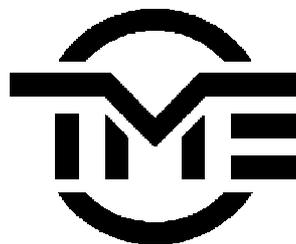


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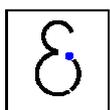
Redispatching in an interconnected electricity system with high renewables penetration

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Redispatching in an interconnected electricity system with high renewables penetration

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Abstract

Grid congestion management is gaining importance in certain parts of the European electricity grid. The deployment of renewable electricity sources at locations with a weak grid connection and far from the load centers can lead to overloading of transmission lines. Redispatching, i.e., rearranging scheduled generation and consumption, might be needed to obtain a feasible and safe operational state of the electricity system. This paper studies the impact of three parameters on the redispatching quantities and costs: (1) loop flows through the electricity system, (2) an increase in renewable generation in remote areas, and (3) a curative and preventive N-1 security criterion. Towards this aim, a dedicated generation scheduling model is developed, consisting of a day-ahead market and a redispatch phase. The Belgian power system is considered as case study. Three general conclusions can be drawn from this paper. First, it is important to consider loop flows when quantifying redispatching, especially in a highly interconnected electricity system as the European system. The case study shows that loop flows can more than double the need for redispatching. Second, transmission grid constraints might restrict the deployment of renewables in certain areas. Third, relaxing the N-1 security criterion in congested grid areas from preventive to curative can drastically reduce the redispatch costs.

Keywords: Congestion management, redispatching, renewables integration, loop flows, N-1 security.

Nomenclature

Sets

I (index i) set of conventional power plants (subset I_{nuc} contains nuclear units)

J (index j) set of renewable generation units

L (index l) set of transmission lines

N (index n) set of nodes

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	S (index s)	set of line contingencies
11	T (index t)	set of time steps
12	Parameters	
	$A_{n,t}^{PLANT}$	matrix linking power plants to nodes {0,1}
	$A_{n,j}^{RES}$	matrix linking renewable units to nodes {0,1}
	C_i	generation cost at minimum power output [EUR/h]
	CC_j	cost of curtailment [EUR/h]
	$D_{n,t}$	electricity load [MW]
	$\overline{F}_{l,s}$	transmission capacity of a line [MW]
	LC	cost of lost load [EUR/MWh]
	MC_i	marginal generation cost [EUR/MWh]
13	MDT_i	minimum down time [h]
	MUT_i	minimum up time [h]
	\overline{P}_i	maximum power output [MW]
	\underline{P}_i	minimum power output [MW]
	$PTDF_{l,n,s}$	power transfer distribution factors
	SR^+	required upward spinning reserve [MW]
	SR^-	required downward spinning reserve [MW]
	SUC_i	start-up cost [EUR/start-up]
	$RES_{j,t}$	available renewable generation [MW]
14	Variables	
	$curt_{j,t,s}^{RD}$	renewables curtailment (redispatch) [MW]
	$g_{i,t}^{DA}$	power generation above minimum output (day-ahead) [MW]
	$g_{i,t,s}^{RD}$	power generation above minimum output (redispatch) [MW]
	$inj_{n,t,s}^{RD}$	grid injection (redispatch) [MW]
	$ll_{n,t,s}^{RD}$	loss of load (redispatch) [MW]
15	$v_{i,t}^{DA}$	start-up status (day-ahead) {0,1}
	$v_{i,t}^{RD}$	start-up status (redispatch) {0,1}
	$w_{i,t}^{DA}$	shut-down status (day-ahead) {0,1}
	$w_{i,t}^{RD}$	shut-down status (redispatch) {0,1}
	$z_{i,t}^{DA}$	on/off-status (day-ahead) {0,1}
	$z_{i,t}^{RD}$	on/off-status (redispatch) {0,1}

1. Introduction

Transmission constraints restrict the amount of electric power that can be transported between two points in the grid. A grid congestion occurs whenever the physical or operational transmission limit of a line is reached or violated [1]. Congestion management can be defined as all actions taken to avoid or relieve congestions in the electricity grid [2].

Congestion management is becoming increasingly important in a system with a high penetration of intermittent renewables. According to ENTSO-E, the association of European Transmission System Operators for Electricity, 80% of the bottlenecks identified in the European grid are directly related to renewables integration [3]. Renewable generation units are often installed in areas with a high load factor, but not necessarily close to the load center or to the existing high voltage grid (e.g., offshore wind farms) [4]. ENTSO-E distinguishes between direct connection issues (i.e., the connection between the renewable generation unit and the existing grid) and congestion issues (i.e., congestion in the existing grid between the renewable generation unit and the load center). The latter is dealt with in this paper.

Often, transmission constraints are only taken into account to a limited extent in electricity markets. The market clearing algorithm determines the accepted generation and consumption bids within a bidding zone, and the exchange with other zones.¹ The transmission limits between different bidding zones are considered in the market clearing, but transmission constraints within a bidding zone are neglected. This can lead to grid congestions which need to be solved by proper congestion management. Different forms of congestion management are discussed in the literature. One can distinguish between a centralized or a decentralized approach [5]. According to the first approach, one centralized entity is responsible for managing grid congestions. This entity is typically the Transmission System Operator (TSO) or the Independent System Operator (ISO). In such centralized approach, generators and consumers trade electricity and schedule their generation and consumption units without taking account of the grid constraints within their bidding zone. The system operator then undertakes all required actions after the market clearing to avoid line overloading within the bidding zone. One of the possible remedial actions is redispatching. Redispatching is defined as rearranging the generation (and consumption) schedule in order to obtain a feasible schedule that respects all transmission constraints

¹Allocation of the cross-border capacity to generators or consumers can happen explicitly or implicitly. In explicit cross-border allocation, a market player first has to obtain the right to use the cross-border capacity before electricity can be traded with a market player in another bidding zone. In implicit cross-border allocation, cross-border capacity is allocated together with the trade of electricity between different bidding zones.

44 [6],[7],[8]. Other short-term remedial actions are changing the set point of flexible transmission systems
45 like phase shifting transformers [9]. On the longer run, the system operator might invest in grid rein-
46 forcements to solve structural grid congestions [10],[11],[12]. According to the decentralized approach,
47 the size of bidding zones is reduced and more transmission constraints are taken into account in the
48 market clearing (i.e., the transmission constraints between the bidding zones). In the limit, every node
49 in the electricity grid is a bidding zone. The result is locational price signals, i.e., electricity prices
50 which can differ between different places in the grid when congestion occurs [13]. On the short term,
51 locational electricity prices give an incentive to generate and consume electricity at places in the grid
52 which do not lead to congestion [14],[15]. On the longer term, locational price signals would drive
53 generators and consumers to install new generation or consumption units at places in the grid with
54 little grid congestion.

