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In-beam γ -ray spectroscopy of 35 Mg and 33 Na

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Excited states in the very neutron-rich nuclei 35 Mg and 33 Na were populated in the fragmentation of a 38 Si projectile beam on a Be target at 83 MeV/u beam energy. We report on the first observation of γ -ray transitions in 35 Mg, the odd-N neighbor of 34 Mg and 36 Mg, which are known to be part of the 'island of inversion' around N=20. The results are discussed in the framework of large-scale shell-model calculations. For the A=3Z nucleus 33 Na, a new γ -ray transition was observed that is suggested to complete the γ -ray cascade $7/2^+ \rightarrow 5/2^+ \rightarrow 3/2^+_{gs}$ connecting three neutron two-particle-two-hole intruder states that are predicted to form a close-to-ideal K=3/2 rotational band in the strong-coupling limit.

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I. INTRODUCTION

The structure of nuclei in the so-called "island of inversion" [1,2], a region of the nuclear chart composed of neutron-rich Ne, Na, and Mg isotopes around neutron number N=20, has provided much insight into the driving forces of shell evolution. In this region, driven largely by the spin-isospin parts of the nuclear force [3], neutron *n*-particle–*n*-hole (np-nh) "intruder" configurations of $v(sd)^{-n}(fp)^{+n}$ character (labeled $n\hbar\omega$) gain "correlation energy" [4] with respect to the normal-order configurations and dominate the wave functions of low-lying states, including the ground states, signaling the breakdown of N = 20 as a magic number in these nuclei. The resulting onset of collectivity was quantified with inelastic scattering experiments [5-10] and inferred from measurements of the 2_1^+ excitation energies [11–14] on even-even nuclei out to 32 Ne and 36 Mg at Z = 10 and Z = 12, respectively. These collective properties of even-even nuclei are rather well described by state-of-the-art Monte Carlo shell model (MCSM) calculations (SDPF-M effective interaction) that allow for unrestricted mixing of neutron particle-hole configurations across the N=20 shell gap. However, experimental information on their odd-N neighbors, ^{31,33}Mg [15–22] and ³⁰Na [23], for example, has posed significant challenges for these calculations and led to controversial interpretations, indicating that odd-A and odd-odd nuclei pose very stringent benchmarks for a shell-model description of this region.

In this paper we present results from the first γ -ray spectroscopy of $^{35}_{12}{\rm Mg}_{23}$ and report a new γ -ray transition observed in the A/Z=3 nucleus $^{33}{\rm Na}$ (N=22). Excited

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states in these very neutron-rich nuclei were populated in the fragmentation of an intermediate-energy ³⁸Si rare-isotope beam on a ⁹Be target. The results are confronted with large-scale shell-model calculations.

II. EXPERIMENT

The ³⁸Si secondary beam was produced by fragmentation of 140 MeV/nucleon ⁴⁸Ca primary beam delivered by the Coupled Cyclotron Facility of the National Superconducting Cyclotron Laboratory onto a 752 mg/cm² primary ⁹Be fragmentation target. The isotope of interest was selected in the A1900 fragment separator [25], using a 750 mg/cm² Al wedge degrader for purification. The ³⁸Si secondary beam interacted with a 376(4)-mg/cm²-thick ⁹Be reaction target positioned at the pivot point of the large-acceptance S800 spectrograph [26]. The reaction residues were identified on an event-by-event basis from the time of flight taken between two scintillators and the energy loss measured in the S800 ionization chamber. The flight times were corrected for the reaction residue's trajectories as reconstructed from the position and angle information provided by the cathode-readout drift chambers of the S800 focal-plane detector system. The particle identification spectrum for the reaction residues produced in ${}^{9}\text{Be}({}^{38}\text{Si}, {}^{A}Z)X$ is shown in Fig. 1.

Since the measurement's main focus was the study of ^{36}Mg in the two-proton knockout from ^{38}Si [13,27,28], the magnetic rigidity of the S800 spectrograph was set to center the longitudinal momentum distribution of ^{36}Mg in the S800 focal plane. Therefore, ^{35}Mg and ^{33}Na entered the focal plane off center and were impacted by acceptance cuts (estimated to be of the order of 20%–30%). The cross sections for the production of these nuclei from ^{38}Si were measured to be $\sigma(^{36}\text{Mg})=0.10(1)$ mb [13], $\sigma(^{35}\text{Mg})\gtrsim0.05$ mb, and $\sigma(^{33}\text{Na})\gtrsim0.03$ mb.

