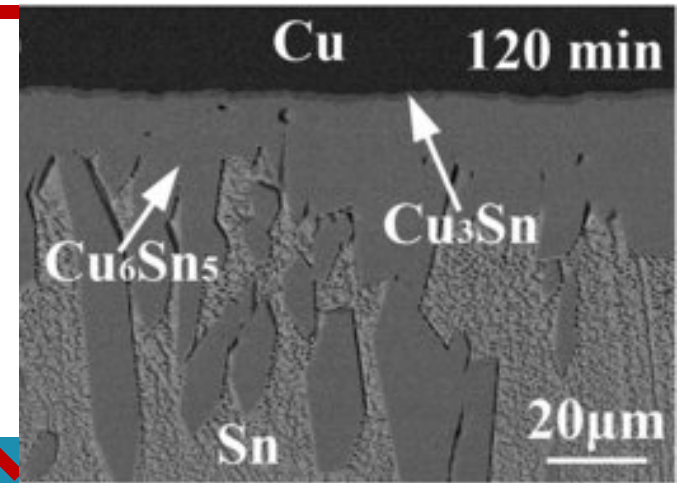
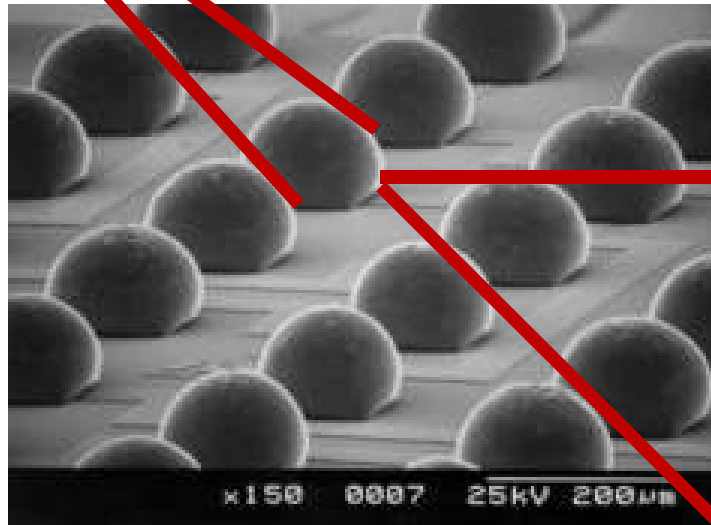
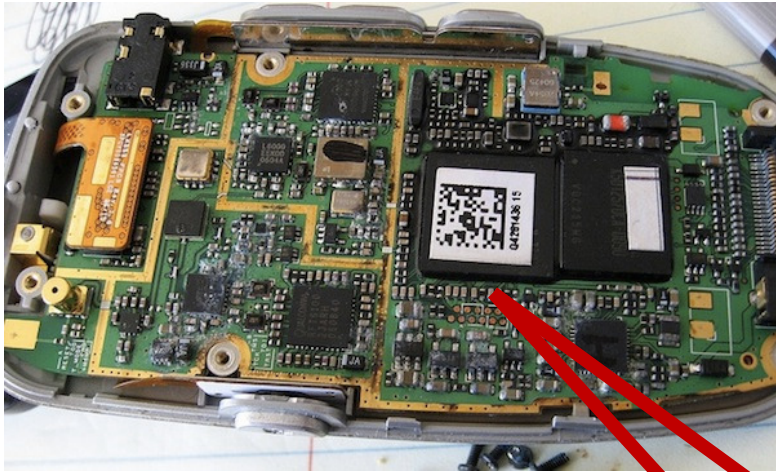


Info: [https://www.mtm.kuleuven.be/MTM Tabel van Mendeleev](https://www.mtm.kuleuven.be/MTM_Tabel_van_Mendeleev)  
Currently at Campus Library Arenberg

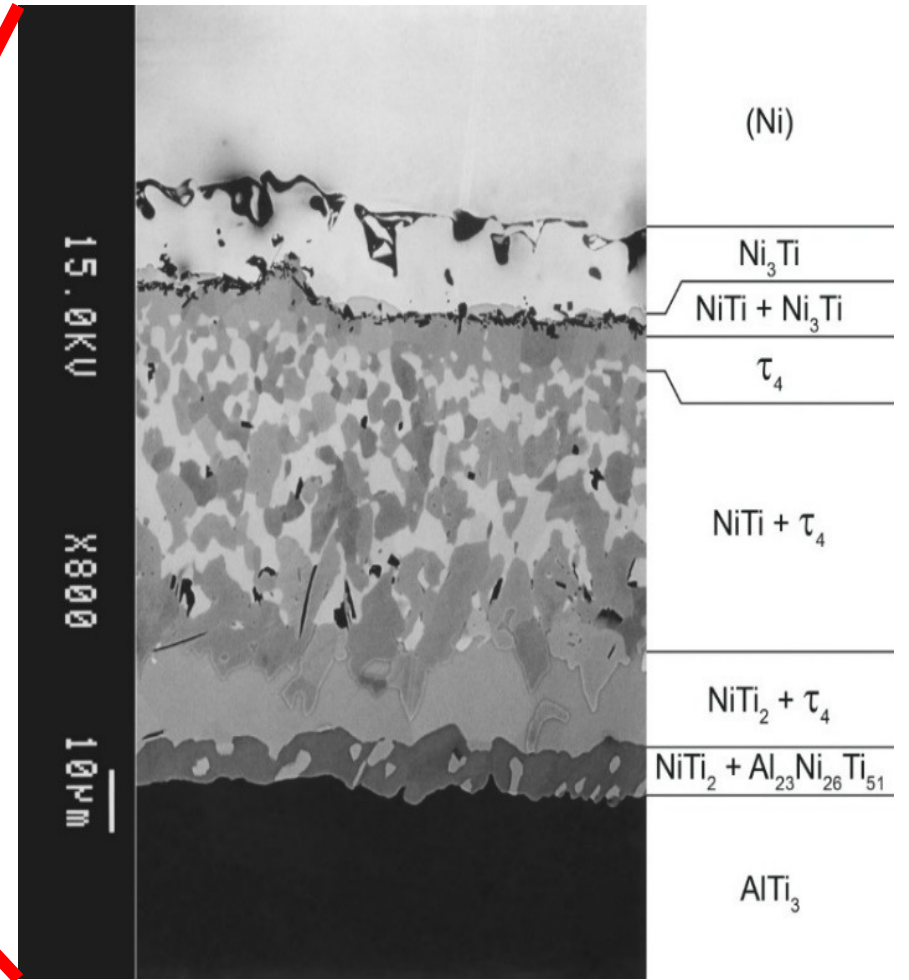
## More principle elements in new materials