55 Redispatching is an important congestion management measure in the European electricity sector, and
56 this for two reasons. First, a centralized approach to congestion management is implemented, where
57 the TSOs have the responsibility to avoid grid congestions within their bidding zone. Second, due to
58 the rapid deployment of renewable electricity, grid congestions become more common. On the short
59 term, redispatching is the main tool for the TSO to relieve the grid congestions. Due to these two
60 reasons, one sees an increase in redispatching in the European electricity grid [6]. In Germany, for
61 instance, redispatching is a pressing issue at the time of writing.

62 This paper focusses on redispatching as congestion management tool. The aim of this study is to
63 quantify the redispatch quantities and costs for a realistic case study, and investigate the impact of
64 loop flows, increasing renewable generation and the N-1 security criterion. Towards this aim, the
65 Belgian electricity system is studied in detail. The Belgian system is an exemplary case to illustrate
66 the congestion issues that can arise due to renewables deployment. Belgium aims to integrate a
67 considerable amount of offshore wind generation, but the current grid connection between the shore
68 and the main load centers is rather weak, causing grid congestions. Similar situations occur in other
69 places in the European grid. Although the results presented in this paper are case-specific, general
70 trends and conclusions can be derived.

71 This paper addresses congestion management with a market oriented approach. The focus lies on the
72 market design in place to deal with congestion management and the redispatching that results from
73 it. In this regard, a proper modeling of the generation portfolio is important in order to take account
74 of dynamic power plant constraints which can impact redispatch costs (e.g., minimum up and down

75 times). Another approach to congestion management is taken by a series of papers which focuses
76 on the computational challenges related to models that determine a safe and secure grid operation,
77 i.e., Optimal Power Flow (OPF) models [16]. An OPF determines the optimal network operation. A
78 Security Constrained Optimal Power Flow (SCOPF) is a generalization of the OPF that additionally
79 considers a set of postulated contingencies in the OPF [17]. The (SC)OPF is a non-linear, non-convex,
80 optimization problem which makes it hard to solve for large-scale electricity systems. However, large
81 scale studies exist which present SCOPF case studies of, for instance, Great Britain [18] and Poland
82 [19].

83 The added value of this paper to the existing literature is twofold. First, the results presented in
84 this paper follow from a case study with very detailed grid data and time series, based on a real-
85 life electricity system. This unlike most market-oriented case studies on redispatching presented in
86 the literature, which typically use a simplified or methodological test system [9],[8],[12]. Second, this
87 paper studies quantitatively the impact of various parameters on redispatching (loop flows, increased
88 renewable generation, and N-1 security criterion) whereas the existing literature takes these parameters
89 as fixed. This paper complements the existing literature and indicates the complexity of redispatching.
90 The paper proceeds as follows. Section 2 gives an overview of the different redispatch options and
91 costs for the TSO. Section 3 describes the dedicated model that is developed to simulate the day-
92 ahead generation scheduling and the redispatching phase. Section 4 presents the Belgian electricity
93 system as case study. Section 5 presents and discusses the results. Finally, section 6 concludes.

94 **2. Redispatch actions and costs**

95 Electricity markets in Europe are zonal markets, meaning that every bidding zone is represented as
96 one single node and connected to other nodes by cross-border links.² As a result, the market clearing
97 does not take into account transmission limits within a bidding zone, and this may lead to technically
98 infeasible generation schedules. At this point, the TSO comes into play. The TSO performs an ex-post
99 analysis to validate the feasibility of the generation schedule. If grid congestions occur within the
100 bidding zone, the TSO issues redispatch orders to generators to reschedule their generation.

101 The TSO can issue different types of redispatch orders, each with a related cost (or revenue);

²Most bidding zones in Europe coincide with countries, e.g., Belgium is one bidding zone, but exceptions exist. For instance, Germany and Austria are one bidding zone.

- 102 • A TSO can request an increase in power output of a conventional generation unit.³ In return,
103 the generator will expect a compensation for increasing its power output, equal to at least the
104 additional generation cost. The additional generation cost consists of the cost for additional fuel,
105 CO₂ emissions and possibly extra start-ups.
- 106 • A TSO can request a decrease in power output of a conventional generation unit. The generator
107 will pay the TSO to decrease its power output, equal to at most the avoided generation cost.⁴
108 The avoided generation cost consists of the cost for the non-used fuel, CO₂ emissions and possibly
109 avoided start-ups.
- 110 • A TSO can request a decrease in renewable generation, if technically, practically and regulatory
111 feasible.⁵ The renewable generator will expect a compensation for curtailing its generation equal
112 to at least the missed financial support for renewables (assuming a zero marginal generation
113 cost).

114 Figure 1 gives a schematic overview of the possible redispatch actions and costs for the TSO. The
115 following numbers are used in this study and can give an idea of the costs and revenues related to
116 redispatch orders. The marginal generation costs of conventional units range from 18 EUR/MWh
117 for nuclear units to 95 EUR/MWh for open-cycle gas turbines. The renewable support for curtailable
118 renewables goes from 0 to 100 EUR/MWh. The cost used in this paper for loss of load and curtailment
119 of renewables with priority access is 10,000 EUR/MWh (i.e., indicating system infeasibilities). The net
120 redispatch cost of the TSO will always be positive as the starting point of the redispatch phase, i.e., the
121 day-ahead market outcome, is the result of a minimization of generation costs (without considering grid
122 constraints). In the redispatch phase, expensive generation, which was not scheduled in the day-ahead
123 market, needs to replace cheaper generation, which was scheduled in the day-ahead market.

124 Other redispatch actions than the ones mentioned in this section might be possible, such as topolog-
125 ical actions and the use of phase shifters. However, they are not dealt with in this paper as they are
126 not applicable to the considered case study. Topological actions are not used by the TSO to avoid
127 redispatching of conventional generation units due to the short-term and time-variable character of

³Conventional generation units refer to centralized and dispatchable units. In this paper, conventional generation units refer to nuclear units and gas fired units (no coal fired units are operational in the considered electricity system).

⁴The running generation units have sold their electricity already in the day-ahead market at the day-ahead price. Conventional generators have the same pay-off when they run and incur generation costs then when they are off-line and pay the avoided generation costs to the TSO.

⁵A renewable generation unit can be used for redispatching purposes if curtailment of its power output is technically feasible, can be measured for billing purposes and is allowed by regulation.