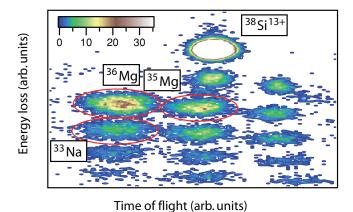


FIG. 1. (Color online) Identification spectrum for the reaction residues produced in ${}^9\mathrm{Be}({}^{38}\mathrm{Si},{}^AZ)X$ at 83 MeV/u midtarget energy. All reaction residues can be unambiguously identified by plotting the energy loss measured in the S800 ionization chamber vs the ion's time of flight. The magnetic rigidity of the S800 spectrograph was set to center ${}^{36}\mathrm{Mg}$ in the focal plane (see Ref. [13]). The H-like charge state of the projectile beam, produced by electron pickup of the originally fully stripped ${}^{38}\mathrm{Si}$ passing through the reaction target, is the most intense constituent of the reacted beam.

The secondary $^9\mathrm{Be}$ target was surrounded by SeGA, an array of 32-fold segmented high-purity germanium detectors [29]. The high degree of segmentation was used to event-by-event Doppler reconstruct the γ rays emitted by the reaction residues in flight. For this, the location of the segment that registered the largest energy deposition determines the γ -ray emission angle relative to the target position. Sixteen detectors were arranged in two rings (at 90° and 37° central angles with respect to the beam axis). The 37° ring was equipped with seven detectors, while nine detectors occupied positions at 90° . The array was calibrated for energy and efficiency with $^{152}\mathrm{Eu}$ and $^{226}\mathrm{Ra}$ calibration standards.

III. RESULTS

Figure 2 shows the Doppler-reconstructed γ -ray spectra measured in coincidence with $^{35}{\rm Mg}$ and $^{33}{\rm Na}$, respectively. In the following sections we discuss the experimental results in comparison to Monte Carlo shell-model calculations using the SDPF-M effective interaction [24] that allows for unrestricted mixing of neutron particle-hole configurations across the N=20 gap and to large-scale shell-model calculations with the SDPF-U effective interaction [30] that does not include neutron intruder configurations in the model space.

A. 35Mg

For 35 Mg, a γ -ray transition at 446 keV is clearly visible, and there are possibly indications of two other transitions at 621 and 670 keV. There is no evidence for γ -ray peaks at higher energies; in fact, the spectrum has remarkably few counts beyond 700 keV, likely indicative of a low neutron separation energy $[S_n]^{35}$ Mg) = 1020(200) keV reported in Ref. [31] and

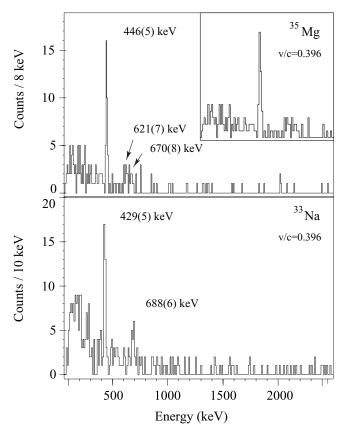


FIG. 2. (top) Doppler-reconstructed γ -ray spectrum in coincidence with 35 Mg reaction residues. (bottom) Gamma-ray spectrum in coincidence with 33 Na.

 $S_n(^{35}\text{Mg}) = 730(460)$ keV estimated in the compilation by G. Audi *et al.* [32]].

With its even-even neighbors ³⁴Mg and ³⁶Mg shown to be part of the island of inversion, one expects neutron particlehole intruder excitations to dominate the structure of ³⁵Mg as well. The Monte Carlo shell-model calculation with the SDPF-M effective interaction predicts eight excited states below 1.2 MeV, with a $5/2^-$ ground state almost degenerate with the first 3/2⁻ level at 30-keV excitation energy (see Figure 3 and Table I). The 446-keV transition observed in the experiment could correspond to the decay of any of the excited $7/2_1^-$, $3/2^{+}$, $1/2^{-}$, or $7/2^{-}$ states between 350 and 560 keV to either the ground state or the low-lying excited state predicted by theory. We note that it was impossible for the measurement presented here to detect a γ -ray transition below $\sim 80 \text{ keV}$ due to the energy threshold settings of the SeGA electronics for this run. Assuming that the neutron separation energy is, indeed, low for ³⁵Mg, the possible transitions at 621 and 670 keV likely proceed to one or both of the $5/2^{-}_{1}$ or $3/2_1^-$ near-degenerate states. It might be possible that the two transitions originate from the same level and that their energy difference of 49(11) keV corresponds to the energy spacing of the alleged $3/2^--5/2^-$ doublet near the ground state. The possible scenarios of a decay level scheme are summarized in Fig. 3, assuming that the tentatively proposed 621- and 670-keV transitions are not feeding each other based on the assumption of a low neutron separation energy.

