# Optimizing agents with genetic programming An evaluation of hyper-heuristics in dynamic real-time logistics

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Abstract Dynamic pickup and delivery problems (PDPs) require online algorithms for managing a fleet of vehicles. Generally, vehicles can be managed either centrally or decentrally. A common way to coordinate agents decentrally is to use the contract-net protocol (CNET) that uses auctions to allocate tasks among agents. To participate in an auction, agents require a method that estimates the value of a task. Typically, this method involves an optimization algorithm, e.g. to calculate the cost to insert a customer. Recently, hyper-heuristics have been proposed for automated design of heuristics. Two properties of automatically designed heuristics are particularly promising: 1) a generated heuristic computes quickly, it is expected therefore that hyper-heuristics perform especially well for urgent problems, and 2) by using simulation-based evaluation, hyper-heuristics can create a 'rule of thumb' that anticipates situations in the future. In the present paper we empirically evaluate whether hyper-heuristics, more specifically genetic programming (GP), can be used to improve agents decentrally coordinated via CNET. We compare several GP settings and compare the resulting heuristic with existing centralized and decentralized algorithms based on the OptaPlanner optimization library. The tests are conducted in real-time on a dynamic PDP dataset with varying levels of dynamism, urgency, and scale. The results indicate that the evolved heuristic always outperforms the optimization algorithm in the decentralized multi-agent system (MAS) and often outperforms the centralized optimization algorithm. Our paper demonstrates that designing MASs using genetic programming is an effective way to obtain competitive performance compared to

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traditional operational research approaches. These results strengthen the relevance of decentralized agent based approaches in dynamic logistics.

Keywords Hyper-heuristics · Genetic programming · Multi-agent systems · Logistics · Decentralized · Centralized · Operational research · Optimization · Real-time

#### <span id="page-1-0"></span>1 Introduction

The pickup and delivery problem (PDP) is a logistics problem where a fleet of vehicles transports customers or goods from origin to destination [\[1\]](#page-24-0). The dynamic pickup and delivery problem with time windows (PDPTW) is an online variant where some or all customers' orders arrive during the operating hours and where customers impose time window constraints on pickups and deliveries [\[2\]](#page-24-1). Typically, the objective in PDPTW is to serve all customers while minimizing fuel costs and time window violations. In a purely dynamic PDPTW, no order is known before the operating hours. When a new order is announced, the available computation time for an algorithm is limited by the order's urgency, the amount of available time until the order needs to be serviced [\[3\]](#page-24-2). Together, the dynamism, urgency, and scale of a problem, directly affect the amount of computations that need to be done as well as how much time is available for performing them [\[4\]](#page-25-0).

Decentralized multi-agent systems (MASs) are commonly considered to be a good fit for large scale and dynamic problems because of their ability to make quick local decisions [\[5–](#page-25-1)[8\]](#page-25-2). Together, the local decisions made by all agents aim to solve the global optimization problem. There are two different approaches for making these decisions: 1) explicitly searching through the space of possible schedules using an (exact or heuristic) optimization procedure, or, 2) using a heuristic, a rule of thumb, that guides the agent by assigning priorities to actions without explicitly searching the space of schedules. The aim of the present paper is to compare the performance of these two different approaches. For the first approach we use a tabu search algorithm from the OptaPlanner [\[9\]](#page-25-3) optimization library. For the second approach we use genetic programming to automatically design an agent-based heuristic.

#### 1.1 Related work

A recent empirical study by van Lon and Holvoet [\[8\]](#page-25-2) employs a MAS with an auction based contract-net protocol (CNET). The agents place bids to the customer indicating the estimated additional cost to perform the transportation task. Each agent computes this bid value by running an optimization procedure for a limited time. The experiments indicate that the MAS only outperforms a reference centralized algorithm in case the problem is medium to very dynamic, very urgent, and medium to large scale. A problem instance with these properties is changing continuously (medium to very dynamic), vehicles have a short amount of time to respond to incoming requests (very urgent), and there are relatively many vehicles and orders (medium to large scale). In this situation the computational demands are very high, limiting the viability of searching the solution space centrally. The CNET approach, however, uses implicit partitioning of the search space, apparently this helps in these circumstances to find a good solution in a short period. Since the paper by van Lon and Holvoet [\[8\]](#page-25-2) considers purely dynamic PDPTWs, we know that the problem is likely to change soon after a bid value is computed. A reasonable assumption is therefore that a good bid value should incorporate expected future events that affect the transportation cost of an order. However, in the setup of that paper, the optimization algorithm, OptaPlanner [\[9\]](#page-25-3), only considers all information that is known up to the moment of computation. An alternative for the optimization procedure is a heuristic that may include estimates of future events. Designing such a heuristic is, however, a difficult task. A local decision made by an agent can have far reaching global consequences. That is because a collection of agents acting according to decentralized local rules constitutes a complex system with emergent and difficult to predict behavior.

Research on dynamic optimization problems, such as dynamic PDPTWs, is concerned with optimization in an environment that changes over time [\[10\]](#page-25-4). Dynamic optimization problems are often approached using metaheuristics [\[11,](#page-25-5) [12\]](#page-25-6). Metaheuristics, such as swarm intelligence and evolutionary computation, are a good fit for these dynamic problems because they are inspired on natural processes, which themselves are subject to a continuously changing environment. In present paper, instead of using evolutionary algorithms to solve our problem directly, we use genetic programming to generate a heuristic that solves our problem.

Hyper-heuristics is a branch of optimization literature concerned with the automatic design of heuristics [\[13\]](#page-25-7). Burke et al. [\[14\]](#page-25-8) distinguishes two different categories of hyper-heuristics, heuristic selection and heuristic generation. Heuristic selection comprises methodologies for choosing or selecting existing heuristics while heuristic generation is concerned with generating new heuristics from components of existing heuristics. Genetic programming (GP) is a subfield of evolutionary computing [\[15\]](#page-25-9), that works with variable size LISP-tree representations and thus is able to evolve functions of arbitrary complexity, making it particularly suitable for the design of heuristics. Hyper-heuristics and GP in particular, have been applied in a wide range of contexts, including production scheduling [\[16\]](#page-25-10), traveling salesman problems [\[17\]](#page-26-0), bin packing [\[18\]](#page-26-1), etc.

The combination of hyper-heuristics and MAS for dynamic PDPTW has been explored before. To the best of our knowledge, Beham et al. [\[19\]](#page-26-2) were the first to apply hyper-heuristics to an agent-based algorithm for the PDPTW. In their MAS, vehicle agents are governed by two separate heuristics, one heuristic determines its next location to travel to and another heuristic determines the order(s) to pick up at a pickup site. Both heuristics are weighted sums of hand-crafted heuristics, the weights are set by an evolution strategy (ES). Determining the quality of the heuristics during evolution is done with a simulation-based fitness function. Beham et al. [\[19\]](#page-26-2) did not compare their approach with alternative algorithms.

Similarly, van Lon et al. [\[20\]](#page-26-3) used GP to evolve the guiding heuristic for a MAS in a dynamic PDPTW context. Vehicles have a capacity of one order, implying that a vehicle must immediately go to an order's destination after pick up. The evolved heuristic assigns priorities to all available orders. Each vehicle that is not currently carrying an order executes its heuristic frequently, and travels to the order with the highest priority. The agents do not communicate amongst each other, leading to inefficiencies in case several vehicles have the same priority. Because the problem is dynamic, priorities of vehicles change, causing vehicles to divert from their route. In their paper, [van Lon et al.](#page-26-3) show that their MAS approach with an evolved heuristic outperforms a centralized meta-heuristic.

