Monitoring moisture movements in building materials using X-ray attenuation: Influence of beam-hardening of polychromatic X-ray photon beams

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Abstract

X-ray attenuation measurements are commonly used as a non-destructive method to monitor internal concentration changes of moisture (i.e., moisture content) and other chemical compounds in porous building materials. The technique provides direct measurements of moisture content changes through analysis with a composite model consisting of a dry porous material and a thickness of water equivalent to the moisture content of the material. The current formulation of this composite model relies on certain assumptions, including a monochromatic X-ray photon beam source (i.e., X-ray photons of a single, consistent energy) and that interactions between the X-ray photons and the materials (water and porous material) are independent. However, X-ray sources typically used by researchers in this field of study produce X-ray photon beams over a spectrum of energy levels, or polychromatic X-ray photons. Implications of this inconsistency are introduced and discussed. This paper presents both an overview of fundamental descriptions of the X-ray attenuation measurement technique and results from a parametric experimental study of various porous construction materials, including calcium silicate board, aerated autoclaved concrete, clay brick, cementitious materials, and wood. Results from the parametric investigation indicate the attenuation coefficient of water is dependent on the type and thickness of the porous material.

Keywords: Moisture content, X-ray, Attenuation coefficient, Porous media

1. Introduction

Moisture, and more specifically varying moisture conditions, often significantly affects structural performance and durability of construction materials. For example, moisture movements may affect warping of timber studs [1], workability [2] and plastic cracking [3] of fresh cementitious materials, maturation of bond strength of lime mortars [4], aging of bitumen binders [5], freeze-thaw damage of concretes [6], etc. Furthermore, moisture influences various chemical, biological and thermal characteristics of materials. In general, moisture and moisture movements are key determining factors in the durability of structures constructed from a multitude of materials. Therefore, experimental approaches for accurate non-destructive monitoring of moisture conditions are essential. Various non-destructive methods are available [7]; however, X-ray

attenuation measurements are emerging as a popular technique for monitoring moisture movements in various porous materials, particularly in cracked materials [8–21]. Measurement speed and resolution, ease of two-dimensional (or three-dimensional [22]) imaging, availability of facilities, and direct measurement of changes in moisture content are key advantages.

X-ray technologies are commonplace in the medical and security fields; however, application of X-ray attenuation measurements for monitoring of moisture movements in porous media is relatively complex. Changes in moisture content necessitate comparison of multiple X-ray measurements captured at different states (i.e., times). Currently, descriptions of basic and fundamental controlling mechanisms and influential factors are somewhat lacking.

Quantification of moisture content in porous materials from X-ray attenuation measurements is achieved by decomposing a water-containing (saturated or partially saturated) porous material into a dry porous material of the same thickness and a water layer with a thickness

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equivalent to the moisture content [14, 16–18, 20]. Using the composite system, equations have been derived allowing for calculation of moisture content changes from X-ray measurements taken at different states. The derived expressions however depend upon certain assumptions. Firstly, calculations assume the incoming X-ray photons are of a single, constant energy. Secondly, the quantification of moisture content in porous material with X-ray attenuation is based on a non-interacting composite concept where the attenuation of X-ray photons provided by the porous material and the water are assumed independent. This paper demonstrates these assumptions are not generally valid, and that the interaction between material and water needs to be accounted for to accurately quantify moisture contents in porous materials via X-ray attenuation. Further, the common use of polychromatic X-ray sources, which produce X-ray photons over a spectrum of energies, needs to be accounted for to accurately quantify moisture contents in porous materials via X-ray attenuation.

The first section of the paper summarizes the physics of X-ray attenuation, including both monochromatic and polychromatic X-ray photon beams. Key terminology and common misconceptions within the civil/materials engineering communities, particularly the various definitions of attenuation coefficient, are introduced. In the remaining section the composite concept typically utilized to relate changes in X-ray photon counts to changes in moisture content is challenged. Factors affecting the composite concept, including primarily beam hardening and the resulting dependence of the attenuation coefficient of water on the 'parent' material, are discussed. While specific results presented are dependent on the type of materials investigated (calcium silicate board, aerated autoclaved concrete, clay brick, cementitious materials, and wood here) and also likely on the X-ray system used, vital conclusions on and potential pitfalls of the general measurement technique are discussed in this paper.

2. Fundamentals of the X-ray attenuation measurement technique

Fig. 1(a) illustrates the required equipment and the behaviour of an X-ray photon beam during X-ray attenuation measurements. For such measurements a specimen is placed between an X-ray source, which produces a conical beam of X-ray photons, and an X-ray detector (camera used here). Additional details on the interactions between X-ray photons and the specimen are described in a following section. Fig. 1(b) illustrates the commonly accepted composite concept, consisting

of a dry or partially saturated specimen and a thickness of water, to describe the effect moisture content changes have on X-ray attenuation measurements [8, 14, 16–18, 20, 23]. Using this composite system along with several assumptions, a relationship can be derived to convert changes in X-ray photon counts to changing moisture content of porous materials. One key assumption in the derivation of this relationship is that the porous material does not impact the X-ray attenuation provided by water, and vice versa; therefore, the model illustrated in Fig. 1(b) is referred to as a 'non-interacting' composite concept. The following sections describe the X-ray attenuation measurement technique in detail, provide the derivation of the photon count-moisture content relationship, and introduce other common assumptions.