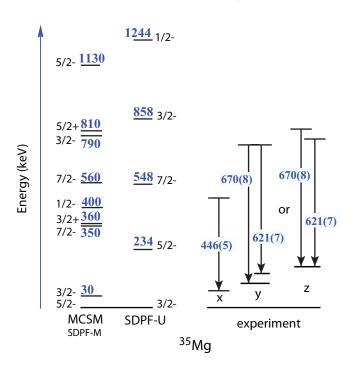


FIG. 3. (Color online) (right) Excited states below 1.2-MeV excitation energy predicted by the two shell-model calculations. (left) Possible arrangement of the experimentally observed transitions in the decay scheme of ³⁵Mg. A low-lying excited state below 80 keV could not have been detected with the threshold setting of the SeGA array.

The reaction process leading to ³⁵Mg from ³⁸Si will not predominantly proceed as the *direct* removal of two protons and a neutron from ³⁸Si but is likely dominated by the two-proton knockout into the continuum of ³⁶Mg and subsequent neutron emission. Therefore, one cannot expect the final-state and nuclear structure selectivity of a strictly direct reaction and would rather expect all bound low-lying states to be

TABLE I. Composition of the 35 Mg wave functions with respect to $n\hbar\omega$ probabilities calculated within the MCSM. Only excited states with $E_x \leqslant 1.29$ MeV are listed.

J^+	E	$1\hbar\omega$	$3\hbar\omega$	5ħω
	(MeV)	(%)	(%)	(%)
3/2+	0.36	96.5	3.5	0.0
$5/2^{+}$	0.81	97.1	2.9	0.0
7/2+	1.29	97.4	2.5	0.0
J^-	E	0ħω	2ħω	4ħω
	(MeV)	(%)	(%)	(%)
1/2-	0.40	1.7	97.8	0.4
$3/2^{-}$	0.03	6.9	92.5	0.6
	0.79	56.1	43.5	0.4
5/2-	0.00	4.6	94.9	0.5
•	1.13	10.1	89.6	0.4
$7/2^{-}$	0.35	12.4	87.0	0.6
•	0.56	4.7	94.6	0.7
$9/2^{-}$	1.22	7.8	91.8	0.4

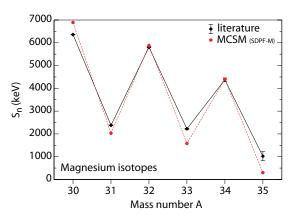


FIG. 4. (Color online) Neutron separation energies S_n for neutron-rich magnesium isotopes from the literature (A = 30-33 taken from Ref. [32]; A = 34, 35 based on the mass excess reported in Ref. [31]) compared to the MCSM (SDPF-M) calculations. The overestimated odd-even staggering supports the assumption that pairing effects are overestimated, leading to an underestimation of S_n for the odd-A isotopes by several hundred keV.

populated without preference for certain configurations. This consideration together with the predicted high-level density in the MCSM and the exceptionally clean γ -ray spectrum, showing evidence for at most three γ -ray transitions, suggests that the neutron separation energy of ³⁵Mg is, indeed, low, likely at the lower end of $S_n = 1020(200)$ keV, and that the γ -ray transitions we observe are not in coincidence and depopulate excited states at ≈ 500 and ≈ 700 keV to the ground state or the alleged near-degenerate excited state below 100-keV excitation energy (this corresponds to the scenario in Fig. 3 with $x \leq 80$ keV and y = 0 keV or $z \leq 80$ keV).

The neutron-separation energy predicted in the MCSM calculation is too low with $S_n \approx 300$ keV. This is likely related to the pairing matrix elements in the interaction as evidenced by an overestimation of the odd-even staggering in the calculation of S_n in the magnesium isotopes (see Fig. 4).