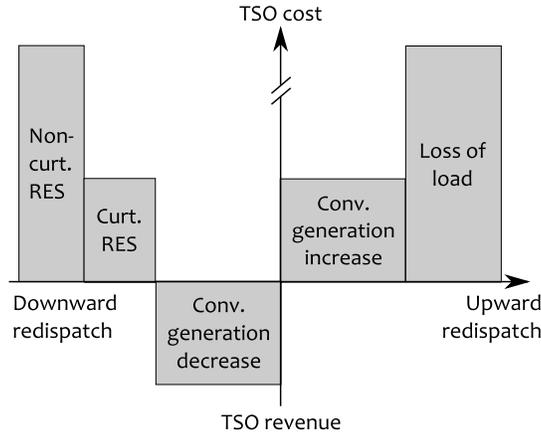


Figure 1: Schematic overview of possible redispatch actions for the Transmission System Operator (TSO) (RES: renewables, Curt.: curtailment, Conv.: conventional).

128 redispatching, especially when caused by intermittent renewable generation. Moreover, by not using
 129 topological actions for short-term congestion management, a certain margin is still available to guar-
 130 antee a safe grid operation, which can be used to deal with grid maintenance situations. No phase
 131 shifters are present within the studied electricity network (although there are phase shifters installed
 132 on the borders of the considered case study but they are used to control loop flows through the system
 133 and not for solving local congestions within the grid).
 134 Note that this paper only deals with day-ahead congestions caused by neglecting network constraints
 135 within bidding zones in the day-ahead market. Congestions which occur intra-day or real-time due
 136 to contingencies or large variations in renewable generation are not discussed. However, a similar
 137 approach as presented in this paper can be used to address the latter (although possibly without
 138 contingency constraints).

139 3. Model description

140 To study redispatching, the authors have developed a dedicated model. The model consists of two
 141 sub-models which are solved sequentially, reflecting a two-step approach. In a first step, the optimal
 142 day-ahead generation schedule is determined, without taking into account the transmission limits
 143 within the bidding zone. In a second step, the day-ahead generation schedule is evaluated by means
 144 of a DC power flow and redispatch actions are taken to avoid transmission line overloading in the
 145 bidding zone. This two-step approach corresponds to the actual market design in which generators
 146 first schedule their generation units without considering intra-zonal transmission limits, followed by a
 147 feasibility evaluation of the generation schedule by the TSO.

148 The optimal day-ahead generation schedule is determined by a unit commitment model. The output
149 of the unit commitment model is the generation schedule that fulfills load at minimal operational
150 generation cost. As already mentioned, transmission constraints within the considered bidding zone
151 are not considered in this first step. Commercial exchange of electric power with neighboring bidding
152 zones is limited by the Net Transfer Capacity (NTC) of the cross-border connections.

153 If the day-ahead generation schedule is infeasible due to grid constraints, generation needs to be
154 rearranged. Any deviation from the day-ahead generation schedule will result in a net cost for the TSO
155 as generation needs to be replaced by more expensive generation. The optimal redispatch schedule
156 is determined by a redispatch model that minimizes the cost for the TSO. However, the possible
157 redispatch actions are constrained by the unit commitment decision taken in the day-ahead market.
158 The redispatch model determines a curative N-1 secure system operation, meaning that the solution
159 of the redispatch model is able to deal with line contingencies if curative actions are allowed after
160 the contingency occurred. Curative actions refer to changing the economic dispatch of conventional
161 generation units and changing the curtailment of renewables [16].

162 The optimization model presented in this paper is meant to be used for market oriented studies of
163 redispatching, and can be used towards this aim by researchers, policy makers, TSOs and regulators.
164 Both sub-models -unit commitment and redispatch- are formulated as mixed-integer linear programs
165 in GAMS and solved with CPLEX 12.6, using an optimality criterion of 0.1%. The considered time
166 period is one year with an hourly time step. The models solve blocks of two days, with one day overlap
167 to ensure a correct coupling between the consecutive days.⁶

168 The applied methodology entails certain assumptions. First, the study is fully deterministic, meaning
169 that no stochastic variables are considered (e.g., wind power forecast errors). The input parameters
170 are the same in the day-ahead market and the redispatch model and are assumed to be perfectly
171 known to all generators in advance. Second, the models use an hourly time step since the day-ahead
172 markets in Europe are currently based on an hourly time resolution. Within this time resolution, not
173 all variations in the time series for load and renewable generation are seen. Moreover, the (technical)
174 ramping constraint of conventional units is not restricting on an hourly basis; no ramping constraints
175 are considered in this study. Third, the modeling framework assumes a centrally cleared and perfectly

⁶The one-day overlap is based on the largest minimum up/down time in the generation portfolio (i.e., a 24 hour minimum up/down time for nuclear units, see Table 1). By working with a one-day overlap, the model considers the full length of the nuclear minimum up/down time when taking a decision to start-up/shut-down a nuclear unit at the end of the first considered day.

176 competitive electricity market. In Belgium (and other European countries), electricity is traded day-
 177 ahead bilaterally and through power exchanges with (simplified) bidding. However, assuming a perfect
 178 competitive market, the market outcome of both market designs is very similar. Fourth, it is assumed
 179 that all conventional units can be called upon by the TSO for redispatching at a cost (revenue) equal
 180 to the additional (avoided) generation cost for increasing (decreasing) their power output. However,
 181 this might not be the case as the bidding strategies and generation costs are private and confidential
 182 information.

183 3.1. Day-ahead model (unit commitment)

184 The objective function of the unit commitment model is the minimization of the operational generation
 185 cost:

$$\min \sum_t \sum_i C_i z_{i,t}^{DA} + MC_i g_{i,t}^{DA} + SUC_i v_{i,t}^{DA} \quad (1)$$

186 For clarification on the symbols, the reader is referred to the nomenclature section at the outset of the
 187 paper. The generation cost consists of generation costs (fuel and CO₂ emissions) and start-up costs.
 188 The objective function is subject to the market clearing constraint (equation 2), generation limits of
 189 conventional units (equation 3), minimum up and down time constraints (equations 4-5), the logic
 190 relation between different states of the power plants (equation 6), upward and downward spinning
 191 reserves (equations 7-8), binary constraints (equation 9) and non-negative constraints (equation 10),
 192 all displayed here below:

$$\sum_i (z_{i,t}^{DA} \underline{P}_i + g_{i,t}^{DA}) = \sum_n D_{n,t} - \sum_j RES_{j,t} \quad \forall t \quad (2)$$

$$0 \leq g_{i,t}^{DA} \leq (\overline{P}_i - \underline{P}_i) z_{i,t}^{DA} \quad \forall i, t \quad (3)$$

$$z_{i,t}^{DA} \geq \sum_{t'=t+1-MUT_i}^t v_{i,t'}^{DA} \quad \forall i, t \quad (4)$$

$$1 - z_{i,t}^{DA} \geq \sum_{t'=t+1-MDT_i}^t w_{i,t'}^{DA} \quad \forall i, t \quad (5)$$