- Super alloys
- Magnetic materials
- New solar cell materials
- High-entropy alloys
- ...

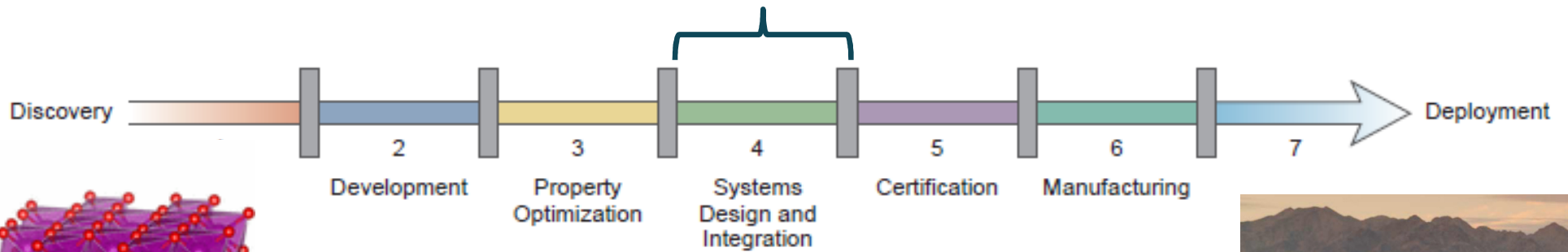






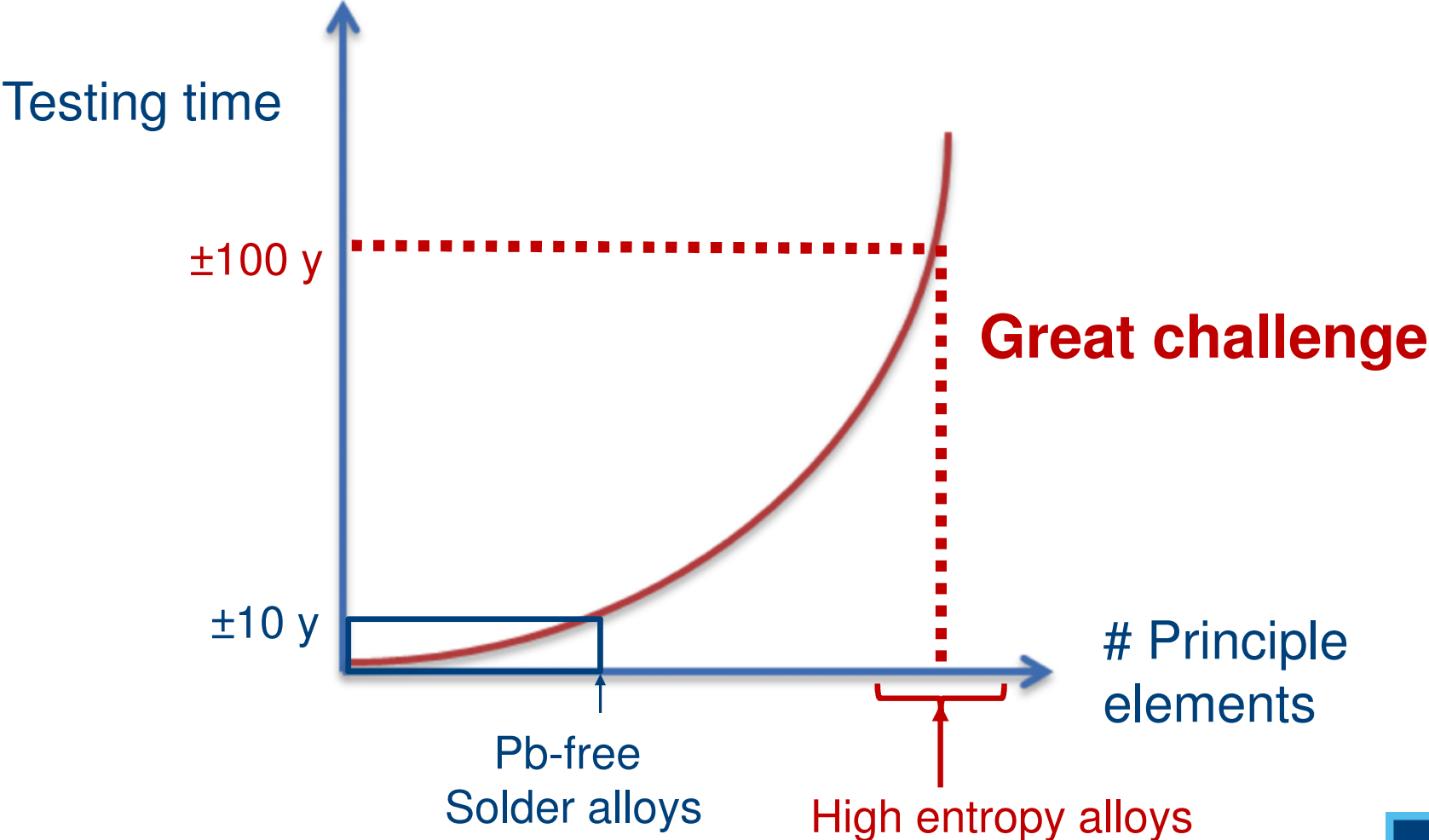


Long testing times  
high degree of trial-and-error