The work by Vonolfen et al. [\[21\]](#page-26-4) extends [\[20\]](#page-26-3). Instead of using just three terminals in GP as was done in [\[20\]](#page-26-3), [Vonolfen et al.](#page-26-4) use 18 different terminals. This includes several terminals that incorporate information about other agents' distances and destinations. The authors compare their approach with two algorithms, a (centralized) tabu search algorithm and the evolution strategy presented in [\[19\]](#page-26-2). [Vonolfen et al.](#page-26-4) report that the tabu search algorithm outperforms both the GP as well as the ES approach, while GP outperforms ES.

Continuing in this line of research, Merlevede et al. [\[22\]](#page-26-5) use neuroevolution of augmenting topologies (NEAT) to evolve a neural network as a priority heuristic. The authors use the same MAS approach as in [\[20\]](#page-26-3) but they evaluate their performance on an existing dynamic PDPTW benchmark. They are the first to report negative results, the reference centralized algorithm always outperforms the NEAT approach. These results are likely caused by the lack of a coordinating mechanism for their MAS.

# 1.2 Contributions and overview

The papers described above that apply hyper-heuristics to MAS for dynamic PDPTW have several drawbacks which we aim to overcome in present paper. First, the discussed hyper-heuristics have not been evaluated in real-time. In a dynamic logistics problem, algorithm computation time directly affects the performance of the fleet of vehicles. Therefore, when comparing hyper-heuristics to traditional optimization algorithms in dynamic PDPTW, a real-time simulator is required. Second, for a fair comparison of two different algorithms, it is important that both algorithms are subject to exactly the same constraints. When comparing hyper-heuristics in a MAS setting, a fair comparison is to have a reference algorithm that is also used in a MAS setting. Unfortunately, none of the above described works evaluate their agent-based hyper-heuristic in this way. Third, to understand the exact circumstances in which one algorithm outperforms another, it is imperative to vary the problem properties on which they are evaluated. Fourth, to allow reproducibility and extensibility, the algorithms, datasets, and software that are used should be freely available.

The aim of present paper is to determine whether using hyper-heuristics can improve the performance of an existing MAS for a real-time logistics problem. More specifically, we are investigating two hypotheses comparing a hyper-heuristic setup with the centralized OptaPlanner algorithm and the decentralized MAS both from  $[8]$ :

- GP designed heuristic in a MAS can outperform OptaPlanner in a MAS.
- GP designed heuristic in a MAS can outperform centralized OptaPlanner.

If these hypotheses are true, it would demonstrate the relevance of decentralized MASs in dynamic logistics and constitute an important first step towards their automatic design. Since a heuristic typically requires only a fraction of the computation time that a solver requires, we also investigate the following hypothesis:

– GP designed heuristic works especially well for more urgent problems because of its minimal computational cost.

Using the dataset and dataset generator from [\[4\]](#page-25-0) we can train and test the heuristics on instances with different values of dynamism, urgency, and scale. We define a specialized heuristic as a heuristic that is trained on one specific scenario setting with specific properties, as opposed to a generalized heuristic that is trained on a wide range of scenario settings. We expect that:

- Specialized heuristics outperform general heuristics on scenarios for which they are specialized.
- Generalized heuristics outperform specialized heuristics on scenarios for which they are not specialized.

The paper is organized as follows. A formal problem definition, including dynamism, urgency, and scale, and the real-time simulation platform are presented (Section [2\)](#page-4-0). The MAS that we start from is presented in Section [3.](#page-8-0) The paper presents the following contributions:

- a new application of hyper-heuristics to decentralized MAS using GP is presented (Section [4\)](#page-11-0);
- the performance of GP and the resulting heuristics are thoroughly evaluated using real-time simulation and compared to existing results obtained by a centralized and a decentralized OptaPlanner algorithm under varying circumstances (Section [5\)](#page-15-0);
- following [\[8\]](#page-25-2), all code, data, and results needed to reproduce this work are made available online.

Finally, we summarize the paper and discuss directions for future research (Section [6\)](#page-23-0).

# <span id="page-4-0"></span>2 Dynamic pickup-and-delivery problems

This section is adapted from [\[4,](#page-25-0) [8\]](#page-25-2). In PDPs there is a fleet of vehicles responsible for the pickup-and-delivery of items. Dynamic PDP is an online problem. Customer transportation requests are revealed over time, during the fleet's operating hours. It is further assumed that the fleet of vehicles has no prior knowledge about the total number of requests nor about their locations or time windows. In this section, we provide an overview of the work about dynamic PDP from [\[4,](#page-25-0) [8\]](#page-25-2) as it serves as a foundation of the evaluation in present paper.

# 2.1 Formal definition

In [\[4\]](#page-25-0) a scenario, which describes the unfolding of a dynamic PDP, is defined as a tuple:

$$
\langle \mathcal{T}, \mathcal{E}, \mathcal{V} \rangle := \text{scenario},
$$

where



 $[0, \mathcal{T})$  is the period in which the fleet of vehicles V has to respond to customer requests. The events,  $\mathcal{E}$ , represent customer transportation requests. Since we consider the purely dynamic PDPTW, all events are revealed between time 0 and time  $\mathcal{T}$ . Each event  $e_i \in \mathcal{E}$  is defined by the following variables:

> $a_i := \text{announce time}$  $p_i := [p_i^L, p_i^R) =$  pickup time window,  $p_i^L < p_i^R$  $d_i := [d_i^L, d_i^R) =$  delivery time window,  $d_i^L < d_i^R$  $pst_i := \text{pickup service time span}$  $dst_i :=$  delivery service time span  $ploc_i := \text{pickup location}$  $dloc_i :=$  delivery location

Reaction time is defined as:

$$
r_i := p_i^R - a_i = \text{reaction time} \tag{1}
$$

The time window related variables of a transportation request are visualized in Figure [1.](#page-5-0)

<span id="page-5-0"></span>

Fig. 1: Visualization of the time related variables of a single order event  $e_i \in \mathcal{E}$ .

Furthermore it is assumed that:

- vehicles start at a depot and have to return after all orders are handled;
- the fleet of vehicles  $V$  is homogeneous;
- the cargo capacity of vehicles is infinite (e.g. courier service);
- the vehicle is either stationary or driving at a constant speed;
- vehicle diversion is allowed, this means that a vehicle is allowed to divert from its destination at any time;
- vehicle fuel is infinite and driver fatigue is not an issue;
- the scenario is completed when all pickup and deliveries have been made and all vehicles have returned to the depot; and,
- each location can be reached from any other location.

Vehicle schedules are subject to both hard and soft constraints. The opening of time windows is a hard constraint, hence vehicles need to adhere to these:

$$
sp_i \ge p_i^L \tag{2}
$$

$$
sd_i \ge d_i^L \tag{3}
$$

 $sp_i$  is the start of the pickup operation of order event  $e_i$  by a vehicle; similarly,  $sd_i$  is the start of the delivery operation of order event  $e_i$  by a vehicle. The time window closing  $(p_i^R \text{ and } d_i^R)$  is a soft constraint incorporated into the objective function, it needs to be minimized:

<span id="page-6-1"></span>
$$
min := \sum_{j \in V} (vtt_j + td\{bd_j, \mathcal{T}\}) + \sum_{i \in \mathcal{E}} \left(td\left\{sp_i, p_i^R\right\} + td\left\{sd_i, d_i^R\right\}\right) \tag{4}
$$

where

$$
td\{\alpha,\beta\} := \max\{0,\alpha-\beta\} \ = \ \text{tardiness} \tag{5}
$$

 $vtt_j$  is the total travel time of vehicle  $v_j$ ;  $bd_j$  is the time at which vehicle  $v_j$  is back at the depot. In summary, the objective function computes the total vehicle travel time, the tardiness of vehicles returning to the depot and the total pickup and delivery tardiness.