$$z_{i,t-1}^{DA} - z_{i,t}^{DA} + v_{i,t}^{DA} - w_{i,t}^{DA} = 0 \quad \forall i, t \quad (6)$$

$$\sum_{i \notin I_{nuc}} ((\bar{P}_i - P_i) z_{i,t}^{DA} - g_{i,t}^{DA}) \geq SR^+ \quad \forall t \quad (7)$$

$$\sum_{i \notin I_{nuc}} g_{i,t}^{DA} \geq SR^- \quad \forall t \quad (8)$$

$$z_{i,t}^{DA}, v_{i,t}^{DA}, w_{i,t}^{DA} \in \{0, 1\} \quad \forall i, t \quad (9)$$

$$g_{i,t}^{DA} \geq 0 \quad \forall i, t \quad (10)$$

193 The unit commitment model, as presented in this section, is based on [20].

194 3.2. Redispatch model

195 The objective function of the redispatch model aims at minimizing the redispatch cost for the TSO:

$$\begin{aligned} \min \sum_t \sum_i & \left(C_i (z_{i,t}^{RD} - z_{i,t}^{DA}) + MC_i (g_{i,t,1}^{RD} - g_{i,t}^{DA}) + SUC_i (v_{i,t}^{RD} - v_{i,t}^{DA}) \right) \\ & + \sum_t \sum_j CC_j curt_{j,t,1}^{RD} + \sum_t \sum_n LC u_{n,t,1}^{RD} \end{aligned} \quad (11)$$

196 Again, the reader is referred to the nomenclature section at the outset of the paper for clarification on
 197 the symbols. Only the N-situation is considered in the objective function (s equal to 1), but all N-1
 198 situations are considered in the constraints. The objective function is subject to the market clearing
 199 constraint (equation 12), the day-ahead on/off-decision for nuclear units (equation 13), generation
 200 limits of conventional units (equation 14), minimum up and down time constraints (equations 15-16),
 201 the logic relation between different states of the power plants (equation 17), upward and downward
 202 spinning reserves (equations 18-19), curtailment limits (equation 20), loss of load limits (equation
 203 21), grid limitations (equations 22-23), binary constraints (equation 24) and non-negative constraints

204 (equation 25), as follows:

$$\sum_i A_{n,i}^{PLANT} (z_{i,t}^{RD} \underline{P}_i + g_{i,t,s}^{RD}) + \sum_j A_{n,j}^{RES} (RES_{j,t} - curt_{j,t,s}^{RD}) = D_{n,t} - ll_{n,t,s}^{RD} + inj_{n,t,s}^{RD} \quad \forall n, t, s \quad (12)$$

$$z_{i,t}^{RD} = z_{i,t}^{DA} \quad \forall i \in I_{nuc}, t \quad (13)$$

$$0 \leq g_{i,t,s}^{RD} \leq (\overline{P}_i - \underline{P}_i) z_{i,t}^{RD} \quad \forall i, t, s \quad (14)$$

$$z_{i,t}^{RD} \geq \sum_{t'=t+1-MUT_i}^t v_{i,t'}^{RD} \quad \forall i \notin I_{nuc}, t \quad (15)$$

$$1 - z_{i,t}^{RD} \geq \sum_{t'=t+1-MDT_i}^t w_{i,t'}^{RD} \quad \forall i \notin I_{nuc}, t \quad (16)$$

$$z_{i,t-1}^{RD} - z_{i,t}^{RD} + v_{i,t}^{RD} - w_{i,t}^{RD} = 0 \quad i, t \quad (17)$$

$$\sum_{i \notin I_{nuc}} ((\overline{P}_i - \underline{P}_i) z_{i,t}^{RD} - g_{i,t,1}^{RD}) \geq SR^+ \quad \forall t \quad (18)$$

$$\sum_{i \notin I_{nuc}} g_{i,t,1}^{RD} \geq SR^- \quad \forall t \quad (19)$$

$$curt_{j,t,s}^{RD} \leq RES_{j,t} \quad \forall j, t, s \quad (20)$$

$$ll_{n,t,s}^{RD} \leq D_{n,t} \quad \forall n, t, s \quad (21)$$

$$-\overline{F}_{l,s} \leq \sum_n PTDF_{l,n,s} inj_{n,t,s}^{RD} \leq \overline{F}_{l,s} \quad \forall l, t, s \quad (22)$$

$$\sum_n inj_{n,t,s}^{RD} = 0 \quad \forall t, s \quad (23)$$

$$z_{i,t}^{RD}, v_{i,t}^{RD}, w_{i,t}^{RD} \in \{0, 1\} \quad \forall i, t \quad (24)$$

$$g_{i,t,s}^{RD}, curt_{j,t,s}^{RD}, ll_{n,t,s}^{RD}, inj_{n,t,s}^{RD} \geq 0 \quad \forall i, t, s \quad (25)$$

205 The redispatch model is developed by the authors and dedicated to this study. A DC power flow
 206 model of the electricity network is being used. The main advantage of a DC power flow model is its
 207 linearity compared to the non-linear AC power flow model. This allows solving large power systems
 208 for multiple time steps in a limited run time. The disadvantage of a DC power flow is its reduced
 209 accuracy. The literature mentions, for high voltage grids, an average 5% deviation between line flows
 210 in a DC power flow model and in an AC power flow model [21]. However, the use of a DC power flow
 211 is justified in this paper given its focus on yearly aggregated redispatch quantities and costs, rather
 212 than on particular line flows in specific hours.

213 4. The Belgian power system as case study

214 The case study presented in this paper is the expected Belgian 2016 system (see Figure 2). Belgium
 215 has a well developed and meshed high voltage grid, connecting the main load and generation centers.
 216 Therefore, grid congestions and congestion management were never a pressing issue for the Belgian TSO
 217 in the past. However, this has changed due to the deployment of offshore wind power in the Belgian
 218 North Sea. Over the last years, about 800 MW of offshore wind power has been commissioned. This
 219 raises congestion issues as the transmission grid connecting the shore with the 380 kV grid was not
 220 designed to accommodate large landward power flows from offshore wind. As a result, congestions in
 221 the existing 150 kV grid in the coastal area become more apparent. At the same time, injections of
 222 onshore renewable generation in this area are increasing as well, further worsening the situation. The
 223 Belgian case is exemplary for the difficulties associated with the deployment of renewable generation
 224 in areas where the grid was not built to accommodate these new injections.⁷

⁷The Belgian TSO is, at the time of writing, strengthening the grid with a new 380 kV connection between the shore and the existing 380 kV grid. This new connection is not expected to be in place before the end of 2016.