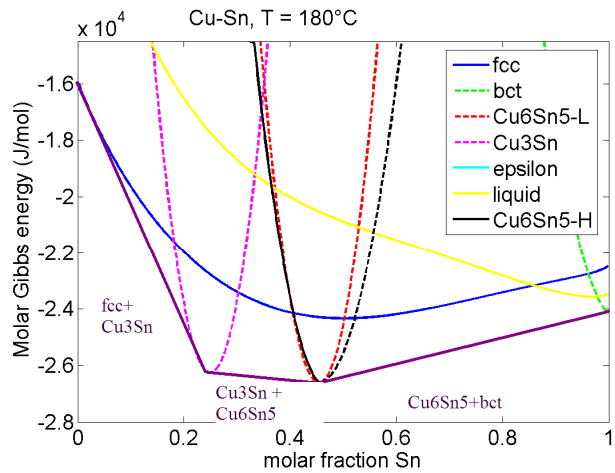


Numerous iterations

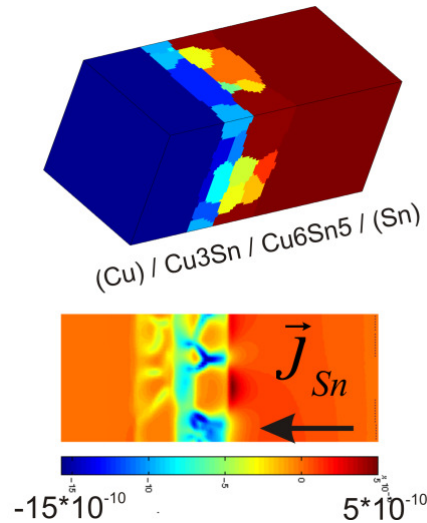




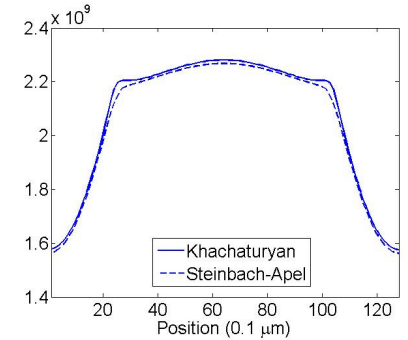
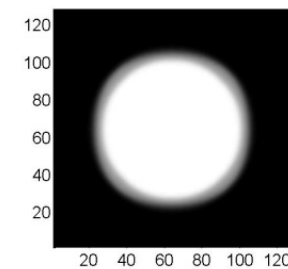
## Thermodynamic models/databases