#### 2.2 Dataset

Earlier work has argued for, and presented, a dataset characterized by three different properties of dynamic PDPs: dynamism, urgency, and scale [\[4\]](#page-25-0).

## 2.2.1 Dynamism

Dynamism is defined in van Lon et al. [\[3\]](#page-24-2). Informally, a scenario that changes continuously is said to be dynamic while a scenario that changes occasionally is said to be less dynamic. In the context of PDPTWs a change is an event that introduces additional information to the problem, such as the events in  $\mathcal{E}$ . Formally, the degree of dynamism, or the continuity of change, is defined as:

<span id="page-6-0"></span>
$$
dynamicsm := 1 - \frac{\sum_{i=0}^{|\Delta|} \sigma_i}{\sum_{i=0}^{|\Delta|} \bar{\sigma}_i}
$$
 (6)

 $\Delta$  is the list of event interarrival times:

$$
\Delta := \{ \delta_0, \delta_1, \dots, \delta_{|\mathcal{E}|-2} \} = \{ a_j - a_i | j = i+1 \land \forall a_i, a_j \in \mathcal{E} \}
$$
(7)

For a scenario with 100% dynamism, the perfect interarrival time is defined as:

$$
\theta := \text{perfect interarrival time} = \frac{\mathcal{T}}{|\mathcal{E}|} \tag{8}
$$

(9)

Based on this definition, the deviation and maximum possible deviation to the perfect interarrival time can be computed:

$$
\sigma_i := \begin{cases} \theta - \delta_i & \text{if } i = 0 \text{ and } \delta_i < \theta \\ \theta - \delta_i + \frac{\theta - \delta_i}{\theta} \times \sigma_{i-1} & \text{if } i > 0 \text{ and } \delta_i < \theta \end{cases}
$$

0 otherwise

$$
\bar{\sigma}_i := \theta + \begin{cases} \frac{\theta - \delta_i}{\theta} \times \sigma_{i-1} & \text{if } i > 0 \text{ and } \delta_i < \theta \\ 0 & \text{otherwise} \end{cases} \tag{10}
$$

Eq. [6](#page-6-0) uses the proportion of the actual deviation and the maximum possible deviation. Using this definition the degree of dynamism of any scenario can be computed.

# 2.2.2 Urgency

 $\vert_0$ 

In [\[3\]](#page-24-2) urgency is defined as the maximum reaction time available to the fleet of vehicles in order to respond to an incoming order. Or more formally:

$$
urgency\left(e_i\right) := p_i^R - a_i = r_i \tag{11}
$$

To obtain the urgency of an entire scenario the mean and standard deviation of the urgency of all orders can be computed.

# 2.2.3 Scale

Scale is defined by van Lon and Holvoet [\[4\]](#page-25-0) as maintaining a fixed objective value per order while scaling the number of orders up in proportion to the number of vehicles in the fleet. Scaling up a scenario  $\langle \mathcal{T}, \mathcal{E}, \mathcal{V} \rangle$  with a factor  $\alpha$  will create a new scenario  $\langle \mathcal{T}, \mathcal{E}', \mathcal{V}' \rangle$  where  $|\mathcal{V}'| = |\mathcal{V}| \cdot \alpha$  and  $|\mathcal{E}'| = |\mathcal{E}| \cdot \alpha$ .

### <span id="page-7-0"></span>2.3 Realistic simulation platform

The experiments performed in van Lon and Holvoet [\[8\]](#page-25-2) use the RinSim real-time logistics simulator [\[23\]](#page-26-6). For fair comparison we use the same simulator. RinSim is a discrete-time logistics simulator that supports running both centralized algorithms and decentralized multi-agent systems. RinSim is written in Java and has a modular design (Figure [2\)](#page-8-1), a Model encapsulates a part of a problem domain or algorithm. The simulator can be customized by selecting the models that are used, this allows simulating a wide variety of logistics problems while maximally reusing existing code.

RinSim supports simulations using simulated time as well as real-time. The standard Java virtual machine (JVM) has no built-in support for real-time execution. However, RinSim is designed such that it provides soft real-time behavior using the standard JVM. Soft real-time, as opposed to hard real-time, allows occasional deviations from the desired execution timing.

RinSim discretizes time into intervals called 'ticks'. The simulator is initialized with a fixed tick length, for example a tick length of 250 milliseconds. When

<span id="page-8-1"></span>

Fig. 2: UML component diagram of RinSim. The simulator subsystem can be configured with a variety of models that all provide some interface. MASs, solvers, and the graphical user interface use these interfaces to interact with RinSim.

simulating without real-time constraints, the simulator computes all ticks as fast as possible. In a real-time simulator the interval between the start of two ticks should be the tick length (e.g. 250 ms). Since the JVM doesn't allow precise control over the timings of threads it is generally impossible to guarantee hard realtime constraints. In real-time mode, RinSim uses a dedicated thread for executing the ticks. If computations need to be done that are expected to last longer than a tick, they must be done in a different thread. This minimizes interference of computations with the advancing of time in the simulated world. Additionally, the processor affinity of the threads are set at the operating system level. Setting the processor affinity to a Java thread instructs the operating system to use one processor exclusively for executing that thread. In practice, the actual scheduling of threads on processors depends on the number of available processors and the operating system.

Running a complete logistics simulation in real-time is time consuming, as it will simulate every tick synchronized with real time. However, depending on the specific simulation that is being run, there may be long intervals where no computations are being done other than that of the simulator advancing time in the simulated world. For this reason, RinSim employs a mechanism to dynamically switch between real-time and simulated time. When the simulator is in simulated time, ticks will be executed as fast as possible speeding up the simulation significantly. As soon as a computation needs to be done, the simulator must first switch back to real-time mode before this computation can be started.

# <span id="page-8-0"></span>3 Multi-agent systems for dynamic PDP

This section is adapted from [\[8\]](#page-25-2). The multi-agent system that is extended is an implementation of the dynamic contract-net protocol (DynCNET) presented by Weyns et al. [\[24\]](#page-26-7). DynCNET is a dynamic extension of the CNET first proposed by Smith [\[25\]](#page-26-8). Inspired by how companies use subcontracting to collaboratively solve problems, CNET uses contracting to approach the task assignment problem. In CNET, the agent that tenders a task is called the *manager* and sends a task announcement to potential contractors. Each potential contractor can either ignore the announcement or send a bid to the manager. The manager then selects the best bid and awards the task to the contractor. Figure [3](#page-9-0) shows the UML interaction <span id="page-9-0"></span>diagram for the CNET auction process. Although an auction can be, and usually



Fig. 3: UML interaction diagram of a CNET auction.

is, used in a competitive setting, we use auctions in a purely cooperative setting. We assume that both the contractors and the manager are working for the same company. The dynamic extension of CNET provides flexibility to the assignment until a contractor has to commit to the execution of the task. The same task can be announced several times before its execution, its assignment changing after every announcement.

In our MAS implementation for the dynamic PDPTW, both the vehicle as well as the transportation requests are modeled as agents. In the remainder of this text we will call the agent controlling a vehicle a VehicleAgent and the agent responsible for a transportation request an OrderAgent. OrderAgents are playing the role of the manager in DynCNET, VehicleAgents are the potential contractors. Figure [4](#page-10-0) shows an interaction diagram of an auction using our DynCNET implementation. At the end of an auction, each VehicleAgent is either awarded the order or notified of the end of the auction. At this moment the VehicleAgents have the possibility of starting a new auction by offering one of their previously awarded orders. The VehicleAgent will inform the OrderAgent responsible for the order that is to be offered to start a new auction, the OrderAgent will then perform a new auction process similar to Figure [4.](#page-10-0) A possible outcome of this auction is that the order is not awarded to another vehicle but stays assigned to the original vehicle. Allowing the vehicles to start a new auction process enables the dynamic (re)allocation of orders and makes the CNET implementation dynamic.