225 The model to simulate the electricity grid in this study is a detailed DC power flow model with 161
 226 nodes and 241 line elements (transmission lines, transformers and couplings). The whole Belgian 380
 227 kV transmission grid is included, together with the 150 kV grid in the Western part of Belgium.
 228 The remaining part of the 150 kV grid and the 220 kV grid are represented by equivalent lines and
 229 nodes. The grid model allows to study grid congestions in the coastal region in detail. Not all line
 230 contingencies are considered in the N-1 analysis. Eight critical line outages are determined ex-ante
 231 by the TSO experts and taken into account in the redispatch optimization. In an N-1 situation,
 232 transmission flows can go to 120% of the rated line capacity.

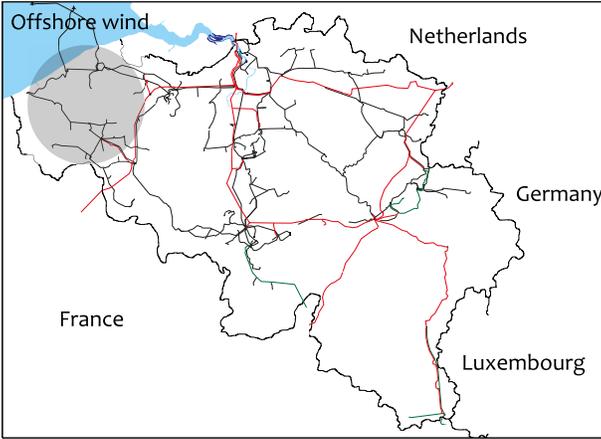


Figure 2: Overview of the Belgian high voltage grid (red: 380 kV lines, green: 220 kV lines, black: 150 kV lines) [22]. Grid congestions occur in the grey area between the offshore wind farms in the North Sea and the 380 kV grid.

233 Historical nodal load measurements are scaled up and used as demand time series. The annual electric
 234 energy demand is 90.2 TWh, with a peak demand of 13.9 GW in the winter and the lowest demand
 235 in the summer of about 6 GW. About 7% of the electricity consumption is located in the coastal
 236 region. The load time series are corrected for commercial exchange with neighboring countries. The
 237 commercial cross-border trade is imposed on the model as an exogenous parameter. In the case study,
 238 Belgium imports on an annual basis 10.8 TWh from France and 3.3 TWh from the Netherlands. Note
 239 that no direct connection with Germany exists at the present time.

240 The generation portfolio consists of 23 conventional generation units, with an aggregated capacity of
 241 8.6 GW. Table 1 shows the technical parameters and generation costs allocated to the conventional
 242 generation units [23]. In this study, the authors assume that all online conventional units can ramp-up
 243 and ramp-down for redispatching purposes. Gas fired units (combined-cycle gas turbines and open-
 244 cycle gas turbines) can also start-up and shut-down for redispatching purposes. Nuclear units cannot

	Units	$\sum \bar{P}$ [GW]	\underline{P} [% \bar{P}]	MUT,MDT [h]	C [EUR/h]	MC [EUR/MWh]	SUC [kEUR/start]
NUC	6	5.1	95	24	8,000-18,000	18	6
CCGT	9	2.9	35	3	1,200-16,000	65-95	83-555
OCGT	8	0.6	30	1	1,000-4,000	70-85	28

Table 1: Overview of technical characteristics per technology (NUC: nuclear, CCGT: combined-cycle gas turbines, OCGT: open-cycle gas turbines, \bar{P} : maximum power output, \underline{P} : minimum power output, MUT: minimum up time, MDT: minimum down time, C: generation cost at \underline{P} , MC: marginal generation cost, SUC: start-up cost) [23].

245 change their on/off-state for redispatching purposes due to too large minimum up and down times.

246 Historical time series for renewable generation and generation from cogeneration units are scaled up

247 and used. Renewable generation refers to generation from conventional hydro, wind energy (offshore

248 and onshore), bio-energy and photovoltaic energy. Three types of renewables are considered, based

249 on the curtailment cost for redispatching purposes. One distinguishes onshore renewable generation

250 with a flexible contract, offshore wind generation and onshore renewable generation with priority grid

251 access. The flexible onshore renewable generation is located in the coastal area and connected to the

252 grid under the condition that the TSO can curtail them at zero cost for redispatching purposes. About

253 180 MW of renewable generation capacity is operated under such a flexible capacity, accounting for a

254 generation of 0.4 TWh/a. Offshore wind can be curtailed in the redispatch phase at the cost of the

255 financial support for offshore wind generation, i.e., 100 EUR/MWh. By 2016, 870 MW of offshore

256 wind capacity is expected in the Belgian North Sea, accounting for a generation of 3.1 TWh/a (i.e.,

257 normal wind year with a load factor of 40 %). The onshore renewable generation capacity with priority

258 access to the grid is about 6.2 GW, responsible for a yearly generation of 11.2 TWh. The redispatch

259 model allows curtailment of these last renewable generation units only at a very high cost of 10,000

260 EUR/MWh. Moreover, 4.1 GW of cogeneration units (electric capacity) is installed, with a yearly

261 electricity generation of 23.5 TWh/a. No curtailment of cogeneration units is allowed.

262 Recall that the studied power system is the expected 2016 Belgian power system, based on hypotheses

263 regarding the development of generation capacity and demand. The authors are not responsible for

264 the realisation of these hypotheses. The results of the paper can only be interpreted correctly taken

265 into account these hypotheses.

266 5. Results and discussion

267 This section presents the redispatch quantities and the redispatch costs due to grid congestions in the

268 considered case study. First the reference case is presented, i.e., the anticipated Belgian 2016 power

269 system. In the following subsections, the impact of loop flows, increasing offshore wind and the N-1
270 security criterion are discussed.

271 *5.1. Reference scenario: Belgian 2016 power system*

272 The day-ahead market outcome for the reference scenario is shown on Figure 3. In terms of TWh/a,
273 the system load is mainly covered by renewable generation and cogeneration units (42%), nuclear
274 generation (38%) and import (16%). CCGTs generate 2.5 TWh/a (load factor of the operating CCGTs
275 is only 18%; part of the CCGT units is never used) and OCGTs generate 1 TWh/a (load factor of
276 17%). These gas units are mainly brought online to fulfil the spinning reserve requirement. The total
277 annual generation cost (fuel, CO₂ emissions and start-ups, excluding the cost of import) is 899 Mio
278 EUR.

279 This day-ahead market solution then possibly needs to be adapted to get a feasible generation schedule
280 that takes account of the grid constraints. The feasibility of the day-ahead generation schedule can
281 be checked by calculating the grid flows through all transmission lines resulting from the day-ahead
282 generation schedule, and this for the N-state and each considered N-1 state. If the capacity of at least
283 one transmission line is exceeded, redispatching will be needed. It turns out that during 1,972 hours
284 of the year (23% of the time), grid congestions occur and redispatching will be needed.