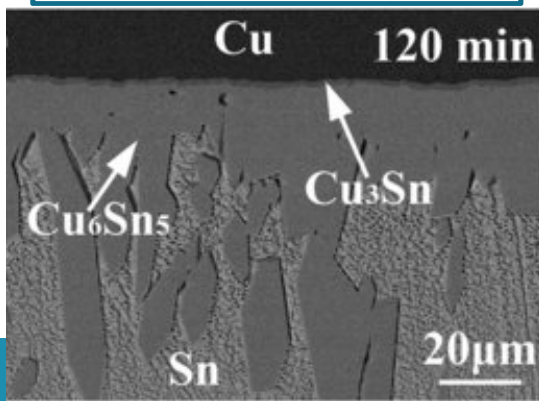
## Phase field simulations



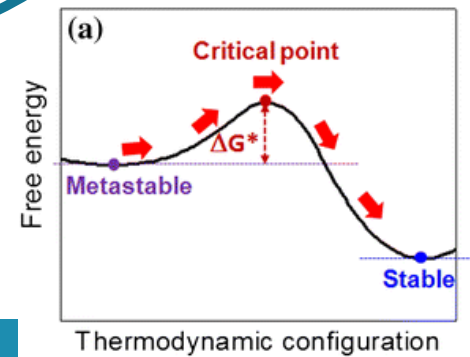
## Mechanical models



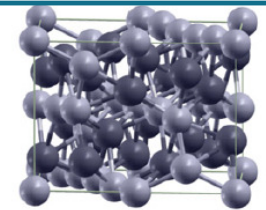
## Experiments



## Nucleation theory

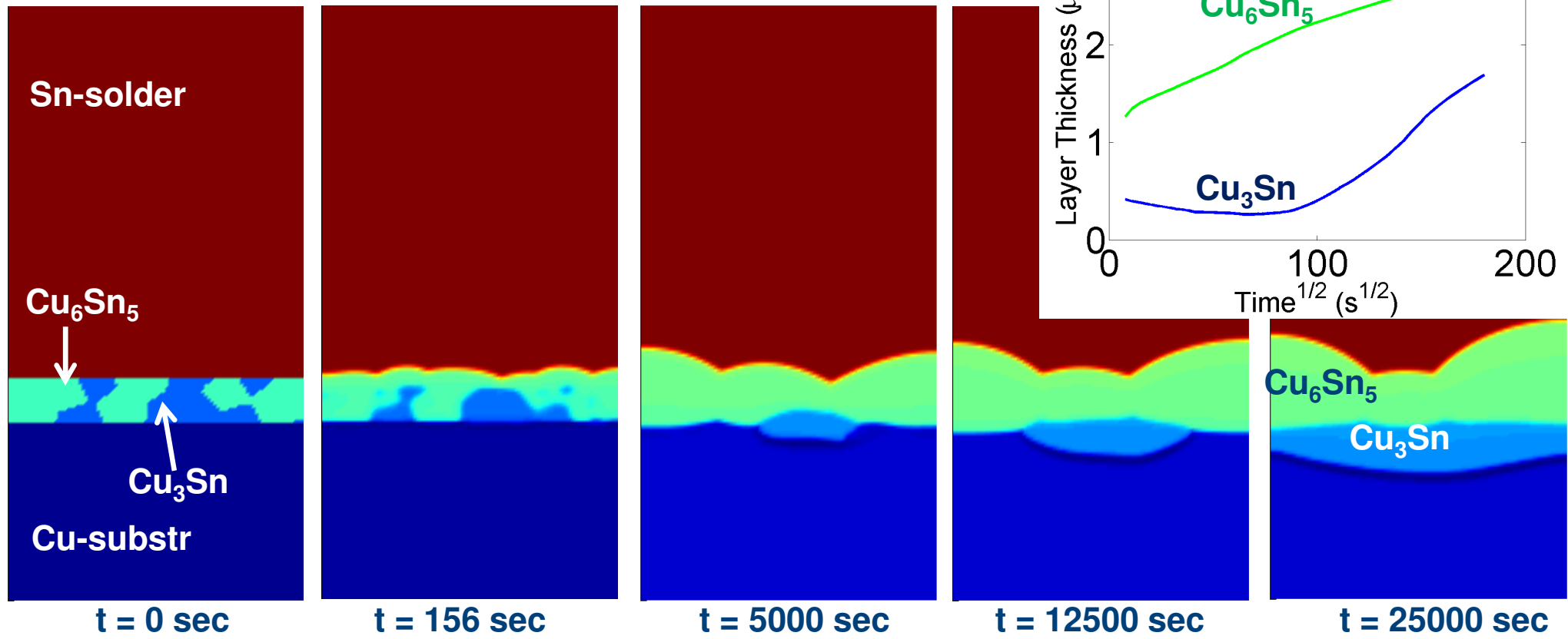


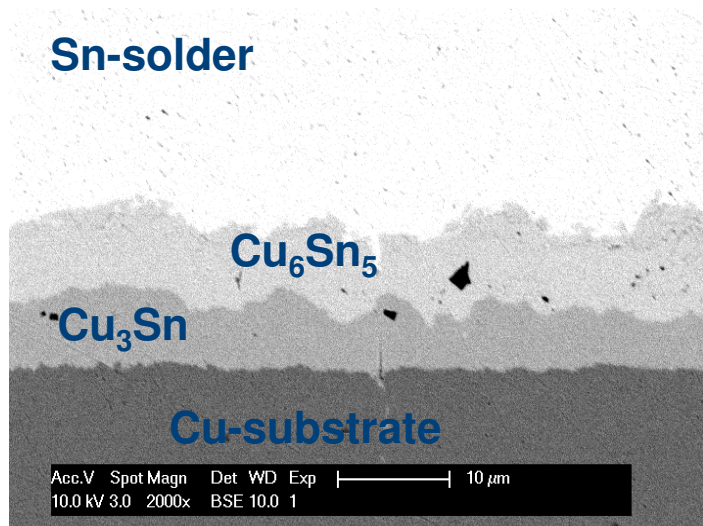