2.1. Interactions between X-ray photons and building materials

As illustrated in Fig. 1(a) an X-ray photon beam with an initial intensity, I_0 is produced by an X-ray source and passes through a specimen. A portion of the photons interact with the specimen, reducing the initial intensity to the transmitted intensity, I . The reduction in intensity for a monochromatic X-ray photon beam (i.e., photons of single and constant energy) is described by Eq. 1 and 2:

$$\frac{dI(x)}{dx} = -\mu \cdot I(x) \quad (1)$$

or in the more common form, known as the Beer-Lambert law [24]:

$$I = I_0 \cdot e^{-\mu \cdot t} \quad (2)$$

where μ is the linear attenuation coefficient [m^{-1}], $I(x)$ is the number of X-ray photons present at depth x , and t is the thickness of the specimen [m]. The units for intensity are counts or hits, simply indicating the number of X-ray photons.

The linear attenuation coefficient, μ is equivalent to the total probability of X-ray photon-material interaction per unit length of a material. An X-ray photon passing through a building material may interact on the atomic level in one of three ways – photoelectric effect, Compton scatter, or pair production [25]. Eq. 3 defines μ therefore as:

$$\mu(E, Z_{eff}, \rho) = \tau(E, Z_{eff}, \rho) + \sigma(\rho) + \kappa(E \geq 1022 \text{ keV}, \dots) \quad (3)$$

where τ , σ , and κ are the photoelectric, Compton, and pair production cross-sections [m^{-1}], respectively, all of

Figure 1: Schematic representation of a typical X-ray attenuation experimental setup. (a) illustrates the Beer-Lambert Law while (b) illustrates a composite experimental system consisting of a dry specimen and an amount of liquid water to represent movement of moisture.

which are characteristics of the material through which X-ray photons are passing.

The photoelectric effect describes one possible interaction between a photon and a bound atomic electron in the specimen, wherein the photon is absorbed and a photoelectron is produced. The probability of this interaction (τ) increases with the effective atomic number, Z_{eff} and density, ρ [kg/m³] of the specimen and decreases significantly with increased X-ray photon energy, E [keV]. Compton scatter occurs when an X-ray photon collides with a free electron, causing a change in direction and reduction in energy of the photon. The probability of this interaction (σ) increases with ρ and is slightly influenced by E at energies far higher than typically used for the type of investigations discussed here [25]. Pair production, wherein the photon and an atomic nucleus interact to create an electron-positron, only occurs for $E > 1022$ keV (i.e., minimum kinetic energy required to initiate pair production) [25]. Such energies far exceed typically used X-ray source energy settings [8–23]. Therefore, for $E < 200$ keV the energy-, effective atomic number-, and density-dependent linear attenuation coefficient, μ can be described according to Eq. 4 [26–28]:

$$\mu(E, Z_{eff}, \rho) = \left(a \frac{Z_{eff}^{3.8}}{E^b} + c \right) \cdot \rho \quad (4)$$

where a and c are coefficients describing the photoelectric and Compton cross-sections, respectively and

b describes the shape of the photoelectric cross-section curve. The first term of Eq. 4 is equivalent to the photoelectric cross-section, τ in Eq. 3, while the second term is equivalent to Compton cross-section, σ . The Compton cross-section is assumed to be photon energy-independent below 200 keV [26–28].

Fig. 2 shows fitting results of Eq. 4 against tabulated data on linear attenuation coefficients for liquid water, μ_w , in [29]. Due to the photoelectric effect low energy X-ray photons are attenuated more efficiently, a trend inherent in all elements and compounds (see [e.g., 29]). Compton cross-section controls μ_w -values for photon energies greater than approximately 26 keV.

2.2. Impact of polychromatic X-ray sources

The X-ray source utilized here (described in [8]) and sources utilized by others [7, 9–22] produce X-ray photons over a spectrum of energies (i.e., polychromatic) limited to the user-defined X-ray energy setting, E_m as illustrated in Fig. 3(a). Furthermore, the X-ray camera used here, described below, and similar devices used by others [7, 14, 17, 18] detect only the presence of individual X-ray photons and not the energy of individual photons. The use of these non-energy discretizing X-ray cameras with a polychromatic X-ray source requires the introduction of an average attenuation coefficient, $\bar{\mu}$ as discussed below. Further, the polychromatic X-ray source leads to so-called beam hardening [30] illustrated in Fig 3(b), which must be considered.

Figure 2: Fitting provided by Eq. 4 to tabulated data on μ_w from [29] including contributions from photoelectric and Compton cross-sections R^2 was 0.999 for μ between 0-200 keV.

Fig. 3(a) illustrates a possible X-ray spectrum produced by an X-ray source, assuming an X-ray source energy (i.e., E_m) of 85 keV. The shape of the initial intensity spectrum presented in Fig. 3(a) comes from [31] where a photon energy detector measured the X-ray spectrum produced by the exact source utilized here. The shape of the photon energy spectrum, described by $\Psi_E(x)$, changes due to attenuation as it passes through increasing thicknesses, x of material. To illustrate this effect, the transmitted spectrum was calculated by applying Eq. 2 at each X-ray energy level and using the fitted linear attenuation coefficients of water for a 15 mm thickness of water as shown in Fig. 3(b). Attenuation provided by the water progressively increases the average X-ray photon energy, meaning the remaining X-ray photons are ‘harder,’ hence the term beam hardening. Due to beam hardening, pre-filters, or thicknesses of various materials placed between the X-ray photon source and measurement specimen, are used by some researchers to attenuate the lowest energy X-ray photons prior to their interaction with the measurement specimen. Various materials are used including water in combination with aluminum [30] and gadolinium [8]; however, it should be noted that pre-filters minimize, and do not eliminate, beam hardening [30]. Pre-filters were not utilized in the work presented in this paper.