285 The TSO has one option for upward redispatching -increasing conventional generation (Conv+)- and
286 two for downward redispatching -decreasing conventional generation (Conv-) and curtailing flexible
287 onshore renewable generation and offshore wind (RES-). From the redispatch simulation follows that
288 34.3 GWh/a of upward redispatching is required. The amount of upward and downward redispatching
289 is by definition equal (the electricity demand still has to be met). The downward redispatching consists
290 of 29.3 GWh/a of conventional generation that is ramped down and 5 GWh/a of curtailed renewable
291 generation. Overall, the amount of redispatching is rather limited as only 0.08% of the annual load
292 is redispatched.⁸ Loss of load and curtailment of renewable generation with priority access is only
293 possible at the very high cost of 10,000 EUR/MWh, indicating system infeasibilities. However, neither
294 loss of load nor curtailment of renewable generation with priority access occurs in the reference case.
295 The annual redispatch cost is 2.9 Mio EUR.

⁸The redispatch simulations indicate redispatch due to two reasons; grid congestions and renewables curtailment. In the day-ahead market, no renewables curtailment is allowed, while in the redispatch phase curtailment of flexible onshore renewables and offshore wind is possible. If renewables curtailment is a cost-efficient measure, the model will perform curtailment in the redispatch phase and reduce overall system costs (i.e., a net income for the TSO). However, this study only deals with redispatching due to grid congestions. Therefore the numbers shown in this paper refer only to redispatching due to grid congestions.

296 The total amount of downward redispatching, i.e., 34.3 GWh/a, can be split up in 15 GWh/a of
 297 downward redispatching in the coastal area and 19.3 GWh/a of downward redispatching in the rest of
 298 Belgium. The downward redispatching in the coastal area is a direct consequence of grid congestions
 299 (i.e., there is not enough transmission capacity to transport all planned generation from the coastal
 300 area landward). Downward redispatching in the rest of Belgium is caused by the minimum operating
 301 point of the units delivering upward redispatching. If a unit starts up for redispatch purposes, that
 302 unit has to operate above its minimum operating point. Therefore, additional downward redispatching
 303 might be needed elsewhere.

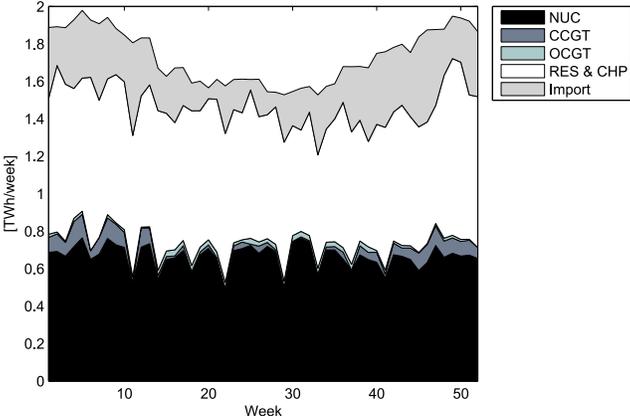


Figure 3: Weekly day-ahead generation schedule in the reference scenario (NUC: nuclear, CCGT: combined-cycle gas turbines, OCGT: open-cycle gas turbines, RES: renewables, CHP: cogeneration).

304 *5.2. Impact of loop flows*

305 In the reference case, only the commercial exchange of electricity with the neighboring countries was
 306 considered. However, the actual power flows on the cross-border lines can largely deviate from the
 307 commercial cross-border exchange, due to loop flows. Loop flows are power flows through the Belgian
 308 grid caused by injections or withdrawals in other parts of the European grid. As these loop flows enter
 309 and leave the control area (by the same amount), they do not impact the net exchange position of the
 310 Belgian system, but they do impact the flows through the transmission lines in the Belgian system
 311 and hence also the need for redispatching. This is clarified in an example below.

312 Loop flows are particularly important in a highly interconnected electricity grid like the European
 313 grid. The Belgian electricity grid is connected to the Netherlands in the north and to France in the
 314 south. The northern border has a Net Transfer Capacity (NTC-value) of 1,000 to 1,500 MW and the

315 southern border has a NTC-value of 2,000 to 2,500 MW, both for the importing direction [24].⁹ The
316 NTC-values are given to the electricity market as import/export constraint and used for commercial
317 exchange between different market zones.

318 To check the effect of loop flows, an annually fixed loop flow is added to the commercial cross-border
319 flow in the redispatch phase. The positive direction of the loop flow is defined from north to south (i.e.,
320 from the Netherlands to France). Consider, for instance, a certain time step where Belgium imports
321 commercially net 1,000 MW from France in the south and 500 MW from the Netherlands in the north
322 (net exchange position of Belgium is -1,500 MW). If a loop flow of 100 MW is imposed, the resulting
323 physical flow on the southern border is 900 MW (net import) and 600 MW on the northern border
324 (net import). The net exchange position of the Belgium area stays the same (-1,500 MW), but the
325 power flows within the Belgium system are impacted by the loop flow.

326 Figure 4 and Figure 5 show the impact of loop flows on the amount of redispatching and the redispatch
327 costs, respectively. Loop flows are varied from -2,000 MW to 2,000 MW in steps of 500 MW. The zero
328 loop flow scenario corresponds to the reference case discussed in the previous subsection. Figure 4
329 shows, for each loop flow scenario, the amount of upward redispatching (left bar, consisting of increas-
330 ing conventional generation and loss of load) and the amount of downward redispatching (right bar,
331 consisting of decreasing conventional generation and renewables curtailment). As explained before, the
332 amount of upward and downward redispatching are equal. The impact of loop flows on redispatching
333 is considerable. The redispatched energy and the redispatch costs more than double for large negative
334 loop flows, i.e., northward loop flows. At a loop flow of -2,000 MW, loss of load is needed in the
335 simulations, indicating system infeasibilities (all nodal load can no longer be met). Curtailment of
336 renewables with priority access, i.e., another system infeasibility, never occurs. It turns out that loop
337 flows from the south to the north strongly increase the need for redispatching, whereas loop flows in
338 the other direction have a more modest impact on redispatching. This can be understood as follows;
339 grid congestions are mainly caused by west-east flows in the coastal region (offshore wind generation
340 needs to be transported from the Sea in the west to the main load centers landinward). A loop flow
341 from France to the Netherlands increases this west-east flow as part of the loop flow will enter Belgium
342 in the south-west and leave Belgium in the north-east. A loop flow from the Netherlands to France
343 counteracts the west-east flow, relieving congestion in this direction. However, a north-south loop flow

⁹The NTC-value of a cross-border link depends on the direction (import or export) and the considered moment in time.