#### 3.1 Order agent

The OrderAgent (the manager in CNET terminology) is responsible for the auction process. It announces the start of the auction to all vehicles and waits until it receives enough bids to make a decision. The stop criterion for the bidding process is:

 $|bids| > 2 \land (|bids| = |vehicles| \lor auction\_duration > 5000)$ 

where,  $|bids|$  is the number of received bids,  $|vehicles|$  is the total number of vehicles which equals the potential maximum number of bids and *auction\_duration* is the duration of the auction in milliseconds.

When the stop criterion evaluates to true, the OrderAgent finalizes the auction by selecting the best bid as the winner. The best bid is defined as the bid with the

<span id="page-10-0"></span>

Fig. 4: UML interaction diagram of an auction of an order with two vehicles. Upon receiving the auction announcement, both VehicleAgents start computing a bid. The computations take several ticks. As soon as the OrderAgent has met the stop criterion, in this case receiving two bids is enough, the auction is finalized and the order is awarded to v1. Vehicle v2 is notified of the end of the auction. The RinSim lifeline is a simplified view of the multi-threaded computation facilities provided by RinSim. Note that the filled arrows indicate synchronous calls and the stick arrows indicate asynchronous calls.

lowest price (cost). The order is assigned to the winner, the winner must therefore service that order, unless it decides to auction it and somebody else wins that auction at a later time. All VehicleAgents are informed of the end of the auction. This allows agents that are still computing their bids for this auction to cancel their computations. Bids that are received after the finalization of the auction are ignored.

# 3.2 Vehicle agent

A VehicleAgent needs to compute a bid value in order to propose a bid. In [\[8\]](#page-25-2) the bid value is computed using a solver. The cost of an order is defined as the additional cost that including that order incurs to a vehicle's current schedule:

<span id="page-10-1"></span>
$$
cost(order) = cost(new\_schedule) - cost(current\_schedule)
$$
\n(12)

where, *current\_schedule* is the schedule of the vehicle including all previous order assignments, and new schedule is the current schedule of the vehicle including the proposed order. The task of the solver is finding the best new schedule in a relative short amount of time to get a reliable estimate of the cost of the auctioned order. The time for computing the new schedule is limited because the auction process has a limited duration, the bid needs to be proposed before the end of this duration in order to ensure that the OrderAgent will take the bid into account.

As soon as the assignment of orders to a vehicle has changed, the VehicleAgent needs to update its schedule. The vehicle's schedule is optimized by a solver (the schedule solver), although it is imperative to generate a complete schedule quickly, the solver can compute for a longer time as the solver can continuously notify the VehicleAgent of improved schedules. This allows the optimization process to continue for an extended period.

The VehicleAgent considers starting a new auction (a reauction) in the following two situations:

- when a vehicle has not won an auction for at least five minutes; or,
- when the vehicle's current schedule has changed.

When starting a new auction the vehicle has to decide which of its previously assigned orders it should auction. The order that when removed yields the greatest schedule cost reduction, for that vehicle, is selected. Computing the cost reduction of removing an order from the current route does not require an optimization step (the route is not optimized again) and can therefore be computed quickly for all orders assigned to a vehicle (similar to eq. [12\)](#page-10-1). Orders for which the pickup operation is in process or is already done are not considered for auctioning as they can't be reassigned. If the order with the greatest cost reduction is the last received order, no auction is performed to avoid excessive auctioning. The VehicleAgent itself has to propose a bid to its own auction, only when another agent proposes a better bid will the order be reassigned.

In [\[8\]](#page-25-2) computations by the agents are done using an optimization algorithm from the OptaPlanner library [\[9\]](#page-25-3). OptaPlanner is an open source Java constraint satisfaction engine that optimizes planning problems. The project is developed by [De Smet et al.](#page-25-3) and sponsored by RedHat. OptaPlanner provides a wide range of optimization algorithms such as construction heuristics and metaheuristics. It has support for various problem domains such as scheduling and vehicle routing. In the experiments described in this paper we use version 6.4.0. In [\[8\]](#page-25-2) it was established that a first-fit decreasing construction heuristic followed by step counting hill climbing with tabu search and strategic oscillation performs best on dynamic PDPTWs. Therefore we use the same algorithm in this paper. In the remainder of this paper, when we refer to OptaPlanner we refer to this specific algorithm unless mentioned otherwise.

# <span id="page-11-0"></span>4 Genetic programming for enhancing agents

To enhance the MAS discussed in Section [3](#page-8-0) using GP we replaced OptaPlanner in the VehicleAgent with an evolved heuristic.

#### 4.1 Heuristics in agents

As described in Section [3,](#page-8-0) the VehicleAgent has three different decisions to make:

- 1. Assigning a bid value to an auctioned parcel, currently being done using cheapest insertion cost with the insertion computed by OptaPlanner.
- 2. Deciding what parcel to reauction, currently taking the most expensive parcel.
- 3. Finding the cheapest route to all destinations, currently computed using Opta-Planner.

Assigning a bid value to a parcel (1) and deciding which parcel to reauction (2) can easily be done by a heuristic:

(vehicle,parcel) -> cost

The heuristic is executed by a vehicle, the output is an estimation of the cost of adding the specified parcel into the route of the vehicle and possibly further considerations.

#### 4.2 Genetic programming setup

Since the quality of a heuristic cannot be deduced analytically, we are using simulation-based fitness evaluation. Since real-time simulation is very time consuming, we are using RinSim (Section [2.3\)](#page-7-0) with simulated time during evolution. Additionally, to also save computation time, we use the cheapest insertion cost heuristic instead of OptaPlanner for computing the cheapest route to all destinations. To avoid spending too much time on simulating inferior individuals we use RinSim with a custom stop condition:

$$
stop(t) := \begin{cases} \exists v_i \in \mathcal{V} \text{ route-length}(v_i) > \max(40, |\mathcal{E}_t| - |\mathcal{D}_t|) & \text{if } t \le 8 \text{ hours} \\ \text{true} & \text{otherwise} \end{cases}
$$

where t is the current time,  $|\mathcal{E}_t|$  is the number of parcel announce events up to time t, and  $|\mathcal{D}_t|$  is the number of delivered parcels up to time t. The stop condition is designed to stop the simulation if it takes too long to deliver all parcels or if there is a single vehicle that is hoarding parcels. Hoarding is defined as a vehicle that has more than about 50% of all possible visits in its route. The theoretical maximum number of visits is indicated by  $2 \cdot |\mathcal{E}_t| - |\mathcal{D}_t|$ . A vehicle route may contain each parcel at most twice (once for pickup, once for delivery), if the route length is larger than the number of undelivered parcels this means that about 50% of the parcels are in that route. The stop condition only applies when the total route length is more than 40. The stop condition halts simulations of bad quality individuals, saving computation time for individuals of higher quality.

The fitness function, that needs to be minimized, is:

fitness := 
$$
\begin{cases} \text{fitness}^{\max} - t & \text{if simulation terminated early} \\ \text{cost (eq. 4)} & \text{otherwise} \end{cases}
$$

The fitness of individuals that are stopped by the stop condition is the maximum fitness value subtracted with the time of the simulator at which it was stopped. This adds some differentiation to low quality individuals.

The GP settings that we use are listed in Table [1.](#page-13-0) The best number of evaluations is highly problem specific [\[16\]](#page-25-10). The choice of number of evaluations per individual needs to be high enough to avoid over specialization within a single generation while it needs to be low enough to keep the experiments computationally feasible. Preliminary experiments showed that 50 evaluations produces convergence graphs that are considerably smoother compared to lower number of evaluations, while still being computationally feasible. Similar to [\[20\]](#page-26-3), we choose a large number of evaluations in the last generation since this is the most important generation as it chooses the champion heuristic. The maximum tree depth of 17 is also used by Koza [\[26,](#page-26-9) p. 265] and is the default of ECJ, the evolution software framework [\[27\]](#page-26-10) that we use.