The X-ray camera used measures only the number of X-ray photons (i.e., intensity) as the sum of the area under the $\Psi_E(x)$ -curve, as shown in Fig. 3(a) for an initial intensity, I_0 . The X-ray camera used here does not distinguish between photons of varying energies (certain X-ray cameras, capable of measuring the X-ray pho-

ton spectra at each pixel [36], could potentially provide vastly more information from X-ray attenuation measurements including monitoring of multi-species concentration changes). Therefore, relating the initial and transmitted intensities, I_0 and I respectively, shown in Fig. 3(b) is not directly possible using Eq. 1 and 2. Eq. 1 must be modified, removing the linear attenuation coefficient, μ and introducing an average attenuation coefficient, $\bar{\mu}$ over the spectrum, $\Psi_E(x)$ [32, 33] defined by:

$$\bar{\mu} = \frac{\int_0^{E_m} \mu(E, Z_{eff}, \rho) \cdot \Psi_E(x) dE}{\int_0^{E_m} \Psi_E(x) dE} \quad (5)$$

The X-ray spectrum, $\Psi_E(x)$, which can vary depending on X-ray source (see spectra provided in references [8, 12, 14, 18]), clearly influences the average attenuation coefficient. Fig. 3(c) shows calculated values of $\bar{\mu}$ as a function of water thickness, where the $\Psi_E(x)$ -curves were calculated as previously described. The broken line in Fig. 3(c) indicates the value of the linear attenuation coefficient of water (μ_w) at the X-ray source energy setting of 85 keV. The blue diamonds show the average attenuation coefficient for varying thickness of water, as calculated using Eq. 5. The calculations indicate average attenuation coefficients are potentially several orders of magnitude higher than linear attenuation coefficients. The average attenuation coefficient is asymptotic to the linear attenuation coefficient at the maximum X-ray photon energy as a sufficient thickness would attenuate all but the most energetic photons.

Due to beam hardening, $\bar{\mu}$ is no longer a constant, but varies with the location in the material. Fig. 4 illustrates the thickness-dependency of the average attenuation coefficients from measurements on concrete. The specimen thickness-dependency of the average attenuation coefficient can be described by Eq. 6 [32, 33]:

$$\bar{\mu}(t) = \frac{\mu_0}{(1 + \lambda \cdot t)^2} = \frac{\bar{\mu}(\Psi_E(0), Z_{eff}, \rho)}{(1 + \lambda \cdot t)^2} \quad (6)$$

where μ_0 is the initial average attenuation coefficient [m^{-1}] and λ is the beam hardening coefficient of the material [m^{-1}]. The initial average attenuation coefficient, μ_0 , may be considered the average attenuation coefficient of an infinitely thin section of material, indicating μ_0 -values must depend upon the initial X-ray spectrum, $\Psi_E(0)$. Further, based on Eq. 4, μ_0 -values also likely depend on the density (ρ) and effective atomic number (Z_{eff}) of the material. Therefore, the second definition for $\bar{\mu}$ is included in Eq. 6. Eqs.

Figure 3: Illustration of influence of X-ray spectrum on X-ray attenuation measurements including: (a) possible X-ray spectrum produced by X-ray source with an X-ray source energy setting of 85 keV and the photon energy dependent linear attenuation coefficients, (b) calculated transmitted spectrum through a 15 mm thickness of water, and (c) comparison of average attenuation coefficients at varying thicknesses of water and the linear attenuation coefficient at 85 keV.

4 and 5 provide a means to derive an expression for $\bar{\mu}(\Psi_E(0), Z_{eff}, \rho)$; however, solutions are complicated due to a singularity when the X-ray energy is 0 keV. Therefore, Eq. 7 is suggested as a possible means to relate μ_0 -values to the X-ray source energy setting, E_m and material properties, based upon Eq. 4:

$$\mu_0 = \bar{\mu}(\Psi_E(0), Z_{eff}, \rho) = \left(a^* \frac{Z_{eff}^{3.8}}{E_m^{b^*}} + c^* \right) \cdot \rho \quad (7)$$

where the terms a^* , b^* , and c^* are analogous to a , b , and c described in Eq. 4 for the initial average attenuation coefficient. The term $a^* \cdot Z_{eff}^{3.8}$ can be replaced with a single variable, α to simplify fitting of experimental results presented later due to the complex stoichiometry of the materials tested. Values from Eq. 6 yield tangential slopes of the solid red plot in Fig. 4; therefore, to simplify analysis the effective attenuation coefficient, μ_{eff} , is utilized.

The effective attenuation coefficient, μ_{eff} [m^{-1}], is needed for use in the integrated Beer-Lambert law (Eq. 1) to describe the X-ray attenuation provided by a particular thickness of a material, as defined by Eq. 8:

$$\mu_{eff} = \frac{\int_0^t \bar{\mu} dx}{t} = \frac{\int_0^t \frac{\bar{\mu}(\Psi_E(0), Z_{eff}, \rho)}{(1 + \lambda \cdot x)^2} dx}{t} \quad (8)$$

$$= \frac{\bar{\mu}(\Psi_E(0), Z_{eff}, \rho)}{1 + \lambda \cdot t}$$

Combining Eqs. 8 and 7 provides an expression to describe the effect of X-ray source energy and beam hardening on the effective attenuation coefficients of materials which is measured using a polychromatic X-ray

source and an X-ray camera:

$$\mu_{eff} = \frac{\left(\frac{\alpha}{E_m^{b^*}} + c^* \right) \cdot \rho}{1 + \lambda \cdot t} \quad (9)$$

The various attenuation coefficients illustrated in Fig. 4 are analogous to another material behavior more familiar to the civil engineering community, namely the various measurements of elastic modulus. In this analogy the initial average attenuation coefficient coincides with the initial tangent elastic modulus, the average attenuation coefficient with the tangent elastic modulus, and the effective attenuation coefficient with the secant elastic modulus.