Table I gives the $n\hbar\omega$ decomposition of the wave functions of all negative and positive-parity states at energies $E_x \leq 1.29$ MeV calculated with the MCSM. We note that the first state, with $J^{\pi}=3/2^-$, that is dominated (56%) by $0\hbar\omega$ (nonintruder) configurations occurs at 790-keV excitation energy. All other states calculated in the MCSM in this energy window are almost pure intruder states with $1\hbar\omega$ (positive-parity states) or $2\hbar\omega$ (negative-parity states) neutron intruder configurations.

For comparison, the conventional shell-model calculations with the SDPF-U effective interaction predict only four excited states with $J^{\pi}=5/2^-,7/2^-,3/2^-,$ and $1/2^-$ on top of a $3/2^-$ ground state.

B. ³³Na

The γ -ray spectrum taken in coincidence with ³³Na shows two clear full-energy peaks that correspond to γ -ray transitions at 429(5) and 688(6) keV in the most neutron-rich Na isotope (A=3Z) studied with γ -ray spectroscopy to date. A pioneering experiment at the Radioactive Ion Beam Factory (RIBF) at RIKEN populated one excited state at 467(13) keV

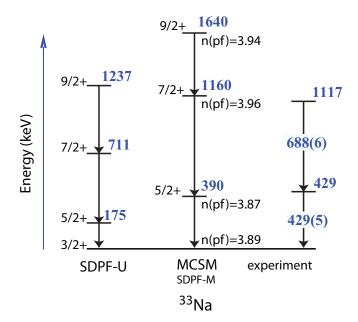


FIG. 5. (Color online) Level schemes of 33 Na as calculated in the shell model (left) compared to the measured γ -ray transitions. Assuming that the observed 429- and 688-keV transitions are in coincidence, the experimental level scheme agrees very well with the MCSM using the SDPF-M effective interaction.

in ³³Na with C-induced inelastic scattering and one-neutron removal [33]. We assume that this is the same γ -ray transition observed by us, noting that the authors of Ref. [33] obtained their value from combining two very different energies of 476(12) and 447(13) keV originating from their two different measurements, with the lower energy closer to the value reported by us. In agreement with Ref. [33] and the systematics presented therein, we propose that the 429(6)-keV ν -ray transition proceeds from the first excited state to the ground state. The MCSM calculations with the SDPF-M effective interaction predict the first excited state in 33 Na, with $J^{\pi} =$ $5/2^+$, at 390 keV on top of a $3/2^+$ ground state, in good agreement with the measurement (see Fig. 5). The calculated second excited state, with $J^{\pi} = 7/2^{+}$ at $E_{x} = 1.16$ MeV, is in good agreement with the data as well when assuming that the γ -ray transition measured at 688 keV depopulates the $7/2^+$ state and feeds the first excited $5/2^+$ state. In the MCSM, the neutron occupation numbers for the pf shell, given in Fig. 5, are close to n(pf) = 4, indicating that all states shown in the calculated level scheme are intruder states with $2\hbar\omega$ neutron configurations relative to two neutrons occupying the pf shell in normal-order filling.

From the systematic studies of the onset of intruder configurations and quadrupole collectivity in the chain of Na isotopes approaching N=20 [34], the question arises how quadrupole collectivity and deformation evolve for more neutron-rich isotopes beyond N=20. For this, the quadrupole moments and B(E2) transition strengths for the $3/2^+$, $5/3^+$, and $7/2^+$ states in ³³Na were calculated with the MCSM using $e_p=1.3e$ and $e_n=0.5e$ effective charges (Table II). From the experimental transition energies and the calculated $B(E2;7/2^+ \rightarrow 3/2^+)=67.5$ e^2 fm⁴, $B(E2;7/2^+ \rightarrow 3/2^+)=67.5$

TABLE II. Quadrupole moments, E2 transition strengths, and extracted intrinsic quadrupole moments Q_0 for the $3/2^+$, $5/2^+$, and $7/2^+$ lowest-lying states in 33 Na calculated with the MCSM (SDPF-M with proton and neutron effective charges of $e_p=1.3e$ and $e_n=0.5e$). Q_0 was deduced assuming that this is a K=3/2 rotational band within the strong-coupling limit. With this assumption, the quadrupole moments and transition strengths in this band are very well described with a common intrinsic quadrupole moment of $Q_0 \sim 70$ fm², indicating that this structure in 33 Na is, indeed, a rather well-deformed K=3/2 rotational band within the MCSM calculation.