Table [2](#page-13-1) lists the functions, and Table [3](#page-13-2) lists the terminals that are used.

Table 1: Genetic programming settings.

<span id="page-13-0"></span>

Parameter	Value
Population size	500
Generations	100
Number of evaluations per individual	50
Num evals in last generation	250
Crossover proportion	$90\%$
Mutation proportion	10%
Elitism	
Selection method	Tournament selection (size 7)
Maximum tree depth	17

Table 2: Functions used in GP.

<span id="page-13-1"></span>

Function name	Arity	Description
if4		if $\arg 0 < \arg 1$ then $\arg 2$ else $\arg 3$
$+, -, /, x$		Mathematical operators
pow	2	$arg0arg1$ , raises $arg0$ to the power of $arg1$
neg		Negates arg0
min, max		Takes the minimum or maximum, respectively, of the pro-
		vided arguments.

<span id="page-13-2"></span>Table 3: Terminals used in GP. The terminals have a context of a vehicle (the vehicle that executes the heuristic) and a parcel of interest.



One of the terminals is based on the concept of flexibility in a route. Flexibility is the degree to which arrival times in a vehicle's route can be changed without introducing time window violations. This is calculated as follows:

<span id="page-13-3"></span>flexibility(root) := 
$$
\sum_{r_i \in \text{route}}^{\text{route}} \text{lpa}(r_i) - \text{epa}(r_i)
$$
 (13)

where,  $\ln(r_i)$  is the last possible arrival time without time window violations and  $epa(r_i)$  is the earliest possible arrival time without time window violations.

Listing 1: Simple heuristic example code.

```
(x \text{ (max } (-1) + \text{insertion} \text{ overtime delivery ureency})insertion flexibility)
(pow insertion tardiness 2.0)(pow\ 10.0\ insertion\ cost))
```
<span id="page-14-1"></span>We use the standard tree-based representation of GP. A simple example of a heuristic composed of an arbitrary set of functions and terminals is shown as a Lisp expression (Listing [1\)](#page-14-0) and as a tree (Figure [5\)](#page-14-1).



Fig. 5: Simple heuristic example visualized as a tree.

We simulate each individual on 50 different scenarios. Each scenario describes a period of four hours in which 120 orders (in the small scale variant) are announced. Since a scenario is the product of a stochastic process, the difficulty of scenarios varies. Within a generation this is not a problem because fitness indicates an algorithm's quality on a set of scenarios. Consequently, when comparing two algorithms within a generation, the fitness values can be compared directly. However, a convergence graph that shows absolute values will show a lot of noise because the values between generations can not be compared directly. Therefore, we normalize the fitness values relative to the cost of the decentralized cheapest insertion cost heuristic.

## 4.3 Tuning

For investigating the performance of GP we ran some experiments with a smaller number of generations. Figure [6](#page-15-1) shows a breakdown of the convergence graph of three such runs. The figure shows that most of the improvement during evolution is caused by a reduction of tardiness and over time while travel time remains relatively constant. This suggests that it may be worthwhile to emphasize the tardiness in the objective function during evolution. We experimented with two weighted versions of decentralized GP (DGP). DGP-1:1 uses the objective function as defined in eq. [4.](#page-6-1) DGP-1:2 replaces the insertion based GP terminals with weighted versions in favor of tardiness and over time. Figure [7](#page-15-2) compares the GP runs with two weighted decentralized insertion cost heuristics, DIC-1:2 and DIC-1:4. From Figure [7](#page-15-2) it can be concluded that DIC-1:2 performs better than the 1:1 objective function while DIC-1:4 performs worse than 1:1. However, replacing the insertion based GP terminals with weighted versions does not benefit evolution, DGP-1:1

<span id="page-15-1"></span>

Fig. 6: Breakdown of cost per generation of three evolutionary runs on a scenario with 50% dynamism, 20 minutes urgency, and scale 1.

<span id="page-15-2"></span>

Fig. 7: Comparison of two evolutionary settings (average of three repetitions each), DGP-1:1 with standard objective function weights of its terminals defined in Table [2](#page-13-1) and DGP-1:2 with objective functions weights in favor of tardiness and over time. DIC-1:2 and DIC-1:4 are using weighted insertion cost (without evolution) on the same set of scenarios as are used in every generation of the GP.

outperforms DGP-1:2. This is presumably because evolution already favors heuristics that emphasize reducing tardiness and over time as this yields the greatest performance increase.

# <span id="page-15-0"></span>5 Evaluation

To compare the agent-based hyper-heuristic approach (DGP, Section [4\)](#page-11-0) with the MAS using OptaPlanner (DOP, Section [3\)](#page-8-0) and the centralized OptaPlanner (COP, [\[8\]](#page-25-2)) we first need to generate (train) the heuristics that can be used in real-time.

#### <span id="page-16-1"></span>5.1 Training

For training we have generated a separate dataset using the same settings (but different random seeds) as used in [\[8\]](#page-25-2). During training we use small scale scenarios to save computation time.

## 5.1.1 Experiment setup

We have opted for four different GP setups (Table [4\)](#page-16-0). Three setups are meant to specialize on one specific scenario class, while the DGP-mixed setup aims to generate generalized heuristics that are equally adapted to all scenarios. Because there are nine small scale scenario classes, we use 54, a multiple of nine, evaluations every generation. This ensures that each generation each individual is evaluated on exactly six scenarios of every scenario class.

<span id="page-16-0"></span>Table 4: The four different GP setups. The three specialized setups, DGP-20-35-1, DGP-50-20-1, and DGP-80-5-1, are trained on one specific class of scenarios. DGP-mixed is a setup that is trained on all small scale scenario classes simultaneously.



For the specialized GP runs we need to do  $500 \cdot (99 \cdot 50 + 250) = 2{,}600{,}000$ simulations and for the generalized GP run  $500 \cdot (99 \cdot 54 + 270) = 2,808,000$ . Since we repeat each setting ten times, the grand total of required simulations is 106,080,000. A single simulation may take from about half a second to several seconds each on a modern PC. If the average simulation time would be exactly 1 second, the expected total computation time is about 1227 days (3.3 years). Clearly, it is not feasible to run such an experiment on a single computer, therefore we have pooled the resources of about 80 modern quad-core computers to run our simulations. Theoretically, these 80 machines allow us to perform about 320 simulations in parallel. In practice, however, these are shared university machines that may have other processes running or may simply be turned off during an experiment. To utilize these machines we use a feature of RinSim that allows to spread simulations over multiple machines (internally using JPPF [\[28\]](#page-26-11)) and that is resistant to single node failures.

# 5.1.2 Results and analysis

A total of 103,374,996 simulations were computed during the course of the 40 evolutionary runs. The cumulative computation time is 1295 days, using the distributed computing setup, it took slightly more than 10 days. The actual number of simulations that were performed is slightly lower than computed in the previous paragraph because when identical individuals are found within a generation they are evaluated only once.

Figure [8](#page-17-0) shows the average convergence graphs of each GP variant. For all

<span id="page-17-0"></span>

Fig. 8: Average convergence graphs based on ten repetitions for each of the four GP settings.

GP variants, the majority of the improvement occurs in the first 25 generations. It is striking that 80-5-1 shows much less improvement compared to the other variants. This may be explained by the fact that this is probably one of the hardest problems for any algorithm. With 80% dynamism, the problem is changing nearly continuously and with an urgency of 5 minutes, each new order needs to be dealt with swiftly. Based on this graph, it appears that the insertion cost heuristic is performing relatively well in these circumstances. For the 20-35-1 and 50-20-1 settings, GP seems to be able to find the largest improvement relative to the insertion cost heuristic. GP-mixed uses all scenario classes and lies, as expected, somewhere between the others.