Figs. 3(c) and 4 indicate the potential for error in X-ray attenuation measurements if an incorrect attenuation coefficient of water is used. Results from the study presented in the second part of this paper further indicate the attenuation coefficient of water is affected by the type and thickness of the porous specimen.

2.3. Composite concept for assessment of concentration changes

Commonly, changes in moisture content (or changes in concentration of other materials [e.g., corrosion products, 23]) in a porous building material are described as the composite system shown in Fig. 1(b). Here an X-ray photon beam with initial intensity, I_0 reduces to a transmitted intensity through a wet material, I_{wet} in two drops: 1) some photons interact with the dry (or partially saturated) porous material resulting in a dry transmitted intensity, I_{dry} , and 2) additional photons interact with a water layer with thickness t_w , equivalent to

Figure 4: Descriptions of linear, average, and effective attenuation coefficients, μ , $\bar{\mu}$, and μ_{eff} , respectively. Values for $\bar{\mu}$ are the tangential slopes of the red line, which is fitted to the shown measured values for concrete (circle symbols) at a maximum X-ray photon energy, E_m of 60 keV. The linear attenuation coefficient, μ for concrete at 60 keV found in [29].

the material's water content resulting in a wet transmitted intensity, I_{wet} . The composite system simulates water uptake by increasing the equivalent water thickness, while drying corresponds to a reduction in water thickness. Using Eq. 2 and assuming interactions between X-ray photons and the dry porous material only influence the quantity of photons (and not photon energy), I_{wet} may be expressed as:

$$I_{wet} = I_{dry} \cdot e^{-\mu_w \cdot t_w} = I_0 \cdot e^{-\mu \cdot t} \cdot e^{-\mu_w \cdot t_w} = I_0 \cdot e^{-\mu \cdot t - \mu_w \cdot t_w} \quad (10)$$

for a monochromatic beam, and as derived in [8, 14] moisture content changes can be directly calculated by measurements of I_{dry} and I_{wet} according to Eq. 11:

$$\Delta w = -\frac{\rho_w}{\mu_w \cdot t} \ln \left(\frac{I_{wet}}{I_{dry}} \right) \quad (11)$$

where Δw is a change in moisture content [kg/m^3], ρ_w is the density of water [kg/m^3], and μ_w is the linear attenuation coefficient of water. Decreases in moisture content (i.e., drying) can also be directly calculated by Eq. 11 by inverting $\frac{I_{wet}}{I_{dry}}$ to $\frac{I_{dry}}{I_{wet}}$.

Eq. 11 also provides a measure of the ability to resolve changes in concentration using the X-ray attenuation measurement technique, which is defined as the change in concentration required to attenuate a single X-ray photon. Eq. 12, from [14], describes concentration resolution mathematically.

$$R_{\Delta w} = -\frac{\rho_w}{\mu_w \cdot t} \ln \left(\frac{I_{dry} - 1}{I_{dry}} \right) \quad (12)$$

Eqs. 11 and 12 are central to the quantification of moisture contents in porous materials by X-ray attenuation, and both make use of the attenuation coefficient of water. Typically the non-interactive composite concept is accepted and the effective attenuation coefficient of water is either determined in isolation without interference from the porous material or, in many cases, experimental descriptions do not adequately describe which measure of attenuation coefficient of water is used for calculations of changes in moisture content [12, 14, 15, 21, 22]. This paper will show the former to be incorrect and indicates the latter requires more attention in future implementations of the X-ray attenuation measurement technique.

3. Experimental program

The goal of the experiments presented in this paper was to investigate whether an interaction exists between the attenuation provided by the porous material and the stored water. The effect of type and thickness of the parent material was investigated. Details on the materials tested, the X-ray measurement system, and measurements conducted are provided in the following sections.

3.1. Materials

Materials tested included various porous building materials, acrylic, steel, and aluminum. Porous materials included aerated autoclaved concrete, calcium silicate, clay brick, cement paste, concrete, and wood. Specimens with varying thicknesses were created either by stacking individual thin plates of the material (e.g., aluminum, acrylic) or by cutting (e.g., cement paste, clay brick). Aalborg white portland cement was used in cement paste and concrete specimens. The cement paste (0.40 water-to-cement ratio) was cured submerged in water for 28 days. Additional details on the concrete used is available in the literature [16, 20].

3.2. X-ray facility

A GNI X-ray system located at the Technical University of Denmark [34], consisting of an X-ray source and camera affixed to three programmable axes, was used for all measurements described here.

The X-ray camera consisted of a 25x25 mm² cadmium telluride (CdTe) semiconductor detector bump bonded to 252x256 16-bit complementary metal-oxide semiconductor (CMOS) pixel circuits [35]. CdTe, a direct conversion X-ray detector, converts X-ray photons to electric signals and is capable of doing so at room

temperatures. The 64,512 (252x256) CMOS pixel circuits record the location and number of photons detected over a set period of time, called the integration time (analogous to shutter time in visible-light photography). The number of photons detected during the integration time is the transmitted intensity, I (Eq. 2). CMOS pixel depth (maximum recordable I) was 65,536 (i.e., 2^{16}); therefore, integration times must be selected to avoid ‘overfilling’ pixels. The X-ray camera used is described in detail in [35].

Beyond transmitted X-ray photons, the X-ray camera detects background radiation sources, largely in the form of dark current. Other background sources (naturally occurring radioisotopes, cosmic rays, etc.) are minimal due to the materials tested and shielding chamber. Trial measurements of dark current indicated time and temperature variations, therefore, dark current was recorded prior to and subtracted from each X-ray attenuation measurement.

Additional details on the X-ray source [8] and other components of the X-ray equipment in its current configuration are available in the literature [20, 23].