## Atomistic models



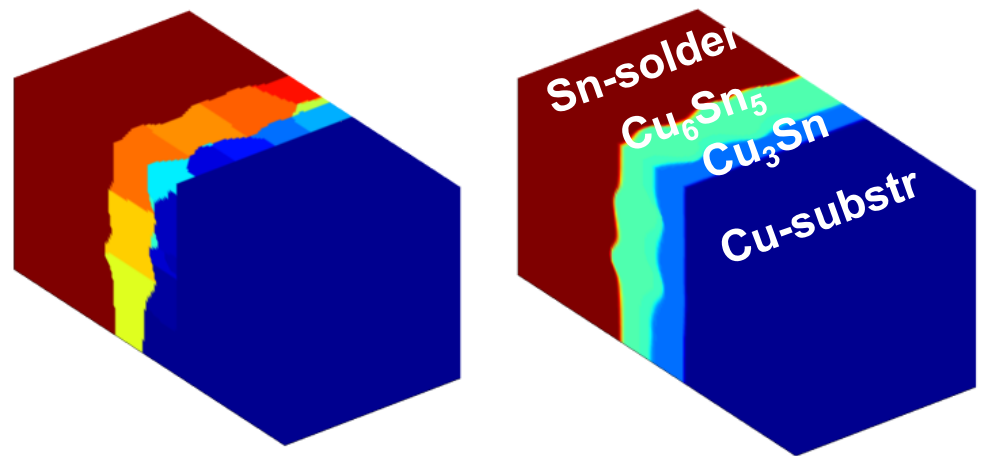
$\eta'$ -Cu6Sn5





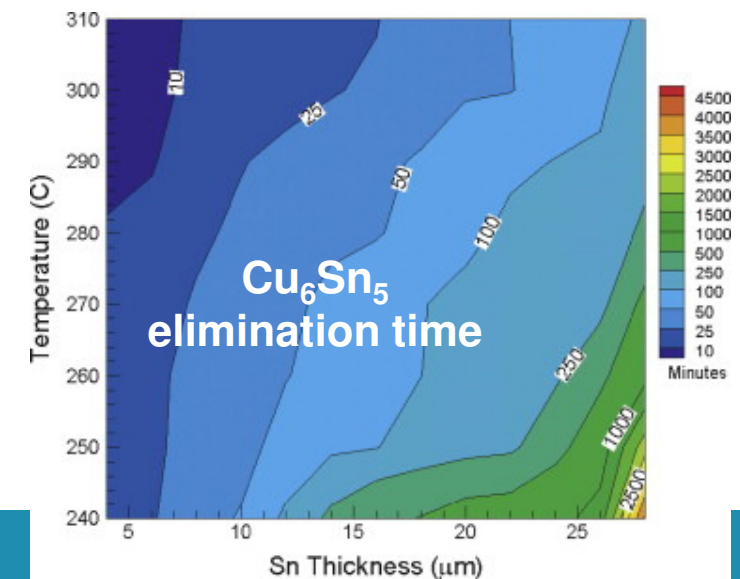
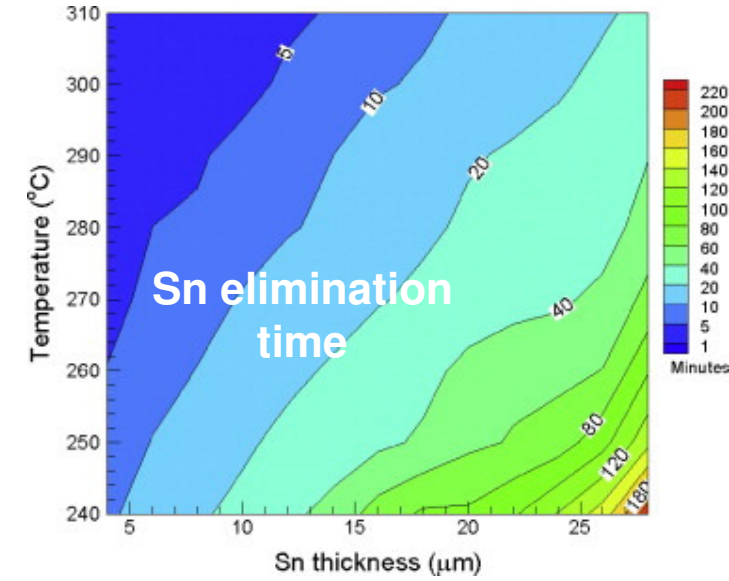
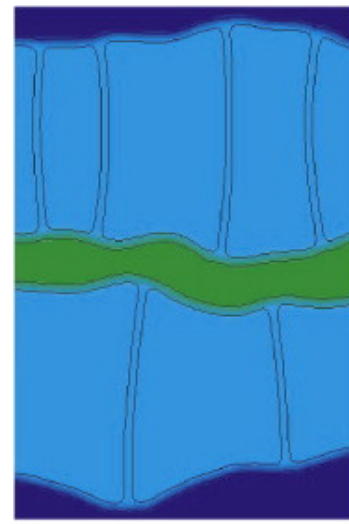
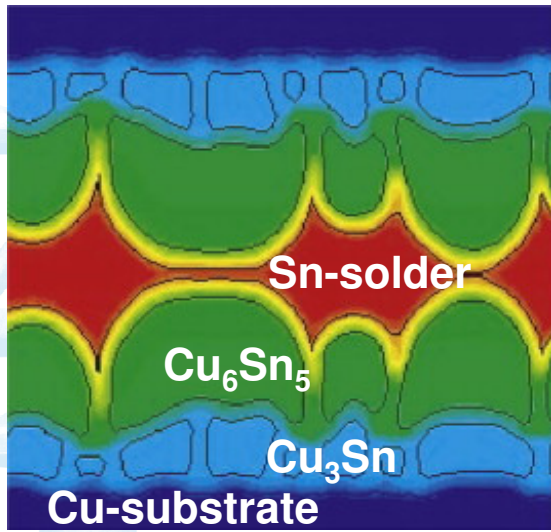
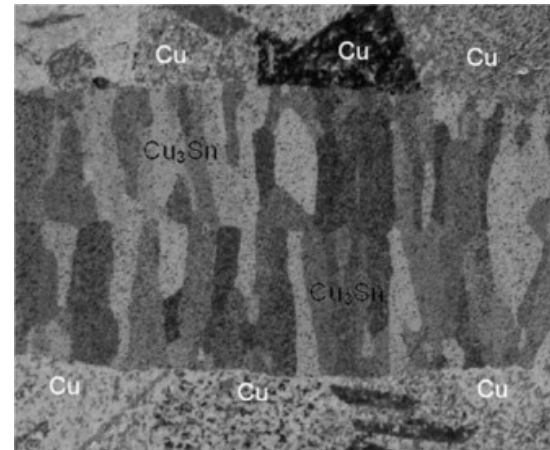