# 5.2 Testing

In order to evaluate the effectiveness of our GP approach, we test the evolved heuristics using real-time RinSim [\[23\]](#page-26-6) on the same dataset as was used in [\[8\]](#page-25-2).

# 5.2.1 Experiment setup

The test dataset has three levels of dynamism, urgency, and scale, resulting in 27 different scenarios classes. For each class, the dataset contains ten scenario instances. The evolutionary runs (Section [5.1\)](#page-16-1) produced 40 heuristics, additionally we are also testing the insertion cost heuristic. This means we have 41 algorithms, each of whom we need to test in real-time on the 270 different scenarios in the dataset, resulting in a total of 11,070 real-time simulations. Unlike [\[8\]](#page-25-2), we do not repeat the execution of simulations with exactly the same settings. Instead, we combine the results of the ten heuristics evolved with the same GP settings and compare those with the results of [\[8\]](#page-25-2).

To allow direct comparison of the results, we use the same hard- and software as in [\[8\]](#page-25-2). The test computer has 24 logical cores (two six core Intel Xeon 2.6GHz E5-2630 v2 processors with hyper threading). A single simulation requires two logical cores, one for the simulator and one for the solver computations. At least one core needs to be available for the operating system, resulting in a maximum of 11 simulations that can be run in parallel. As in [\[8\]](#page-25-2), we warm up the JVM for 30 seconds before starting the real-time experiment.

#### 5.2.2 Results

Table [5](#page-18-0) lists the algorithms that we compare. Similar to [\[8\]](#page-25-2), we apply Welch's

<span id="page-18-0"></span>Table 5: Algorithm names with their meaning and number of simulations per class that were performed. For COP and DOP, three repetitions were done for each of the ten scenarios in a class. For the other algorithms, no repetitions were done. For the DGP variants, each of the ten evolved heuristics were simulated on each scenario.

Algorithm	Description	Simulations per class
COP	Centralized OptaPlanner (from [8])	30
DOP	Decentralized OptaPlanner (from [8])	30
$_{\rm DIC}$	Decentralized insertion cost	10
DGP-20-35-1	Decentralized GP trained on 20-35-1 class	100
$DGP-50-20-1$	Decentralized GP trained on 50-20-1 class	100
DGP-80-5-1	Decentralized GP trained on 80-5-1 class	100
DGP-mixed	Decentralized GP trained on all small scale classes	100

t-test for testing the significance of the differences between the algorithms. In the following analysis we refer to this test by mentioning the p-values (when relevant) that were observed. The significance threshold was set at  $p = .01$ . For pairs of algorithms that have the same number of simulations we perform a paired  $t$ -test instead of an unpaired t-test. The total experiment computation time of the 11,070 real-time simulations was about 551.9 hours ( $\approx$  23 days), during this time 11 simulations were run in parallel. Table [7](#page-20-0) shows all simulation results.

#### 5.3 Analysis

The first hypothesis (Section [1\)](#page-1-0) states that hyper-heuristics (DGP) can outperform DOP. We can accept this hypothesis as the results indicate that there is always at least one of the DGP variants that outperform DOP (Table [6\)](#page-19-0). In fact, DGP-mixed, DGP-80-5-1, and DGP-50-20-1 are better than DOP for all scenario classes. Table [6](#page-19-0) shows that DGP-20-35-1 also often outperforms DOP but not as often. It's also noteworthy that DIC outperforms DOP in several (mostly small scale) classes, indicating that in some cases even a simple heuristic can be better than OptaPlanner.

<span id="page-19-0"></span>Table 6: Summary of relative performance of DGP variants to DOP. Each number indicates the number of classes on which the algorithm is (significantly) better or worse compared to DOP.



n indicates that the difference between the value of rank  $n$  and rank  $n + 1$  is not statistically significant ( $p < 0.01$ ). The results of the four evolved algorithms also report their standard deviation as the numbers are the average of the different homician are duced by CD. different heuristics produced by GP.