3.3. Determination of attenuation coefficients of materials

Initial intensity, I_0 (transmitted intensity through air) was measured with varying X-ray source energies (30, 40, 50, 60, 70, 85 keV) and currents (20, 30, 40, 50, 60, 70 μA). Transmitted intensities, I were measured through varying thicknesses of the porous materials and isolated water using the same X-ray source settings to determine attenuation coefficients. The attenuation coefficient of water was also measured as illustrated in Fig. 1(b) by placing a 20 mm thickness of water (contained in acrylic containers) in series with specimens of varying material and thickness. All measurements conducted as part of this study were made with a warm-up time of 200 seconds, a stabilization time of 600 seconds, and an integration time of 20 seconds.

4. Results

4.1. Initial intensity of X-ray photon beam

Fig. 5 shows measured values of average initial X-ray photon intensity per second as measured by the X-ray camera (average of intensities measured by the 64,512 pixels) for varying X-ray source currents and energies. Eq. 13, which relates initial intensity to X-ray source current, i and energy, E_m , was found to accurately fit

Figure 5: Contour plot of the initial intensity I_0 as a function of the input X-ray source energy and current. The blue contour lines indicate measured values, while red contours indicate calculated values from Eq. 13.

Table 1: Values of coefficients C_{1-6} in Eq. 13.

Fitting coefficient	Value
C_1	-0.0187
C_2	1.502×10^{-4}
C_3	-0.0800
C_4	2.0283
C_5	1.0607
C_6	1.00236

measured initial intensity:

$$I_0 = (C_1 \cdot i) \cdot (C_2 \cdot E_m^4 + C_3 \cdot E_m^3 + C_4 \cdot E_m^2 + C_5 \cdot E_m + C_6) \quad (13)$$

where C_{1-6} are fitting parameters shown in Table 1. Eq. 13 is a polynomial fitting of measured results and therefore is only applicable for the investigated X-ray source inputs (i.e., $30 \leq E_m \leq 85$ keV and $20 \leq i \leq 70$ μA). This expression and the values for the coefficients may not be directly transferrable to other X-ray sources; however values for I_0 are needed to derive I_{dry} for determination of measurement resolution (i.e., Eq. 12).

4.2. Effective attenuation coefficients of materials

Fig. 6 illustrates the typical effects of X-ray source energy and materials thickness on effective attenuation coefficient, μ_{eff} . Measured values in Fig. 6 are indicated by symbols, while fits provided by Eq. 9 are

Figure 6: Influence of (a) X-ray source energy setting, E_m and (b) material thickness, t on effective attenuation coefficient. Measured values indicated by symbols, while lines indicate fits provided by Eqs. 7 and 8.

shown as the solid lines. Table 2 provides values for α , b^* , c^* , λ along with coefficients of determination (R^2) of the resulting fits. Fig. 6(a) indicates μ_{eff} -values decrease as X-ray source energy, E_m increases, and that the X-ray source energy-effect can be accurately estimated by Eq. 7 proposed in Sect. 2.2. Fig. 6(b) shows μ_{eff} -values may be affected by material thickness, depending on the type of material. For example, the thickness of wood has a minimal impact on μ_{eff} -values, while increased clay brick thickness causes significant reductions in μ_{eff} -values. Eq. 9, which considers the X-ray source energy-effect described by Eq. 7 and the beam

hardening-effect described by Eq. 6, provided a worst case R^2 -value of 0.861 for acrylic. The lowest R^2 -value for porous materials was 0.913 for aerated concrete. Alternative expressions to describe the beam hardening-effect were suggested in [32, 33]; however Eq. 6 was selected due to its inherent physical logic (i.e., beam hardening effect, $1 + \lambda \cdot t$ in Eqs. 6 and 9 equals 1 with zero thickness).

Figs. 7(a)-(d), which illustrate both the material thickness, t and X-ray source energy, E_m effects on μ_{eff} -values, show measured and fitted (using Eq. 9) μ_{eff} -values for water, calcium silicate, clay brick, and aluminum, respectively. Measurement points are indicated by blue symbols with the measured μ_{eff} -values indicated by the adjacent number. The red isolines show the fitted μ_{eff} -values provided by Eq. 9. Fitting parameters are provided for all materials in Table 2, including water. The impact of hardening coefficient, λ is indicated by comparison of Figs. 7(a)-(d) where λ increases from 0.888 m⁻¹ in (a) to 8.94 m⁻¹ in (b), 17.8 m⁻¹ in (c) and 57.7 m⁻¹ in (d). As λ increases, the effect of specimen thickness on the μ_{eff} -isolines becomes increasingly more significant – with only minimal changes in μ_{eff} -values as the thickness of water increases (Fig. 7(a)). For aluminum (Fig. 7(d)), thickness increase drastically reduces μ_{eff} -values. Fig. 6(b) also illustrates the impact of material type and thickness on μ_{eff} -values.

4.3. Coupled effect of parent material on effective attenuation coefficient of water

Fig. 8(a) indicates the influence of water and parent material thickness on measured values of the effective attenuation coefficient of water, $\mu_{eff,w}$. Calcium silicate in various thicknesses (0, 0.02, 0.04, and 0.08 m) was used as the parent material in this case while water thickness was also varied (approximately 0.01, 0.02, 0.04, and 0.06 m). While the effect of the parent material's thickness is evident, no clear trend was identified concerning the impact of water thickness. Increasing the water thickness from 0.01 to 0.02 appears to result in an increased $\mu_{eff,w}$ -value, followed by a subsequent decrease with increased water thickness. Measurement variability may explain the apparent differences with water thickness. However, Fig. 8(a) clearly shows a coupling effect of the thickness of the calcium silicate on the effective attenuation coefficient of water. Therefore, the term coupled effective attenuation coefficient of water, $\mu_{eff,w}(t)$; which is a function of the parent material thickness, t ; is introduced here.