Solid state bonding at 170° C, 840 h



# Transient Liquid Phase bonding

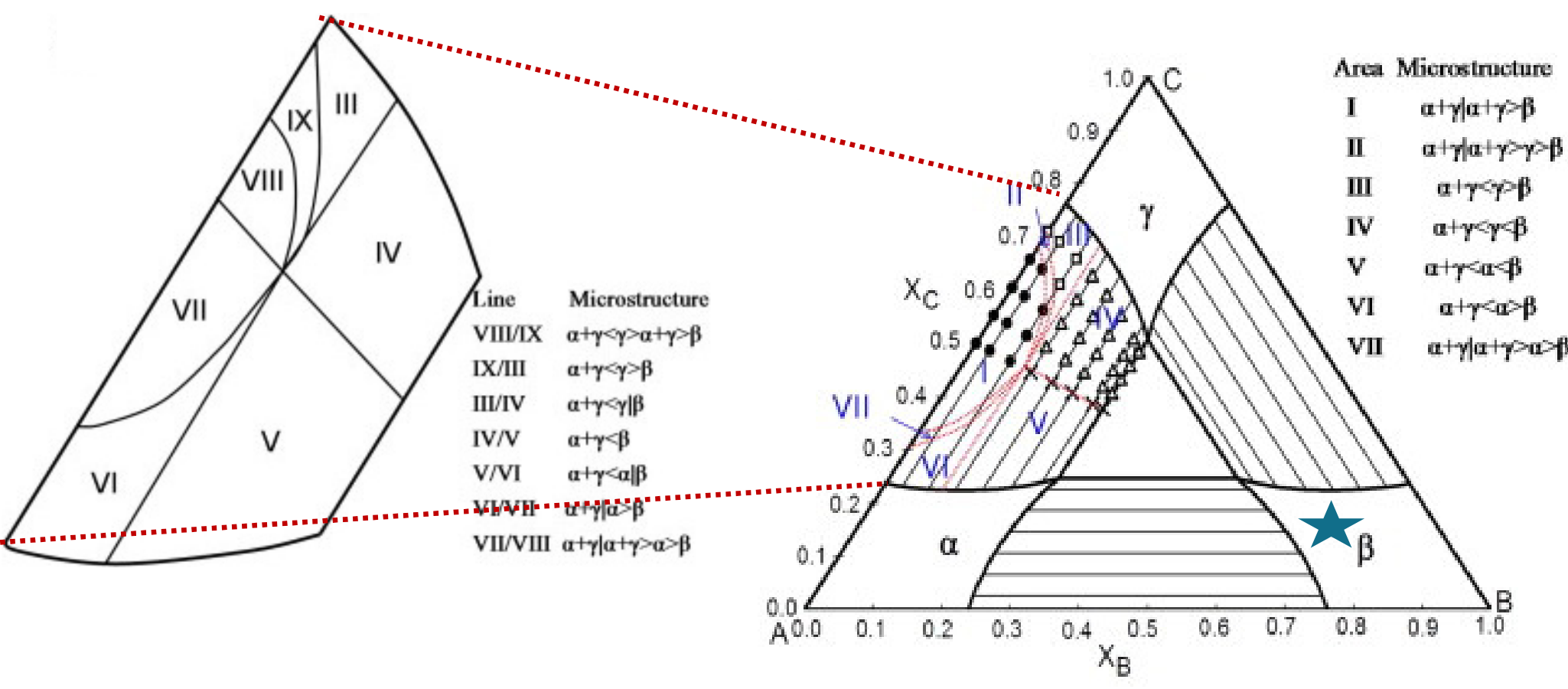
Cu / Sn-solder / Cu sandwich structure



**Slide 11**

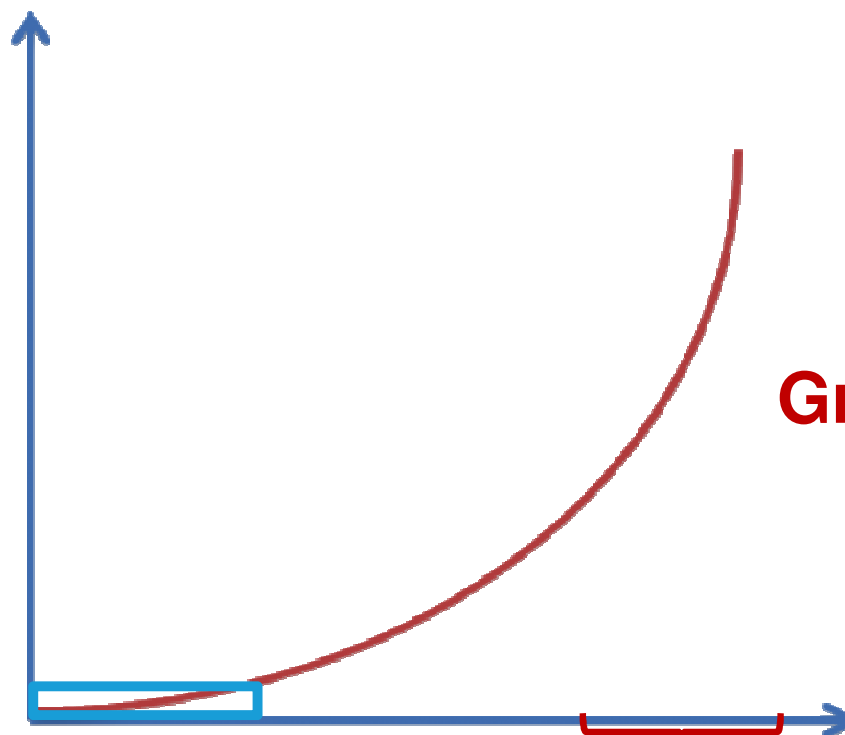
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**NM9**    reference toevoegen  
Nele Moelans; 6/03/2017





# Parameters  
# Simulations



2-3 elements

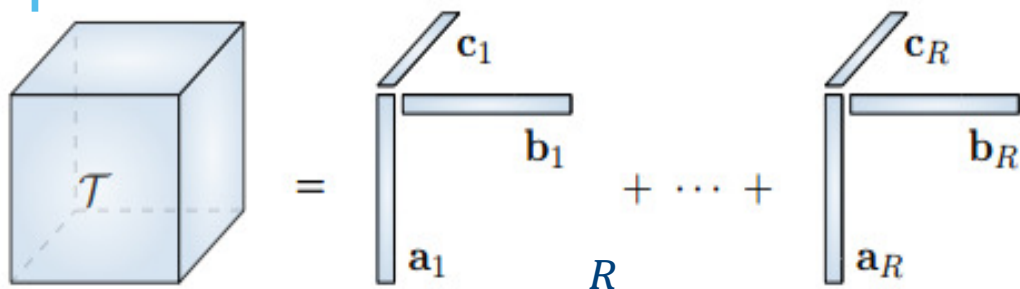
**Great challenge**

# Principle  
elements

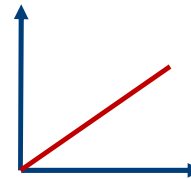
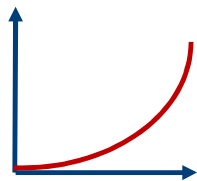
High entropy alloys

# Tensor decomposition

3D:


$$t_{ijk} = \sum_{r=1}^R a_{ir} b_{jr} c_{kr}$$

ND:  $I^3$  elements  $\rightarrow$   $3 \cdot I \cdot R$  data points  
 $I^N$  elements  $\rightarrow$   $N \cdot I \cdot R$  data points



# Thermodynamics Ag-Cu-Ni-Sn liquids

$$G(x_{Ag}, x_{Cu}, x_{Sn}, T) - G_{log} = \sum_{r=1}^4 a_{ir} b_{jr} c_{kr} d_{lr}$$