344 causes new congestions on the north-south lines in the coastal area. Both effects cancel each other
 345 out, resulting in more or less stable redispatch costs for increasing north-south loop flows. Recall that
 346 in this section, it was assumed that a constant loop flow occurs during the whole year. In reality,
 347 different loop flows occur every hour, changing in magnitude and direction.
 348 Loop flows can - to a certain extent - be mitigated by phase shifting transformers.¹⁰ The redispatch
 349 cost savings that can be obtained by mitigating loop flows can be read from Figure 5 by comparing
 350 the costs in a loop flow scenario with the cost in a zero loop flow scenario. Installing a phase shifter
 351 to mitigate redispatch costs can be interesting if the avoided redispatch costs surpass the investment
 352 and maintenance costs over the life time of the phase shifter (although various other aspects should
 353 be considered, such as the controllability of the phase shifter).

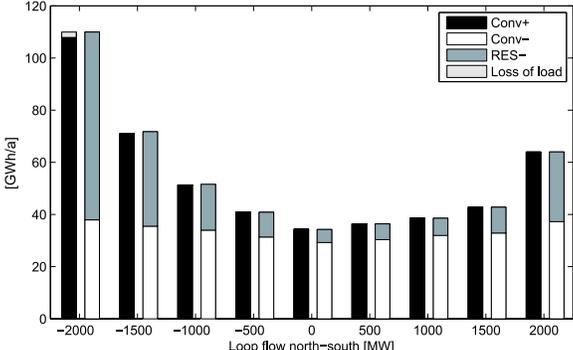


Figure 4: Impact of loop flows on redispatching for 9 loop flow scenarios. The left bar of each loop flow scenario shows the amount of upward redispatching (Conv+: increased conventional generation, and loss of load) and the right bar the amount of downward redispatching (Conv-: decreased conventional generation, and RES-: decreased flexible onshore renewable generation and offshore wind generation). Large negative loop flows can more than double the amount of redispatching.

354 *5.3. Impact of increasing offshore wind*

355 To investigate the effect of increasing offshore wind capacity, a sensitivity analysis is performed. The
 356 installed offshore wind capacity is varied from 800 MW to 2,300 MW in steps of 500 MW (offshore
 357 wind capacity in the reference case is 870 MW, expected offshore wind capacity by 2020 is about
 358 2,300 MW). The offshore wind generation profile is scaled up in proportion to the installed capacity.
 359 This increased offshore generation impacts both the day-ahead generation schedule and the need for
 360 redispatching. The redispatching model considers only a case with zero loop flows.

¹⁰There are phase shifting transformers installed on the Belgian border with the Netherlands and with France, with the aim to mitigate loop flows.

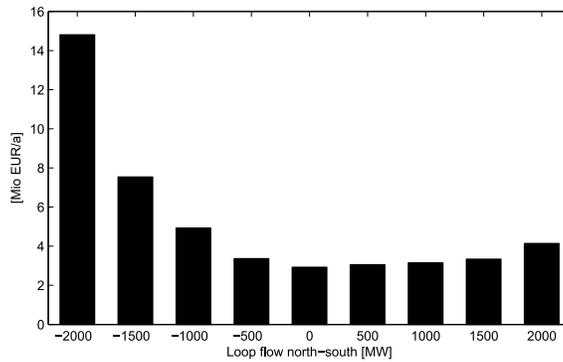


Figure 5: Impact of loop flows on redispatch costs for 9 loop flow scenarios (excluding loss of load cost). Redispatch costs increase drastically for large negative loop flows.

361 The increase in offshore wind generation in the day-ahead market is compensated by a decrease in
 362 generation from nuclear power plants and gas fired power plants. Offshore wind generation increases
 363 from 2.8 TWh/a to 8.1 TWh/a for 800 MW and 2,300 MW of installed capacity, respectively. Addi-
 364 tional offshore wind generation pushes out first the most expensive conventional units, i.e., gas fired
 365 power plants. However, additional offshore wind generation increases the need for flexibility which
 366 is preferably delivered by gas fired generation. These two effects cancel out each other, resulting in
 367 both a decrease in gas fired generation and nuclear generation for an increasing amount of offshore
 368 wind capacity (see Figure 6). The operational generation cost decreases with increasing offshore wind
 369 generation, from 901 Mio EUR for 800 MW offshore wind capacity to 779 Mio EUR for 2,300 MW
 370 offshore wind capacity.

371 Figure 7 and Figure 8 show the amount of redispatching and the redispatch costs for increasing
 372 offshore wind capacity. The amount of redispatching and the redispatch costs increase drastically with
 373 increasing offshore wind generation. For 2,300 MW of offshore wind capacity, about 3% of the annual
 374 electricity demand needs to be redispatched. As of 1,800 MW of offshore wind, loss of load occurs in
 375 the redispatch simulations, indicating system infeasibilities. It might seem counter-intuitive that more
 376 installed offshore wind capacity leads to more loss of load, but more offshore wind generation reduces
 377 the upward redispatch options. Due to more offshore wind generation, some nuclear units are shut
 378 down during certain days in the day-ahead generation schedule. These nuclear units cannot be started
 379 up again in the model for redispatching purposes when it turns out that not all scheduled offshore
 380 generation can be transported to the load centers. This might lead to loss of load in the redispatch
 381 phase. The redispatch costs rise drastically for increasing offshore wind capacity (see Figure 8). This
 382 increase is to a large extent caused by the curtailment of offshore wind at a cost of 100 EUR/MWh. At

383 high installed offshore wind capacities, most of the generation of every additional MW offshore wind
 384 has to be curtailed to avoid line overloading.¹¹

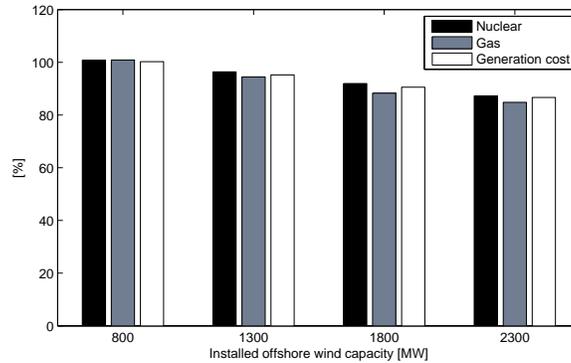


Figure 6: Impact of additional offshore wind capacity on conventional generation and operational generation costs in the day-ahead market. The figure shows the annual nuclear generation, the annual gas generation and the annual generation system costs, all expressed relatively to the reference case with 870 MW offshore wind capacity.