Fig. 8(b) shows this coupling effect of the parent material on the effective attenuation coefficient of water

Figure 7: Comparison of measured and estimated (Eq. 9) effective attenuation coefficients for (a) water, (b) calcium silicate, (c) clay brick, and (d) aluminum as function of specimen thickness and X-ray source energy. Blue data points indicate measured points, while the red broken isolines indicate fitted values from Eq. 9.

Table 2: Values for parameters in Eq. 9 for various materials including the coefficient of determination (R^2) of the fits.

Parameter	Materials								
	Acrylic	Aerated concrete	aluminum	Clay brick	Calcium silicate	Cement paste	Concrete	Wood	Water
ρ [kg/m ³]	1186	422	2700	1795	271	1440	2200	480	1000
α	484.4	3999.8	3112.8	4442.7	5228.4	6750.4	3840.0	481.2	790.3
b^*					2.9				
c^*	0.022	0.075	0.060	0.052	0.078	0.064	0.106	0.020	0.022
λ [m ⁻¹]	3.97	13.6	57.7	17.8	8.94	12.4	9.00	0.863	0.888
R^2	0.861	0.913	0.948	0.990	0.976	0.991	0.953	0.999	0.987

Figure 8: (a) Influence of water thickness on measured coupled attenuation coefficient of water with an X-ray source energy of 85 keV measured through calcium silicate parent specimen with varying thickness and (b) coupled attenuation coefficient of water with an X-ray source energy of 85 keV with varying types and thicknesses of parent materials with symbols indicating measured values and lines indicating fits provided by Eq. 14.

occurs for all porous materials tested. The symbols in Fig. 8(b) indicate measured effective attenuation coefficients of water when the X-ray photon beam passed through varying thickness of the various parent materials prior to interacting with the water. As shown in the figure, the measured effective attenuation coefficient of water decreases from an average of 24.6 m^{-1} for a 0 mm thickness of parent material to as low as 17.8 m^{-1} for a 23.6 mm thickness of cement paste. It should be noted that values of $\mu_{eff,w}(t)$ presented in Fig. 8(b) were measured using a constant 0.02 m thickness of water as Fig. 8(a) indicates water thickness is of less importance. The exponential decay model described in Eq. 14 was found to accurately fit measurements:

$$\mu_{eff,w}(t) = \mu_{eff,w}(\infty) + [\mu_{eff,w}(0) - \mu_{eff,w}(\infty)] \cdot e^{-\eta \cdot t} \quad (14)$$

where, $\mu_{eff,w}(\infty)$ is the coupled effective attenuation coefficient of water through an infinite thickness of the parent material [m^{-1}], $\mu_{eff,w}(0)$ is the coupled effective attenuation coefficient through a zero thickness of the parent material [m^{-1}], and η is the parent material's coupling effect [m^{-1}]. The lines in Fig. 8(b) indicate the fits provided by Eq. 14 for the various parent materials. Table 3 lists the fitted values for coefficients and the coefficients of determination for the fits provided by Eq. 14.

5. Discussion

Comparison of results in Fig. 8(b) showing the coupling effect of the various porous materials and values for the hardening coefficient, λ of the porous materials presented in Table 2 indicates a potential relationship. Fig. 9 assesses this relationship, where the coupling effect is defined in accordance with Eq. 14 as $\ln[\mu_{eff,w}(0) - \mu_{eff,w}(\infty)] \cdot \eta$. Fig. 9 indicates the coupling effect tends to increase with the hardening coefficient of the porous material. Further investigations are required to verify and quantify this relationship. However, Fig. 9 and a comparison of results in Fig. 8(b) and Table 2 indicate a strong correlation between beam hardening and the reduction in the coupled effective attenuation coefficient of water.

Results presented in Fig. 8(b) necessitated the introduction a fourth attenuation coefficient of water, coupled effective ($\mu_{eff,w}(t)$), to describe the attenuation behaviour of water in composite systems. The lack of sufficient descriptions of fundamental mechanisms and the apparently previously undiscovered coupled effect has lead in many cases to unintentionally vague

Figure 9: Hardening coefficient, λ of the parent materials versus the coupling effect of the parent material on the coupled effective attenuation coefficient of water.

descriptions of experimental procedures and potential for mistakes when performing X-ray attenuation measurements with polychromatic X-ray sources. Specifically, a review of the literature yields little information on which attenuation coefficient of water was used for determination of moisture contents in many published results, and in some cases incorrect values being used. In [14, 15, 21, 22], the experimental procedure descriptions do not specify how or if an attenuation coefficient was measured or if tabulated (i.e., linear) values were simply used. Others [8, 12, 18] have correctly indicated the effective attenuation coefficient of water should be measured and used, but do not indicate if they accounted for the coupled effect of the parent material. Eq. 15, a modification of Eq. 11, therefore describes an improved calculation for concentration changes using a polychromatic X-ray photon source:

$$\Delta w = -\frac{\rho_w}{\mu_{eff,w}(t) \cdot t} \ln\left(\frac{I_{wet}}{I_{dry}}\right) \quad (15)$$

where $\mu_{eff,w}(t)$ is the parent material thickness-dependent (coupled) effective attenuation coefficient of water. The coupled effective attenuation coefficient of the water therefore must be directly measured for individual investigations, and tabulated values for μ_w must be avoided. The following procedure describes one method for determining values of $\mu_{eff,w}(t)$ when using a polychromatic X-ray photon source:

1. Measure the transmitted intensity through a conditioned (partially saturated or dried) specimen with given material type and thickness and an

Table 3: Values for parameters in Eq. 14 for various materials including the coefficient of determination (R^2) of the fits.