<span id="page-20-0"></span>

		different heuristics produced by GP.						
Class	COP	DOP	$\overline{DIC}$	DGP-20-35-1	DGP-50-20-1	DGP-80-5-1	DGP-mixed	<b>Best</b>
$20 - 5 - 1$	$25.100^{1\dagger}$	$28.550^{6\dagger}$	$27.042^{5\dagger}$	$31.025^7 \pm 13.876$	$26.480^{4\dagger} \pm 1.169$	$25.754^{3} \pm 0.579$	$25.611^{2\dagger} \pm 0.392$	COP <sup>†</sup>
$50 - 5 - 1$	$22.276^{3\dagger}$	$23.902^{6\dagger}$	$23.218^{5\dagger}$	$25.835^{7} \pm 8.489$	$22.898^{4\dagger} \pm 1.462$	$21.665^{1\dagger} \pm 0.372$	$21.912^{2\dagger} \pm 0.398$	$\text{DGP-80-5-1}^{\dagger}$
$80 - 5 - 1$	$21.481^{2\dagger}$	$23.511^{6\dagger}$	$22.782^{5\dagger}$	$25.969^7 \pm 10.079$	$22.658^{4\dagger} \pm 1.259$	$21.281^{1\dagger} \pm 0.380$	$21.755^3 \pm 0.334$	$DGP-80-5-1$ <sup>†</sup>
$20 - 20 - 1$	$17.692^{1\dagger}$	$21.661^7$	$20.748^{6\dagger}$	$18.987^{4\dagger} \pm 0.363$	$18.705^{2\dagger} \pm 0.300$	$19.152^{5\dagger} \pm 0.330$	$18.869^{3\dagger} \pm 0.306$	COP <sup>†</sup>
$50 - 20 - 1$	$14.852^{1\dagger}$	17.5757	16.8786†	$15.267^{4\dagger} \pm 0.376$	$15.223^{3\dagger} \pm 0.243$	$15.507^{5\dagger} \pm 0.678$	$15.181^{2\dagger} \pm 0.272$	COP <sup>†</sup>
$80 - 20 - 1$	$14.438^{1\dagger}$	17.1686†	17.7507	$15.018^4 \pm 0.338$	$14.800^{2\dagger} \pm 0.155$	$15.335^{5} \pm 0.491$	$14.866^{3\dagger} \pm 0.296$	COP <sup>†</sup>
$20 - 35 - 1$	14.520 <sup>1</sup>	19.3967	18.748 <sup>6†</sup>	$16.477^{3\dagger} \pm 0.340$	$16.373^{2\dagger} \pm 0.277$	$17.021^{5\dagger} \pm 0.818$	$16.569^4 \pm 0.278$	COP
$50 - 35 - 1$	12.921 <sup>1</sup>	$17.359^{6\dagger}$	17.6367	$14.436^{2\dagger} \pm 0.453$	$14.543^{3\dagger} \pm 0.321$	$14.963^5 \pm 0.458$	$14.598^{4\dagger} \pm 0.283$	COP
$80 - 35 - 1$	12.395 <sup>1</sup>	$15.743^{6\dagger}$	16.3037	$13.742^{3\dagger} \pm 0.239$	$13.610^{2\dagger} \pm 0.181$	$14.178^{5} \pm 0.547$	$13.792^4 \pm 0.342$	COP
$20 - 5 - 5$	$18.809^{3\dagger}$	$20.068^{5\dagger}$	$20.229^{6\dagger}$	$22.217^7 \pm 9.248$	$19.101^{4\dagger} \pm 2.516$	$17.781^{1\dagger} \pm 0.231$	$17.883^{2\dagger} \pm 0.288$	$DGP-80-5-1$ <sup>†</sup>
$50 - 5 - 5$	17.131 <sup>5</sup>	16.5654	$18.590^{6\dagger}$	$18.616^7 \pm 6.244$	$16.005^{3\dagger} \pm 1.834$	$14.762^{1\dagger} \pm 0.180$	$14.884^{2} \pm 0.291$	$DGP-80-5-1$ <sup>†</sup>
$80 - 5 - 5$	$17.249^{5\dagger}$	16.402 <sup>4</sup>	18.5497	$18.485^{6\dagger} \pm 6.164$	$15.912^{3\dagger} \pm 1.723$	$14.664^{1\dagger} \pm 0.160$	14.790 <sup>2</sup> $\pm$ 0.231	$DGP-80-5-1$ <sup>†</sup>
$20 - 20 - 5$	$13.987^{3\dagger}$	$16.904^{6\dagger}$	17.6567	$13.941^{2\dagger} \pm 0.303$	$13.833^{1\dagger} \pm 0.139$	$14.690^5$ $\pm$ 0.730	$14.034^4$ $\pm$ 0.263	$DGP-50-20-1$ <sup>†</sup>
$50 - 20 - 5$	$10.198^{4\dagger}$	$11.615^{6}$	14.1767	$9.756^{3\dagger} \pm 0.186$	$9.497^{1} \pm 0.115$	$10.297^5$ $\pm$ 0.725	$9.749^{2\dagger} \pm 0.147$	DGP-50-20-1
80-20-5	$10.329^{4\dagger}$	11.837 <sup>6</sup>	14.8517	$10.082^3 \pm 0.238$	$9.823^1$ $\pm$ 0.163	$10.613^{5}$ $\pm$ 0.729	$10.044^{2\dagger} \pm 0.196$	DGP-50-20-1
$20 - 35 - 5$	$10.967^{1\dagger}$	$14.097^{6\dagger}$	15.5557	$11.083^2 \pm 0.184$	$11.289^4 \pm 0.188$	$11.938^{5}$ $\pm$ 0.660	$11.277^{3\dagger} \pm 0.220$	$COP^{\dagger}$
$50 - 35 - 5$	$8.677^{1\dagger}$	11.326 <sup>6</sup>	14.4437	$8.884^{2\dagger} \pm 0.203$	$8.973^{3\dagger} \pm 0.246$	$9.718^{5}$ $\pm$ 0.674	$9.057^4 \pm 0.201$	COP <sup>†</sup>
80-35-5	8.877 <sup>1</sup>	11.206 <sup>6</sup>	14.8177	$9.099^{2} \pm 0.247$	$9.251^{4} \pm 0.220$	$9.922^5$ $\pm$ 0.614	$9.247^{3\dagger} \pm 0.202$	COP
$20 - 5 - 10$	17.587 <sup>4</sup>	$17.929^{5\dagger}$	$18.926^{6\dagger}$	$20.166^7 \pm 7.779$	$17.156^{3\dagger} \pm 2.665$	$15.858^{1\dagger} \pm 0.142$	$15.929^2$ $\pm$ 0.313	$DGP-80-5-1$ <sup>†</sup>
$50 - 5 - 10$	$15.681^{5\dagger}$	14.588 <sup>4</sup>	$17.517^7$	$16.828^{6\dagger} \pm 6.557$	$13.917^3 \pm 1.828$	$12.835^2 \pm 0.181$	$12.828^{1\dagger} \pm 0.328$	$DGP$ -mixed <sup>†</sup>
$80 - 5 - 10$	$15.898^{5\dagger}$	14.446 <sup>4</sup>	17.7837	$16.518^{6\dagger} \pm 5.572$	$14.100^{3\dagger} \pm 1.828$	$12.895^{1\dagger} \pm 0.160$	$12.935^2$ $\pm$ 0.373	$DGP-80-5-1$ <sup>†</sup>
$20 - 20 - 10$	11.5885	$13.320^{6\dagger}$	15.043 <sup>7</sup>	$10.758^{1\dagger} \pm 0.221$	$10.776^2$ $\pm$ 0.116	$11.554^{4\dagger} \pm 0.717$	$10.939^{3}$ $\pm$ 0.198	$DGP-20-35-1$ <sup>†</sup>
$50 - 20 - 10$	$9.329^{4\dagger}$	10.649 <sup>6</sup>	14.2607	$8.799^{2\dagger} \pm 0.247$	$8.585^{1}$ $\pm 0.067$	$9.478^{5}$ $\pm$ 0.808	$8.799^{3}$ $\pm$ 0.149	DGP-50-20-1
80-20-10	$9.167^{4\dagger}$	$10.469^6$	14.1497	$8.710^{2\dagger} \pm 0.253$	$8.489^{1}$ $\pm$ 0.114	$9.347^{5}$ $\pm$ 0.763	$8.727^{3}$ $\pm$ 0.136	DGP-50-20-1
$20 - 35 - 10$	$9.787^{4\dagger}$	$11.990^{6\dagger}$	13.9837	$9.158^{1} \pm 0.186$	$9.437^{3\dagger} \pm 0.313$	$10.069^5$ $\pm$ 0.641	$9.405^{2\dagger} \pm 0.234$	DGP-20-35-1
$50 - 35 - 10$	$7.827^{1\dagger}$	10.0536	14.0047	$7.838^2 \pm 0.203$	$8.060^{4}$ $\pm$ 0.409	8.744 <sup>5</sup> $\pm$ 0.695	$8.044^{3\dagger} \pm 0.212$	COP <sup>†</sup>
80-35-10	$7.870^{2\dagger}$	9.8796	14.0787	$7.767^{1\dagger} \pm 0.187$	$7.984^4 \pm 0.389$	$8.582^{5} \pm 0.683$	$7.913^{3\dagger} \pm 0.196$	$DGP-20-35-1$ <sup>†</sup>
Average rank	2.7	5.74	6.56	3.81	2.74	3.74	2.7	

The differences between DGP-mixed and DOP and between DGP-80-5-1 and DOP are always significant, even for large scale scenarios. This is interesting because the heuristics were never trained on large scale scenarios. It appears that the evolved heuristic has no problem scaling up to large problem instances. To investigate whether the heuristic's scalability can be explained by its supposed computational efficiency, we have measured the computational runtimes within a single simulation of both the DOP as well as the DGP-50-20-1 on a scenario with class 50-20-10 (Figure [9\)](#page-21-0). The big gap between DGP-50-20-1 and DOP is caused

<span id="page-21-0"></span>

Fig. 9: Average bid computation times for both the DGP-50-20-1 and DOP on a single scenario of class 50-20-10. The error bars indicate the 95% confidence interval. There are no values for route length 0 and 1 for DOP because it is unnecessary to let the OptaPlanner solver compute an insertion in this case. Note that up until route length 7, the average computation time for DGP-50-20-1 is below 1 ms.

by the unimproved time parameter of the OptaPlanner solver. This parameter determines the period the solver keeps searching while it has not found an improving solution. In [\[8\]](#page-25-2), unimproved time is set to 20 ms, which explains why the fastest computation time of DOP is always higher than 20 ms. Additionally, Figure [9](#page-21-0) shows that the DGP heuristic is fast and growing at a low rate (averages range from 0.074 to 5.827 milliseconds between route length 0 and 15).

To investigate the influence of the bid computation time on the performance of the DGP approach, we conducted an additional experiment where we artificially delayed the computation of the heuristic. This experiment was carried out with a single DGP-50-20-1 heuristic and on all ten scenarios in the 50-20-10 class. Table [8](#page-21-1) indicates that the computational efficiency of the DGP approach is a contributing factor for its relatively good performance. With a delay of 100 milliseconds,

<span id="page-21-1"></span>Table 8: Average cost of DOP with a single heuristic from DGP-50-20-1 with and without an artificial bid computation delay.