J	Q (fm²)	Q_0 (fm ²)
3/2+	+14.3	72
5/2+	-4.3	60
7/2+	-14.6	73
$J_i o J_f$	$B(E2)$ $(e^2 \text{ fm}^4)$	$ Q_0 \ (\mathrm{fm}^2)$
$3/2^+ \to 5/2^+$	263	72
$3/2^+ \rightarrow 7/2^+$	135	69
$5/2^+ \to 7/2^+$	133	68

 $5/2^+)=99.75~e^2~{\rm fm}^4$ values together with the predicted rather strong $B(M1;7/2^+\to 5/2^+)=0.59~\mu_N^2$ reduced M1transition probability, the γ -ray branch for the decay to the ground state is estimated to be only 4.2% of the γ -decay branch to the $5/2^+$ state, which is below the sensitivity limit of our measurement due to low statistics. Assuming that these states form a rotational band with K = 3/2 in the strong-coupling limit, the intrinsic quadrupole moments Q_0 were deduced. As shown in Table II, all quadrupole moments and B(E2) values are well described with a common $Q_0 \sim 70 \, \mathrm{fm^2}$. This indicates that in the MCSM calculation this structure is close to the ideal case of a well-deformed K = 3/2rotational band in the strong coupling limit. This is further supported by the excitation energies; the ratio of the energy differences $E(7/2^+) - E(3/2^+)$ and $E(5/2^+) - E(3/2^+)$ in an ideal K = 3/2 rotational band is expected to be 2.4, while the measured energies in ³³Na give a very similar ratio of 2.6. For comparison, the same energy ratio in ³¹Na [33] gives 3.1, indicating that the low-lying states in Na at N=22 are closer to an ideal K = 3/2 rotational band than at N = 20.

To put the predicted deformation into perspective, for the N=22 isotone $^{34}{\rm Mg}$, the MCSM calculates $B(E2;0^+\to 2_1^+)=552~e^2~{\rm fm}^4$ (in agreement with experiment [7,9]) and $Q(2_1^+)=-21.4~{\rm fm}^2$, yielding an intrinsic quadrupole moment of $Q_0=75~{\rm fm}^2$, which is very similar to $^{33}{\rm Na}$. At N=20, $^{32}{\rm Mg}$, the calculated $B(E2;0^+\to 2_1^+)=447~e^2~{\rm fm}^4$ (in agreement with experiment [5–7,9]) and $Q(2_1^+)=-17.1~{\rm fm}^2$ lead to $|Q_0|=67~{\rm fm}^2$ and $60~{\rm fm}^2$, respectively, with the small discrepancy potentially indicative of triaxiality or γ softness.

The level scheme predicted by the conventional shell-model calculations based on the SDPF-U effective interaction, which does not allow for neutron intruder configurations, has the levels in the same order but predicts the $5/2^+$ first excited state to be within 175 keV of the $3/2^+$ ground state (see Fig. 5).

A strong γ -ray transition above 90–100 keV would have been observed in the present measurement.

IV. SUMMARY

In summary, in-beam γ -ray spectroscopy of the very neutron-rich nuclei 35 Mg and 33 Na was performed following the fragmentation of a 38 Si projectile beam on a 9 Be target at intermediate beam energy. In 35 Mg, the odd-N neighbor of the island of inversion nuclei 34 Mg and 36 Mg, γ -ray transitions were measured and provided first information on excited states in this nucleus. In comparison to Monte Carlo shell-model calculations with the SDPF-M effective interaction, the transitions are interpreted as connecting excited states around \sim 450 and \sim 700 keV to the $5/2^-$ ground state and/or the first excited $3/2^-$ state that is predicted to be within 30 keV of the ground state. For the N=2Z nucleus 33 Na, the most neutron-rich Na isotope studied to date with γ -ray spectroscopy, a new γ -ray transition at 688(6) keV was measured in addition to the known transition at 429(5) keV. The

two transitions, if in coincidence, are in very good agreement with MCSM calculations and are proposed to establish the $7/2^+ \rightarrow 5/2^+ \rightarrow 3/2^+_{gs}$ cascade of the ground-state band in 33 Na, predicted in the MCSM to be an almost-ideal K=3/2 rotational band structure (of intruder states) in the strong-coupling limit. Coulomb excitation or excited-state lifetime measurements are needed to confirm the degree of deformation and rotational character and remain a challenge for future experiments. All low-lying states in these two nuclei are predicted to be intruder states, putting 35 Mg and 33 Na inside the island of inversion.

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