Parameter	Materials							
	Acrylic	Aerated concrete	aluminum	Clay brick	Calcium silicate	Cement paste	Concrete	Wood
$\mu_{eff,w}(\infty)$	21.6	19.5	18.5	18.0	18.6	17.5	118.2	22.4
$\mu_{eff,w}(0)$				24.63				
η	62.9	64.0	185.2	60.7	17.7	145.3	120.1	75.1
R^2	0.989	0.975	0.995	0.995	0.991	0.999	0.999	0.943

empty thin-walled acrylic (or similar) container with known inner dimensions at user-defined X-ray source setting(s), or I_e . Either a single wedge-shaped container or a series of parallel-walled containers with varying water thickness may be used for this purpose (or a combination of both). The maximum water thickness, t_w should, in either case, be similar to the anticipated maximum change in moisture content of porous material. Wedge-shaped containers provide $\mu_{eff,w}(t)$ -value determinations with a single measurement. However, as the water thickness varies along the height, careful alignment is required and only 252 measurement locations (number of pixels in a row) are averaged for each thickness. A series of parallel-walled containers requires multiple measurements, but provides 64,512 (252×256) measurements for a single water thickness. Parallel-walled containers were used here.

2. Fill the acrylic container with water or other material investigated [e.g., corrosion products, 23] and again measure the transmitted intensity through the conditioned specimen, acrylic, and water at the same X-ray source setting(s), I_f .
3. Calculate the coupled effective attenuation coefficient of water as the quotient of $-\ln\left(\frac{I_f}{I_e}\right)$ over the water thickness, t_w .

Alternatively, values for I_e and I_f determined by measuring the transmitted intensity through a dry and saturated specimen, respectively, would likely yield the same value for $\mu_{eff,w}(t)$.

Fig. 10 illustrates the impact of using various attenuation coefficients when computing changes in moisture contents. In this example, a 0.40 water-to-cement ratio cement paste specimen (28 days curing submerged in 20°C water) was dried through solvent exchange and subsequently exposed to liquid water from the specimen's top surface. Transmitted intensities were recorded from the dried specimen and repeatedly after exposure to water. The moisture profiles shown were recorded at the same time (after 8 days of exposure to

Figure 10: Example of impact of using different attenuation coefficients of water on measured change in moisture content. Data presented was collected after 8 days of exposure of liquid water to the surface of a dried (through solvent exchange) cement paste specimen using an X-ray source energy of 60 keV.

water), but moisture contents were computed using different attenuation coefficients for water. Attenuation coefficients for water included a tabulated (in [29]) value for the linear attenuation coefficient of water at 60 keV, 20.6 m^{-1} ; the effective attenuation coefficient of water at 60 keV, 27.6 m^{-1} (according to Eq. 9 and the fitting parameters presented in Table 2); and the coupled effective attenuation coefficient, measured to be 23.7 m^{-1} . Differences in moisture content (from correct values calculated using the coupled effective attenuation coefficient) as large as 31.8 kg/m^3 were found in this case.

Eqs. 11 and 15 indicate differences in the calculated moisture content are inversely proportional to the various attenuation coefficients. Table 4 provides an overview of the percentage difference that would result from using incorrect attenuation coefficients of water assuming the X-ray source energy is 85 keV, the parent specimen thickness is 0.02 m, and a water thickness

Table 4: Values for various attenuation coefficients of water in series with various parent materials and the potential error (%) in calculations of moisture content from X-ray attenuation measurements if the linear, μ_w or effective, $\mu_{eff,w}$ attenuation coefficient was used rather than the coupled effective attenuation coefficient, $\mu_{eff,w}(t)$.

Parent Material	Aerated concrete	Clay brick	Calcium silicate	Cement paste	Concrete	Wood
μ_w [m^{-1}]				18.04		
$\mu_{eff,w}$ [m^{-1}]				24.13		
$\mu_{eff,w}(t)$ [m^{-1}]	20.9	20.0	22.8	17.9	18.7	22.9
Error using μ_w (%)	15.8	10.6	26.5	0.7	3.9	26.9
Error using $\mu_{eff,w}$ (%)	13.5	17.4	5.5	25.8	22.4	5.2

of 0.01 m was used to determine the effective attenuation coefficient of water. For the materials investigated and with the stated assumptions, incorrect use of either the linear or effective attenuation coefficient for water would result in calculation errors of up to 26.9%. Table 4 clearly indicates that even the use of the effective attenuation coefficient of water, $\mu_{eff,w}$, measured without the parent material results in potentially excessive errors. Further, these results indicate verification of X-ray attenuation measured moisture content changes should be completed in future works using a comparative experimental technique. For example, gravimetric determination of moisture content changes from two ‘known’ conditions (e.g., moisture content change from a partially saturated to vacuum saturated conditions) could be compared to identical X-ray attenuation measurements. Such comparative experiments, while only reliably verifying a single moisture content change, would provide additional indications of the validity of the X-ray attenuation measurement technique and the importance of using the correct attenuation coefficient of water.

Eq. 16, a modification of Eq. 12, describes the concentration resolution when using the coupled effective attenuation coefficient of water.

$$R_{\Delta w} = -\frac{\rho_w}{\mu_{eff,w}(t) \cdot t} \ln \left(\frac{I_{dry} - 1}{I_{dry}} \right) \quad (16)$$

As shown in Fig. 8, the thickness of the water, t_w used for determination of $\mu_{eff,w}(t)$ -values appears to have a minimal impact. However, the water thickness should likely closely resemble the expected maximum change in moisture content of the parent material. In this way the determination of $\mu_{eff,w}(t)$ will also act as a check to ensure the X-ray source settings and specimen thickness selected will be able to detect anticipated changes in moisture content.