Class	Algorithm	Cost
$50-20-10$	<b>DOP</b>	10.649
$50-20-10$	$DGP-50-20-1$ no delay	8.634
$50-20-10$	DGP-50-20-1 100 ms delay	9.251
$50-20-10$	DGP-50-20-1 200 ms delay	11.102

DGP-50-20-1 still outperforms DOP. However, with a delay of 200 milliseconds, DGP-50-20-1 performs worse compared to DOP. Based on this observation we conclude that the quality of cost estimations made by the evolved heuristics must be higher than the estimations made by DOP.

The second hypothesis states that DGP can outperform COP. This hypothesis can be accepted since the evolved heuristics regularly outperform COP (Table [9\)](#page-22-0). However, COP still performs best in 11 of the 27 classes. The scale and urgency of a problem seem to be good indicators of the relative performance of the DGP approaches and COP. The more urgent and large scale a problem is, the better the DGP approaches perform.

<span id="page-22-0"></span>Table 9: Summary of relative performance of DGP variants to COP. Each number indicates the number of classes on which the algorithm is (significantly) better or worse compared to COP.

Algorithm	sign. better	better (not sign.)	worse (not sign.)	sign. worse
DIC				19
$DGP-20-35-1$				
$DGP-50-20-1$			10	
DGP-80-5-1			10	
DGP-mixed				

The third hypothesis states that the evolved heuristics perform especially well in more urgent circumstances. Based on Table [7](#page-20-0) it is clear that evolved heuristics outperform COP in eight of the nine very urgent classes (urgency of five minutes), we can therefore accept this hypothesis. The class where COP is better than the evolved heuristics is 20-5-1. In this class, COP is not significantly different from DGP-mixed ( $p \approx .45$ ), DGP-80-5-1 ( $p \approx .34$ ), and DGP-50-20-1  $(p \approx .05)$ . Additionally, we expect that the fact that the heuristics have relatively short computation times is a stronger factor in more urgent scenarios, because the available computation time is shorter.

Hypothesis four states that specialized heuristics outperform general heuristics on scenarios for which they are specialized. DGP-20-35-1 outperforms DGP-mixed on class 20-35-1 (but not significantly,  $p \approx .54$ ), however, DGP-50-20-1 performs best of the evolved heuristics on this class. Surprisingly, DGP-mixed outperforms DGP-50-20-1 on its training class, 50-20-1, although not significantly ( $p \approx .76$ ). A possible explanation for the good performance of DGP-mixed in this case is that it is trained on all small scale scenarios and 50-20-1 is an 'average' scenario, it has medium dynamism and medium urgency. DGP-80-5-1 performs best on its training class 80-5-1, the difference with DGP-mixed is significant ( $p \approx .004$ ). So, for all three classes on which was trained explicitly, the specialized heuristic significantly outperforms the general heuristic only once. The difference is not significant in two other cases, therefore we reject the hypothesis. We conclude that in some situations a general heuristic can perform comparably to a specialized heuristic. Our results seem to conform to the 'no free lunch theorem' [\[29\]](#page-27-0). The urgency on which a heuristic was trained is a strong indicator of how well it will perform on a scenario class. We created a summary of the relative performance of the DGP variants, grouped by urgency (Table [10\)](#page-23-1). The table shows that each specialized <span id="page-23-1"></span>Table 10: Summary of relative performance of DGP variants per urgency level. Each number indicates the number of classes on which the algorithm is the best DGP approach for that urgency level.



heuristic performs best on seven out of nine classes that have the urgency level on which the heuristic was trained.

The fifth hypothesis states that generalized heuristics outperform specialized heuristics on scenarios for which they are not specialized. Based on Table [10](#page-23-1) we can reject this hypothesis. There are only three classes, 20-5-1, 50-20-1, and 50-5-10, where DGP-mixed outperforms the other evolved heuristics. This result is somewhat surprising, especially since the number of evaluations for mixed is slightly more than for the specialized heuristics (54 vs 50 evaluations). Nevertheless, the DGP-mixed method produces heuristics of good quality as is demonstrated by its average rank of 2.7 which is the best average rank shared by COP. However, when computing the average ranks of only the four DGP heuristics, DGP-50-20-1 has the same rank as DGP-mixed (average rank 2.19).

As expected, DIC is on average the worst performing algorithm. There are, however, several cases where DGP-20-35-1 performs worse compared to DIC. The data in Table [7](#page-20-0) shows that DGP-20-35-1 performs among the worst in the most urgent scenarios. This is expected considering that it was trained on the least urgent scenarios. The results of this heuristic are made even worse by one instance that performs especially bad (as can be seen by the larger than usual standard deviations). When removing this badly performing heuristic from the analysis, the ranks for the DGP-20-35-1 are still among the worst for the very urgent classes, but the values are much closer to that of DIC. This indicates that the bad performance is not just explained by this one outlier.

## 5.4 Reproducibility

Following the policy in [\[30\]](#page-27-1) we open-sourced all software that was written for the research described in this paper and made it available online. The scripts for running each experiment described in this paper can be found in [\[31\]](#page-27-2). All resulting data, including the scripts that we used for the analysis, as well as visualizations of all heuristics, are available in [\[32\]](#page-27-3). This code depends on several other open source projects that we developed. For all simulations we used RinSim version 4.3.0 [\[33\]](#page-27-4). The code for the OptaPlanner based algorithms is part of RinLog version 3.2.0 [\[34\]](#page-27-5), the evolutionary algorithms related code can be found in [\[35,](#page-27-6) [36\]](#page-27-7). The scenario files that we generated for training were generated using our dataset generator [\[37\]](#page-27-8).

# <span id="page-23-0"></span>6 Conclusion

Agents in a multi-agent system typically compute decisions using traditional optimization algorithms. We have investigated an alternative approach based on hyper-heuristics. The present paper is the first to evaluate the performance of an agent-based hyper-heuristic approach on a real-time logistics problem that systematically varies the dynamism, urgency, and scale of the problem. The results show that our hyper-heuristic outperforms a reference algorithm, based on the OptaPlanner optimization library, in all scenarios. In addition, the decentralized hyper-heuristic approach even outperforms the centralized reference algorithm in most situations. The hyper-heuristic approach performs relatively better on more urgent and larger scale problems. The hyper-heuristic approach has the additional advantage that it can specialize on certain problem characteristics, increasing its performance even further.

We see three interesting directions for future work. The first direction is to make the logistics simulator even more realistic. Examples that will improve realism are, using a road layout of a city, using real-world customer data, having a heterogeneous fleet of vehicles, or, imposing fuel constraints. The goal of increasing realism is to evaluate whether the hyper-heuristic agent approach can outperform traditional algorithms in real-world conditions, hopefully leading to their eventual deployment. The second research direction is to investigate different team compositions and level of selection in the evolutionary process. The work done by Waibel et al. [\[38\]](#page-27-9) seems to be applicable to evolutionary designing multi-agent systems for logistics problems. A possible hypothesis in a heterogeneous setup could be the emergence of agent specializations. For example, agents could optimize towards pickup and deliveries in a specific geographical area, such as inner city versus rural areas. Thirdly, in the current hyper-heuristic setup, the parts of agents that are subject to evolution are relatively small. The agent behavior as well as the contract-net coordination protocol are predetermined. A very interesting line of work would be to give evolution more freedom. A challenge would be to determine a set of basic coordination or communication building blocks. Using these building blocks, evolution could start exploring in the space of possible coordination mechanisms. It would be interesting to see if evolution would create novel coordination mechanisms or if it would reinvent existing coordination mechanisms. Since we made all our algorithms and results freely available, we believe that the present paper provides an ideal starting point for any of these future research directions.

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