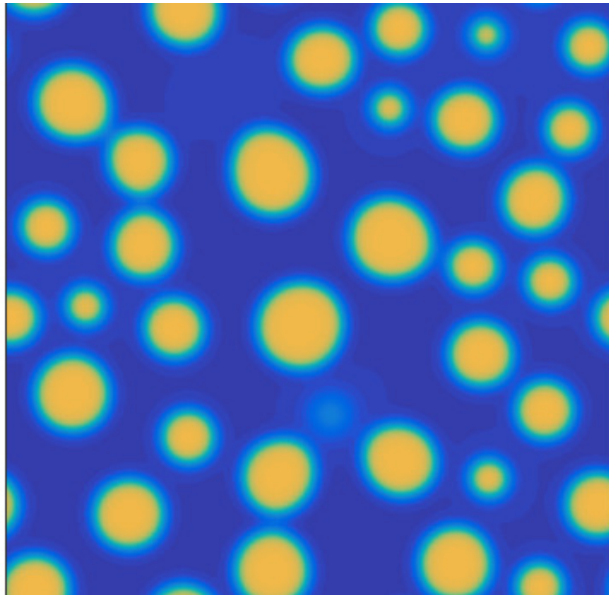
**8 e12 elements**

Error < 1%

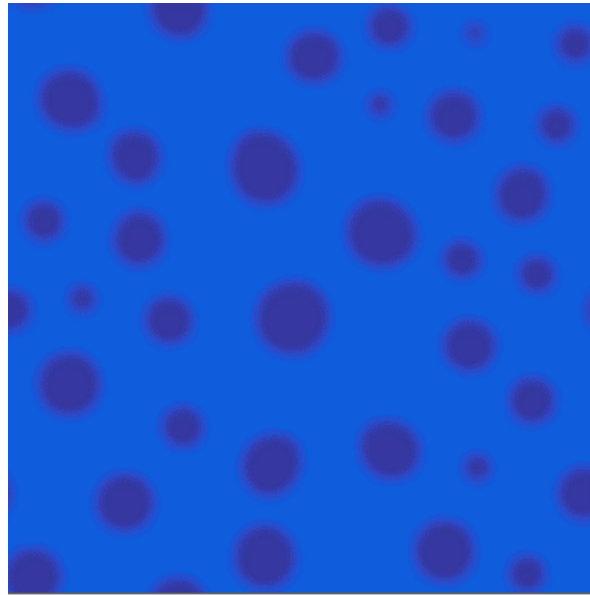
$$a = \begin{matrix} & \begin{matrix} 4 \\ \text{Ag} \end{matrix} \\ \begin{matrix} 10000 \\ \end{matrix} \end{matrix}, \quad b = \begin{matrix} & \begin{matrix} 4 \\ \text{Cu} \end{matrix} \\ \begin{matrix} 10000 \\ \end{matrix} \end{matrix}, \quad c = \begin{matrix} & \begin{matrix} 4 \\ \text{Ni} \end{matrix} \\ \begin{matrix} 10000 \\ \end{matrix} \end{matrix}, \quad d = \begin{matrix} & \begin{matrix} 4 \\ T \end{matrix} \\ \begin{matrix} \infty \\ \end{matrix} \end{matrix}$$

**1,2 e5 data points**

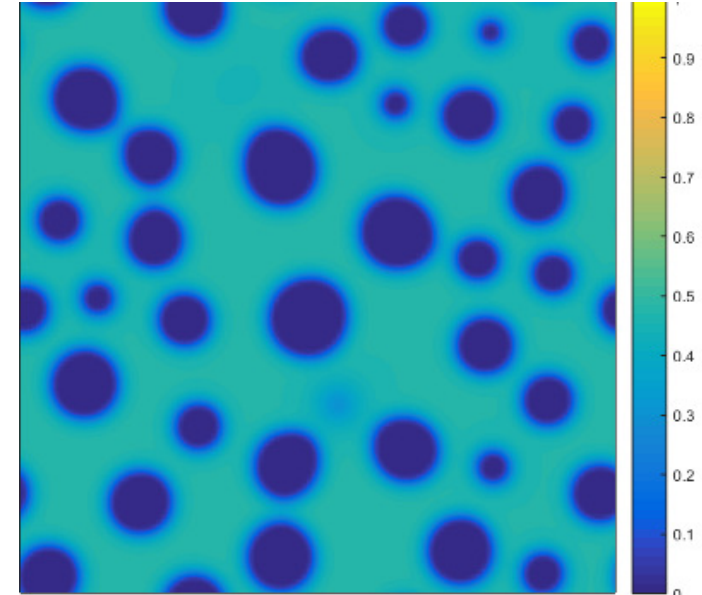
# Phase-field model Ag-Cu-Ni-Sn liquid



$x_{Ag}(x, y, z, t')$



$x_{Cu}(x, y, z, t')$



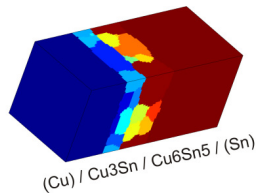
$x_{Ni}(x, y, z, t')$

$$\frac{\partial x_{Ag}(x, y, t)}{\partial t} = \nabla M \cdot \nabla \left[ \frac{\partial G(x_{Ag}, x_{Cu}, x_{Ni}, T)}{\partial x_{Ag}} - \epsilon \nabla^2 x_{Ag} \right]$$

# ERC-2016-StG INTERDIFFUSION

## Innovative & high potential idea

### Phase-field simulations



$$\frac{\partial \phi}{\partial t} = -L \left[ \frac{\partial G}{\partial \phi} - \nabla^2 \phi \right]$$

### Tensor decomposition

$$\mathcal{T} = \begin{matrix} c_1 \\ | \\ a_1 \end{matrix} b_1 + \dots + \begin{matrix} c_R \\ | \\ a_R \end{matrix} b_R$$

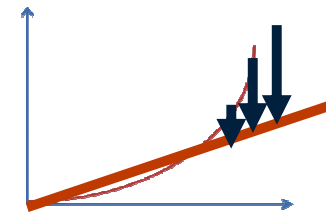
$\mathbb{I}^N \rightarrow \mathbb{R}^* \mathbb{N}^* \mathbb{I}$

Microstructure characteristics  
(comp, t, Temp, ...)

## Breakthroughs

- ❖ Simulations with 5-8 elements
  - ❖ (Re)Interpretation experiments
  - ❖ Search & Discovery
- Accelerated material & product design

Testing time



Principle elements



	Implementation/ Validation module (month 1-24)	Discovery module (month 1-60)	Multi-material design module ( <i>postdoc</i> , <i>month 25-60</i> )
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Tensor decomposition

$\pm 45500$  simulations

130 variables (N), 50 values (I), assume  $R = 7$

Corresponds to  $50^{130} \approx 10^{220}$  tensor elements

(PIB 4, month 15-60)

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Thank you !