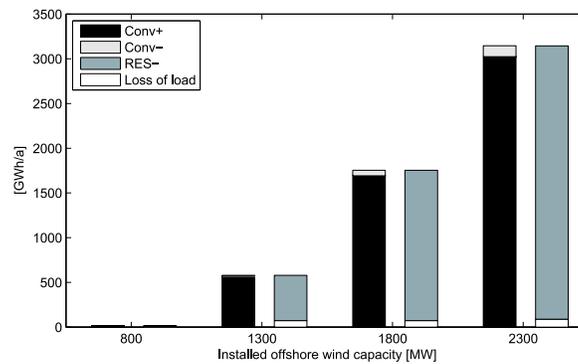


Figure 7: Impact of additional offshore wind on redispatching. The left bar of each offshore wind scenario shows the amount of upward redispatching (Conv+: increased conventional generation, and loss of load) and the right bar the amount of downward redispatching (Conv-: decreased conventional generation, and RES-: decreased flexible onshore renewable generation and offshore wind generation). The amount of redispatching explodes above 1,000 MW offshore wind capacity.

385 5.4. Impact of preventive N-1 security criterion

386 A curative N-1 security criterion has so far been implemented in the redispatch phase. In a curative N-
 387 1 secure system, the economic dispatch of conventional units and the curtailment of renewables can be
 388 changed after the line contingency occurred. In a preventive N-1 secure system, a line contingency has
 389 to be passed without changing the economic dispatch or curtailment. A preventive N-1 secure system

¹¹The Belgian TSO is, at the time of writing, strengthening the grid connection between the shore and the main load centers inland in order to accommodate an increase in offshore wind.

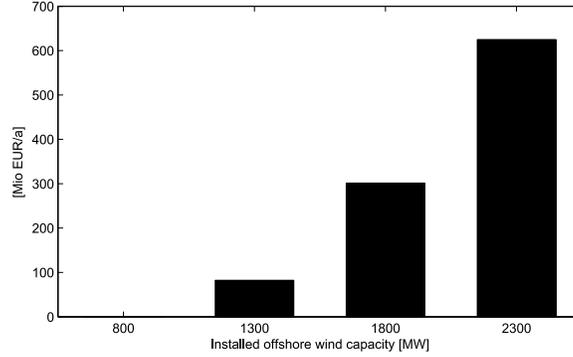


Figure 8: Impact of additional offshore wind on redispatch costs (excluding loss of load cost). Redispatch costs explodes with increasing offshore wind.

390 is hence more stringent than a curative system. This subsection discusses the impact on redispatching
 391 of the more stringent preventive N-1 security criterion, compared to a curative N-1 security criterion.
 392 The redispatch model is extended with the following three equations to impose a preventive N-1 security
 393 criterion, instead of a curative one:

$$g_{i,t,s}^{RD} = g_{i,t,1}^{RD} \quad \forall i, t, s \quad (26)$$

$$curt_{j,t,s}^{RD} = curt_{j,t,1}^{RD} \quad \forall j, t, s \quad (27)$$

$$ll_{n,t,s}^{RD} = ll_{n,t,1}^{RD} \quad \forall n, t, s \quad (28)$$

394 Equations 26-27-28 impose on the model that the economic dispatch, renewables curtailment and loss
 395 of load have to be the same for every N-1 situation.

396 Figure 9 shows the impact of the N-1 security criterion on the redispatch quantities for the reference case
 397 (i.e., 870 MW offshore wind, no loop flows). Without an N-1 security criterion, almost no redispatching
 398 is required. With a curative N-1 security criterion, 34.3 GWh/a of redispatching is needed (i.e., the
 399 reference case). This increases to 220 GWh/a in case of preventive N-1 security. With preventive N-1,
 400 loss of load occurs, indicating system infeasibilities.

401 The redispatch cost increases from 0.2 Mio EUR without an N-1 security criterion to 2.9 Mio EUR
 402 with curative N-1 and 25.9 Mio EUR with preventive N-1. This allows to determine the cost of N-1
 403 security as the difference between the cost with and without N-1 security. For the considered power

404 system, the annual cost of a curative N-1 criterion is 2.7 Mio EUR and 25.7 Mio EUR for a preventive
 405 N-1 criterion.

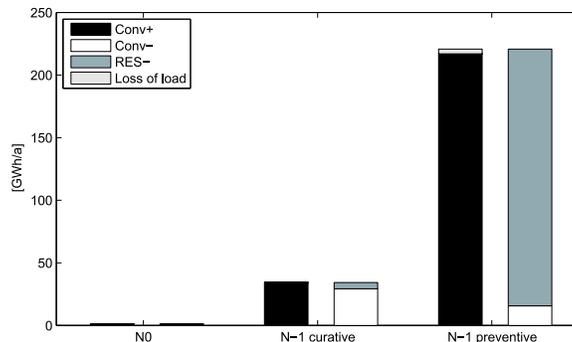


Figure 9: Impact of the N-1 security criterion on redispatching. The left bar of each security criterion shows the amount of upward redispatching (Conv+: increased conventional generation, and loss of load) and the right bar the amount of downward redispatching (Conv-: decreased conventional generation, and RES-: decreased flexible onshore renewable generation and offshore wind generation). The amount of redispatching depends heavily on the N-1 security criterion.

406 6. Conclusions

407 This paper discusses redispatching as tool for congestion management in interconnected electricity
 408 systems with a high penetration of renewables. The Belgian electricity system is studied as a case
 409 study. The Belgian system is embedded in the European electricity system and faces grid congestion
 410 issues due to the deployment of offshore wind without a strong grid connection between the shore and
 411 the main load centers inland. Based on the results presented in this paper, three conclusions can be
 412 drawn.

413 First, it is shown that loop flows can have a considerable impact on redispatching. Loop flows are
 414 unintended power flows through a bidding zone, caused by injections and withdrawals outside the
 415 bidding zone. In the case study, redispatch quantities and costs increase with more than a factor 2
 416 at high loop flows. Loop flows are relevant in a highly interconnected electricity system such as the
 417 European system. One can conclude that the impact of loop flows is too large to neglect and should
 418 therefore be considered, in particular in a highly interconnected power system.

419 Second, redispatch amounts and costs can increase drastically when additional (renewable) generation
 420 is added to congested areas. In the case study, the increase in redispatching amounts and costs with
 421 increasing offshore wind capacity is very steep. One can conclude that transmission grid constraints
 422 restrict the deployment of renewables in certain areas, once grid congestions start to occur.

423 Third, it is shown that the stringency of the N-1 security criterion imposed to the system has a large
424 impact. In the case study, redispatch costs are a factor 8 higher if a preventive N-1 security criterion is
425 imposed, compared to a curative N-1 security criterion. One can conclude that relaxing the stringency
426 of the N-1 security criterion, i.e., going from preventive to curative N-1 security, can reduce redispatch
427 costs drastically.

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