Using the results presented above, the measurement resolution can be calculated using Eq. 16. Values for I_{dry} are computed using Eq. 1, where I_0 is determined from Eq. 13 and values for μ_{eff} of the various porous

Figure 11: Resolution of moisture content changes for various materials and thicknesses with an X-ray source energy of 85 keV and current of 70 μA using fitted effective attenuation coefficients of the various building materials using Eq. 9 and coupled effective attenuation coefficient of water using Eq. 15.

materials determined using Eq. 9 and the regression coefficients in Table 2. Fig. 11 shows the concentration resolutions possible for the various parent materials using an X-ray source energy of 85 keV and current of 70 μA . The curves consider the beam hardening caused by the parent materials and the coupling effect on the effective attenuation coefficients of water, which occurs when polychromatic X-ray sources are used. For cement paste and clay brick optimal thicknesses are discovered, whereas for the other materials increasing the specimen thickness continues to improve measurement resolution for the studied conditions.

6. Summary and conclusions

This paper presents a detailed description of the controlling mechanism behind X-ray attenuation measurement using both monochromatic and polychromatic X-ray sources and non-energy discretizing X-ray cameras. Differences in measurements taken with monochromatic and polychromatic sources are described. Vari-

ous attenuation coefficients, including linear, average, effective, and coupled effective (for water only), were defined and described in order to shed light on possible mistakes made in previous investigations. It is concluded that using tabulated values of the linear attenuation coefficient, μ_w of water should not be used for calculating moisture content changes.

Additionally, a parametric investigation on material type, thickness and X-ray source energy settings on the ability to resolve changes in moisture content was presented. Results obtained through the parametric studies performed on aluminum, acrylic, clay brick, aerated autoclaved concrete, cement paste, concrete, calcium silicate, and wood indicated that:

- The effective attenuation coefficient of water is affected by the type and thickness of the parent specimen, necessitating the introduction of the coupled effective attenuation coefficient of water, $\mu_{eff,w}(t)$. Therefore, when utilizing the X-ray attenuation measurement technique to calculate moisture content (or other material concentration) changes, the attenuation coefficient of water must be directly measured while the parent specimen is in place. A procedure for determining $\mu_{eff,w}(t)$ is presented.
- It was found that calculations of change in moisture content (i.e., Eq. 15) may vary by up to 26.9% if the incorrect attenuation coefficient of water is used.
- Material-dependent optimization functions – in terms of ability to resolve water – have been developed for clay brick, aerated autoclaved concrete, cement paste, concrete, calcium silicate, and wood. These functions consider specimen thickness, X-ray source energy and current, beam hardening caused by the parent material, and the coupled effective attenuation coefficient of water. This extensive study provides a simple means for determination of proper specimen size and X-ray energy settings for a variety of materials.

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Nomenclature

- α Fitting parameter equivalent to $a^* \cdot Z_{eff}^{3.8}$ [-]
- Δw Change in moisture content [kg/m³]
- η Parent material coupling effect [m⁻¹]
- κ Pair production cross-section [m⁻¹]
- λ Beam hardening coefficient [m⁻¹]
- μ Linear attenuation coefficient [m⁻¹]
- μ_0 Initial average attenuation coefficient [m⁻¹]
- μ_w Linear attenuation coefficient of water [m⁻¹]
- $\mu_{eff,w}$ Effective attenuation coefficient of water [m⁻¹]
- $\mu_{eff,w}(0)$ Coupled effective attenuation coefficient of water with 0 m thickness of parent material, fitted [m⁻¹]
- $\mu_{eff,w}(\infty)$ Coupled effective attenuation coefficient of water with infinite thickness of parent material, fitted [m⁻¹]
- $\mu_{eff,w}(t)$ Coupled effective attenuation coefficient of water [m⁻¹]
- μ_{eff} Effective attenuation coefficient [m⁻¹]
- $\bar{\mu}$ Average attenuation coefficient [m⁻¹]
- Ψ_E Shape of photon energy spectrum [-]
- ρ Density [kg/m³]
- ρ_w Density of water [kg/m³]
- σ Compton cross-section [m⁻¹]
- τ Photoelectric cross-section [m⁻¹]
- a Fitting parameter describing photoelectric cross-section [-]
- a^* Fitting parameter describing effective photoelectric cross-section [-]
- b Fitting parameter describing photoelectric cross-section [-]

b^* Fitting parameter describing effective photoelectric cross-section [-]

c Fitting parameter describing Compton cross-section [-]

c^* Fitting parameter describing effective Compton cross-section [-]

C_{1-6} Fitting parameters [-]

E X-ray photon energy [keV]

E_m X-ray source energy (maximum photon energy produced by polychromatic X-ray source) [keV]

f_i Fraction of element i [-]

I Transmitted intensity [counts]

i X-ray source current [μ A]

I_0 Initial intensity [counts]

I_e Transmitted intensity through parent material and empty container [counts]

I_f Transmitted intensity through parent material and container filled with water or other substance being investigated [counts]

I_{dry} Transmitted intensity through a conditioned (dry or partially saturated) porous material [counts]

I_{wet} Transmitted intensity through a wet porous material [counts]

$R_{\Delta w}$ Resolution of change in moisture content [kg/m^3]

t Parent material (specimen) thickness [m]

t_w Thickness of water [m]

x Incremental thickness [m]

Z_{eff} Effective atomic number [-], $Z_{eff} = \sqrt[3.8]{\sum f_i Z_i^{3.8}}$

Z_i Atomic number of element i [-]